Technical Toport: NAVTP ADEVCES 1205-

# SIMULATION OF HELICOPTER AND VISTOL AIRCRAFT

## COMPUTATIONAL METHODS

Study, Equations of Motion of Vertical/Short Take-Off and Landing Operational Flight/Weapon System Trainers

I. A. Castle A. L. Gray Walter McInters

Melpad, inc. 3000 Arlington Bouleyard Falis Church, Virginia

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#### SECTION I

#### INTRODUCTION

The economical production of helicopter simulators is a complex problam in which experience is not as widespread as in the fixed-wing field. The simulation of small perturbation reaction as practiced by helicopter manufacturers may be sufficient for their purposes, but it is impossible to extend this approach to the unrestricted case without gross modifications. As a matter of history, these modifications appeared to be of such magnitude that prior to the design of the first full flight regime helicopter trainer (Davice 2F54, H-37A Helicopter) Melpar, Inc. sought a more analytical scheme for the expressions of helicopter flight. The investigation took full advantage of earlier work performed at NACA and various other institutions and agencies. As a result of this effort the Modified Flads Element Approach was developed and was further expanded and improved during the development of the RSS-2 WST, Device 2Fou. Further extensions and simplifications of the technique were then applied to the HRB-1 OFT. Device 2775. The equations utilised by the Modified Blade Element Approach are developed in reference 1.

A variety of sources have, in the past established criteria for the selection of computer components and systems for aircraft simulation. Their diagnosis has been thorough and well-established. Mark E. Connelly in Computers for Aircraft Simulation, Report 7591-R-2, developed under ONR Contracts N5 ori-07895 and N61339-45, produced a remarkable presentation of analog computer component analysis. No attempt will be made here to repeat or improve on that analysis. References will be made to Mr. Connelly's report and in places injections of practical considerations and variations imposed by the chosen method of helicopter simulation will be made which influence choices of computer components. After a review of computer components, the chosen components will be employed in the simulation task.

#### SECTION II

#### ASPECTS GOVERNING THE CHOICE OF THE OPTIMUM ANALOG COMPUTER

This volume will present recommendations derived from the study of the simulation equations as set forth in Volumes I and II. The recommendations are intended as a guide to the selection of an optimum analog mechanisation for the single rotor helicopter, tandem rotor helicopter, and tilt-wing simulation equations. No attempt will be made here to present an analysis of analog computer characteristics. Sufficient study reports exist that adequately present the details of analog computer techniques, and reference will be made to these reports in support of certain technique selections in the optimisation of the mechanisations.

In the selection of a computer type to be used for aircraft simulation purposes there are several factors that must be considered to arrive at an optimum selection. The optimum computer must have, first of all, a means of communication in order to accept input data which describes the simulation problem and defines the aircraft operational characteristics. Secondly, the simulation equations which describe the problem parameters must be able to be simplified to the extent required by the problem accuracy and still be expressed in the machine language. A third consideration is the need for computer flexibility in order to accept the anticipated aircraft manufacturers design changes. The computational requence, dictated by the optimum use of components and the type of computer, is a fourth point of consideration. The fifth and most important factor is the choice of carrier to be used in the computer.

#### A. AIRCRAFT DATA CONVERSION FOR USE IN THE COMPUTER

Considering the first point mentioned above, it has been the writer's experience that the aircraft data supplied by the sircraft manufacturers is, of necessity, empirical in nature. For instance, the coefficient of lift versus angle of attack curves for rotor airfoils are plots of wind tunnel empirical data. Since this data is predominantly empirical and presented in the form of smooth curves as functions of one or two variables, the introduction and storage of these functions is particularly suited to analog function generation techniques.

These techniques, as the reader well knows, are manifested in several different forms such as tapped or shaped potentiometers or some form of electronic function generators, such as diods function generators. These techniques usually produce straight line approximations of the desired function. The accuracy of the approximation is determined by the number of break points selected during the design.

The person selecting the method of function generation to use in the computer should take into consideration the required simulation accuracy and flaxibility of the chosen method as well as cost considerations. The present state-of-the-art (reference 4) provides the serve potentiometer as the most economical means of generating slowly varying

functions, like the aerodynamic functions required in OF/WST's. The electronic methods provide a more accurate and flexible method but at a higher cost.

The optimum choice of function generation recommended for the V/STOL simulation then is the serve potentiometer, since this is the most economical method and provides sufficient accuracy for the desired simulation. Once the choice has been made to use potentiometers the data conversion aspects do not bear any further on the choice of the computer since potentiometers are equally useful in either an AC or DC carrier computer.

#### B. SIMPLICITY OF SIMULATION EQUATIONS

The mechanisation of unabridged equations of motion for an OFT will produce a needless superfluity of equipment that is completely out of proportion to the amount required to provide adequate training. Consequently it is highly desirable to simplify the equations of simulation to the extent that an optimum balance exists between the information supplied by the equations and the information required for training purposes. For instance, in Volume I (reference 1) equations 5-25a, b, and c give the complete expressions for velocities in the X body axes as

In order to simplify the expressions and provide a less complex mechanisation it was noted that  $\mathbb{U}_G$  is usually the predominantly large valocity. Consequently the contributions of the  $\mathbb{V}_G$  and  $\mathbb{W}_G$  cross-coupling terms may be omitted giving the final expressions

$$v_{G} = \int (\frac{x_{a}}{M_{1}} - g \sin \theta) dt$$

$$v_{G} = \int (\frac{x_{a}}{M_{1}} + g \cos \theta \sin \Phi - v_{G}r) dt$$

$$v_{G} = \int (\frac{z_{a}}{M_{4}} + g \cos \theta \cos \Phi + v_{G}q_{1}) dt$$

as given by 5-26 of Volume I.

Although this simplification does alter the validity of the expressions, the errors caused in the final velocities are negligible and not detectable by the student and consequently the same training value is obtained with less hardware than if the simplification had not been made. In this manner, the balance between input and output information is achieved.

The extent of simulation required by the trainer specifications is the limiting factor that controls the extent of simplification of the simulation equations. In general, the hardware reduction bears a direct proportion to the amount of simplification of the simulation equations. Consequently, the simplification of the equations does not influence the choice of the computer but only reduces the complexity of the final mechanisation.

#### C. COMPUTER FLEXIBILITY

The flexibility of a computer is the ease with which the computer can be reprogrammed to perform a different computation. In the design of OF/WST's the procuring agency usually desires the development of the trainer to be performed concurrently with the development of the aircraft being simulated. This necessitates a close liaison with the aircraft manufacturer in order to keep abreast of design changes required during the aircraft development. Consequently, the design of the OF/WST must include a consideration of the flexibility of the selected computer in order that airframe design changes may be quickly and afficiently incorporated into the OF/WST design.

Fortunately the changes made by the sirframe manufacturers are usually slight modifications to the numerical functions describing the aerodynamics, such as the coefficients of lift and drag. In an analog computer these functions are formed by tapped or shaped potentiometers on the various servo shafts. A change in these constants would result in OF/WST modification to the associated potentiometers and amplifier gain adjustments. If as in section II.A the choice is made to use potentiometers as function generators, no flexibility advantage is realised in either an AC or DC carrier computer. Consequently, the flexibility consideration does not affect the choice of analog computer for the OF/WST.

#### D. COMPUTATIONAL SEQUENCE

The computational sequence formed by the interconnection of the computational elements directly affects the optimum use of components no matter what type of computer is selected for the OF/WST. This is obviously true if one considers the result of forming a computational sequence without regard to optimum component use. For example, the expression for the HSS-2 landing gear pitching moments is given in Volume I as

$$M_{LO} = 4.38(F_{RW} + F_{LW}) = 13.99 F_{TW} + 5.36 X_{LO}$$

This could be mechanized by first forming  $(F_{RN} + F_{LN})$  as the output of a summing amplifier and then scaling 4.38  $(F_{RN} + F_{LN})$  at the input of a second summing amplifier which sums 4.38  $(F_{RN} + F_{LN})$  with -18.99  $F_{TN} + 5.36 \, I_{LS}$ . Obviously the optimum sequence that should be used here is to scale 4.38  $F_{RN}$  and 4.38  $F_{LN}$  separately into a single summing amplifier with -18.99  $F_{TN} + 5.36 \, I_{LS}$  and thus eliminate one summing amplifier. While this is an extremely obvious example it does illustrate the value of sequence considerations for component optimisation.

Commutational sequence also affects the extent of simulation achievable with a given computer. Since a finite response time is inherent in each individual computational element, the accumulative response time of a complete computational loop must be matched to the response times of the system being simulated if a realistic simulation is to be achieved. For example, the CH46-A tandem-rotor helicopter response is such that a 1.58 inch step input of longitudinal forward stick deflection will produce a maximum pitch acceleration of 24 degrees per second2, and the time to reach this maximum acceleration is 0.33 seconds after initiation of the stick deflection. If the simulator is to present a realistic simulation of this computational loop the pitch rate servo,  $q_1$ , must exhibit at least the response indicated above, if a similar step imput to the longitudinal stick is applied to the simulator. This will certainly occur if the computational sequence is arranged to minimize the computational elements and the response times of the q integrator shaft is scaled to produce the required loop response.

Thus, it is evident the computational sequence is an extremely important aspect as far as obtaining a minimum component quantity for an optimum response match. However, it has very little bearing on an optimum choice of computer type, as an AC or DC carrier.

#### E. CHOICE OF CARRIER

The choice of the carrier to be used for a particular simulation computer design is by far the most important aspect to be considered in the selection of an optimum computer. There are three possible solutions that may be decided upon. They are, namely, an AC carrier, a DC carrier or a hybrid AC-DC combination. One additional decision must be made in the event an AC carrier is to be used, and that is the frequency of the AC carrier.

Let us first consider the AC carrier computer and decide which frequency is best suited for application in V/STOL aircraft simulation. The most stringent requirement of the computer is the response characteristics dictated by the angular rates and accelerations of the aircraft to be simulated. Table 1 is a comparison of maximum rates and accelerations of fixed wing and helicopter type aircraft. The fixed wing aircraft values are taken from the MIT-Whirlwind and the Goodyear-Cyclone program (pages 174-175, reference 4). The helicopter angular

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r (yew acc.)	q (pitch acc.)	p (reli acc.)	p (roll rate) q (pitch rate) r (yes rate)	
+ 4.47 to -2.82 red/sec <sup>2</sup>	+ 5.94 to 4.10 rad/sec 2	+ 36.8 to -20.85 rad/sec <sup>2</sup>	MIT - Whirlwind  + 6.3 to -7.8 rad/sec  + .86 to -1.0 rad/sec  + 1.12 to13 rad/sec	
+ 5 rad/sec <sup>2</sup>	+ 8 to -5 rad/sec <sup>2</sup>	+ 40 rad/sec <sup>2</sup>	doodysar-Cyclone  10 rad/sec 1 rad/sec 1.2 rad/sec	
+ 1.5 rad/sec <sup>2</sup>	+ 1.5 rad/sec <sup>2</sup>	± 3.3 rad/sec <sup>2</sup>	Single Rotor HSS-2  + 2.4 rad/sec + 1.44 rad/sec + 1.28 rad/sec	
+ 1 rad/sec <sup>2</sup>	± 5 rad/sec <sup>2</sup>	+ 3 rad/sec <sup>2</sup>	Tandem Rotor Vertol HRB-1  ± 2 rad/sec  ± 3 rad/sec  ± 5 rad/sec	

Table 1. Comparison of Fixed Wing and Helicopter Maximum Angular Rates and Accelerations

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rates and accelerations are those used in the HSS-2 flight trainer and those furnished to Melpar by Vertol Division of Boeing Aircraft for the CH46-A flight trainer. It is easily seen that there is a great difference in the maximum response capabilities of the fixed wing aircraft and the helicopters chosen. Likewise there is a variation in the computational speed requirement of flight simulator computers for helicopter and fixed wing aircraft.

Assuming that the response of a 60 cycle system is marginal in fixed wing applications, it can be seen in Table 1 that a 60 cycle system is better than simply marginal for helicopter simulation since none of the helicopter angular rates and accelerations in Table 1 are as large as the fixed wing rates and accelerations. Note that  $\mathbf{q}_1$ ,  $\dot{\mathbf{q}}_1$ ,  $\mathbf{r}$  and  $\dot{\mathbf{r}}$  are not too different from helicopter to fixed wing, however there is a marked difference in  $\mathbf{p}$  and  $\dot{\mathbf{p}}$ . The required computational speed is based on the highest single rate and acceleration, i.e. roll rate and roll acceleration for the fixed wing aircraft.

Chapter II, page 25 of reference 4 gives an analysis of servo systems and concludes that 400 cycle serves should result in a serve response that is three to four times better than is possible with a comparable 60 cycle system. This is quite true, and one may wonder why bother with 60 cycle systems if 400 cycle systems offer such improvement in response as well as accuracy and size. Both large and small computers have successfully utilised 400 cycle systems. For example, operational airborne computers are predominantly 400 cycle systems, also large operational shipboard fire control systems operate from a 400 cycle carrier. If such systems are developed, then why should flight trainer manufacturers be hesitant to discard a 60 cycle carrier system? Unlike the manufacturer of operational tactical systems the flight trainer manufacturer does not develop flight trainers with weight and size reductions as a prime design goal. Neither does the prototype serve simply as a production model. What argument then can induce a simulator manufacturer to discard an operational 60 cycle system to develop 400 cycle systems with little hope of operational improvement? Before discussing this development consider another point before the problem is considered from a broad viewpoint. Suppose the case arises where the carrier system employed introduces reduced fidelity into the system at maximum acclerations, but operates at a sufficiently high response to follow satisfactorily the highest accelerations or rates that one would normally expect-which may be quite different from the maximum. Compared to other aspects of the trainer how important is maximum fidelity in this extreme operating region? These regions are most often reached just before a crash situation occurs. Very little, if any, actual training is accomplished at the extreme operation region of the aircraft. Regardless of the importance of highly accurate simulation in these areas, the decisions concerning the choice of carrier frequency are based on a balance of performance and cost.

Progressing from the earlier assumption that the response of either a 60 or 400 cycle system is sufficient for helicopter simulation, but

that a 400 cycle carrier offers a greater response margin of safety, consider some other factors that affect the choice of carrier frequency. Factors influencing carrier frequency choice are listed on pages 26 and 27 of reference 4. The statements contained in reference 4 are very true but the injection of some practical considerations may lead to a more selective choice of carrier frequency. The seven factors which follow are similar to those listed in reference 4.

- 1. 60 cycle power is widely available; 400 cycle power must be generated at the OFT in kilowatt quantities and in some cases, with undistorted waveshape and carefully controlled phase.
- 2. A 400 cps carrier produces a smaller and lighter weight computer. This, of course, is the primary reasoning behind the adoption of a 400 cps carrier for airborne and shipboard equipment, but is seldom highly influential in flight trainer design unless space for some special reason is at a premium.
- 3. The problem of phase shift (due to stray capacitance and inductance) and pickup is more likely to occur in a 400 cps system than in a 60 cps system. As reference 4 points out, pickup may be eliminated by proper engineering precautions such as the maintenance of low driving impedance levels, shielding, and careful placement of wiring. This sounds easy to accomplish, but the consideration of the practical aspects of the accomplishment may be enlightening. We must remember that OFT prototype development periods are commonly 16 to 18 months, and the present trend is toward fixed-price contracts. Shielding, for example, should be avoided whenever possible for a number of reasons. First, shielded wires produce as many maintenance troubles (which lead to an increase of computer cost with no increase in design) as any other single factor, particularly in the course of prototype debugging, where wiring is constantly being flexed. The ferrules at the end of each shielded wire cut through the insulation shorting the conductor to the shield and consequently to ground. Each time this occurs, the trainer is turned off and check-out halts. Components are also lost, particularly potentiometers where the wiper becomes grounded due to a fault in the shielded cable. Shielded cable is also costly, bulky, stiff and generally very difficult to work with particularly in large quantities. Another point to consider here is the difficulty of simultaneously reducing stray capacitance and using shielded cable. Available shielded cable has a capacitance of approximately 100 unf per foot. Extremely long cable runs are sometimes necessary especially in two trailer trainers. If these cable runs are shielded then suffer amplifiers must be used to reduce the source impedance sufficiently to minimize phase shift. High impedance wire-wound potentiometers also produce conditions (high source impedance and high inductance) which leads to further phase shift.
- 4. The fact that most aircraft instruments utilize a 400 cycle carrier is of no consequence since a 400 cycle synchro transmitter may be driven by a serve operating on any desirable carrier. With the present trend of reducing GFE, instruments are generally built to any carrier specified by the contractor.

- 5. Amplifier design for a 400 cps system will be simpler in that the lower sideband component of any reasonable signal does not approach zero frequency as it may in the case of a 60 cps system. Particularly in the case of transistorized amplifiers, a 400 cycle center frequency is easier and cheaper to obtain than a 60 cycle midfrequency.
- 6. Tachometers to .03% linearity as discussed in reference 4 are very expensive and greatly exceed the requirements of present-day training devices. Tachometer linearities in the order of 1% with zero speed voltages as low as 9 millivolts are much more common. These may be more cheaply obtained either as 400 or 60 cps units.
- 7. The seventh factor discussed in reference h states the advantages of using magnetic amplifiers to reduce the power and maintenance requirements. The following reductions were realized in a study by Goodyear Aircraft Company: number of tubes--54.5%, power consumption--56.25%, size--46%. Since the advantage may be realized only while employing a 400 cycle carrier, it is implied that this is an advantage that should be credited to a 400 cps carrier. A good deal of these advantages are dependent upon the size and characteristics of the tube type amplifiers. There is also the unanswered question as to whether or not a conversion to transistor circuitry would not have produced equivalent or larger reductions of maintenance and power consumption.

It is recommended then from the above that if an AC computer is selected for the V/STOL mechanization a 60 cycle system should be chosen. While it is true that a 400 cycle system would provide a definite advantage in response and accuracy, it is felt that these advantages are overshadowed by the reduced response requirements of the V/STOL aircraft frequencies. Also the de-emphasis of computer size restrictions in simulators and the maintenance and phase shift problems introduced by 400 cycle carrier further enhance the 60 cycle carrier choice.

Having selected the frequency of the carrier in the event that an AC computer is chosen the choice must now be made between an AC carrier, a DC carrier, or an AC-DC hybrid computer. First, let us make a comparison between AC and DC computers on the basis of the various computational techniques. Reference 4 gives an excellent discussion of the relative merits of AC and DC techniques. A summary of each of the discussions is presented here in support of the choice between AC and DC computers for the V/STOL mechanization.

1. AMPLIFICATION. Amplifiers occur in very large quantities in OF/WST analog computers due to the fact that they are used in so many different applications, such as isolation, summation, servo motor drive, inversion, etc. Consequently, the AC amplifier is afforded a large advantage over the DC amplifier in quantity required for a given mechanisation, since the AC amplifier can produce both polarity outputs by virtue of its center-tapped output transformer. The DC computer requires two separate amplifiers whenever both signal polarities are required. Also, DC amplifiers have an inherent drift problem and require a special consideration in the design to insure that adequate regulation is

provided by the power supplies. This is not required during the design of the AC computer. Due also to the drift problem, BC amplifiers are usually more complex, since stabilisation circuits are required. The only advantage of the BC amplifier over the AC amplifier is its ability to form various transfer functions by the use of passive network. Consequently, the advantage definitely lies with the AC computer as far as amplification is concerned.

- 2. INTEGRATION. DC electronic integration techniques have several decided advantages over AC servo integration methods. The DC technique can integrate much higher frequency signals, have a much higher dynamic range, have a smoother output, cost less and require less space and power. One feature, however, prevents them from being suited to OF/WST application. That is their inability to perform long term open loop integrations as is required in the integration of the Euler angle derivatives for instance. This application requires an angular output of unlimited range which can only be obtained with servo integrators. While a DC servo integrator can be used a DC tachometer is required to provide a response better than an AC servo integrator. Unfortunately, this increases starting and running friction. As far as integration techniques are concerned then AC servo integrators are slightly more desirable for the V/STOL mechanisation.
- 3. MULTIPLICATION. No advantage lies with either AC or DC systems in performing multiplication operations, since nothing can compete economically or from the standpoint of versatility with the serve potentiometer.
- 4. TRIGONOMETRIC RESOLUTION. The use of AC resolvers for coordinate resolution as opposed to sine-cosine potentiometers provides greater accuracy, greater resolution, longer life, and less friction. If the poorer conformance of sine-cosine potentiometers to the trigonometric functions can be tolerated then trigonometric resolution can be accomplished in an AC system more economically using potentiometers rather than resolvers. This can be seen by considering that both the resolver and the potentiometers require two input and two output amplifiers. Even though it's true that the summing of components takes place internally in the resolver, the potentiometer outputs can be summed in the succeeding input amplifiers. The AC techniques definitely have the advantage here.
- 5. FUNCTION GENERATION. Economically and versatility-wise the servo potentiometer has the advantage here. Consequently, AC or DC systems are equally optimum since potentiometers can be used in either system.

On the basis of the marits of the computing techniques described above it appears that the AC carrier computer would have the advantage over the DC carrier computer in the mechanisation of the V/STOL aircraft. In all of the areas discussed, except function generation and multiplication, the AC methods would appear to be the more optimum. In the mechanisation of some of the supersonic fixed wing aircraft, where the signal frequencies that would be encountered were expected

to be much higher than one or two cycles, some of the hybrid methods of DC integration followed by an AC position shaft or DC electronic function generation might be more applicable. In general, it has been the experience of the writer that if the requirements of the simulation problem are such that either an AC or TC carrier computer is adequate to perform the simulation, then the only thing that is achieved by combining AC and DC techniques is additional equipment. This additional equipment is required to make up the AC-DC interface.

It is therefore recommended, on the basis of axamination of the merits of the various techniques, that the optimum mechanization for the V/STOL aircraft would be a 60 cycle AC computer. Section III will examine the mechanizations in detail from the standpoint of optimum sequence and optimum cost and complexity.

#### SECTION III

#### MECHANIZATION OF EQUATIONS OF MOTION

#### A. GENERAL MECHANIZATION

This section deals with the mechanization of the equations of motion for helicopter and V/STOL aircraft. The mechanizations of these aircraft will reflect the use of 60 cps AC, 400 cps AC, DC and possible AC-DC hybrid carrier frequencies, however the flow charts in this section are developed for an AC mechanization with explanation of additions or deletions to these flow charts that are necessary to form flow charts for DC and AC-DC mechanizations. To aid in this extensive task a general flow chart independent of aircraft type and applicable to either helicopter or V/STOL aircraft is developed. In Figure 1 areas of mechanization are the blocks containing a bracketed number i.e. (1). The second task is then to develop the blocks in Figure 1 that are dependent upon the particular aircraft type. This leads to the helicopter and V/STOL mechanizations. Tabulations of the various components necessary to mechanize the various blocks in Figure 1 will be made as a function of AC or DC mechanization so that conclusions regarding optimum mechanization can be made in Section IV.

Before developing the blocks in Figure 1 that have identical representation for any aircraft in this section, a few ground rules will be established. Imputs to a block are described by arrow heads intersecting the blocks and outputs are defined as lines intersecting a block. Table 2 contains definitions of numbered blocks in Figure 1 and Table 3 establishes the meaning of the symbols in the mechanization flow charts. In the actual mechanization all imputs for a particular flow chart are assumed to be previously generated. Each block in Figure 1 will be considered in the following paragraphs.

- Hock (1) Pilot Control. The signal inputs that will be shown for the various aircraft will be due to control stick movements. The particular signal inputs will be observed as inputs to Block (4) for each aircraft described. Inputs to Block (2) are not considered.
- Block (2) Engine Simulation. The signal imputs to Block (4) from the Engine Simulation represent the required performance output parameters. Simulation of engines is not described in this report; only the specific output terms necessary for the simulation of the particular aircraft.
- Elock (3) Aero Variables. The serodynamic (Aero) variables are generated by signals that complete the major loop in the computer representing the aircraft equations of motion. Block (8) for the V/STOL aircraft and Elock (12h) for the helicopters feedback the velocities U, V and W to Block (3). Block (10) or Elock (12) feed back the pressure altitude (h,) to Elock (3).
- Hock (4) Aero Terms. In this block the aerodynamic equations are formed that will result in the generation of the aerodynamic forces ( $X_a$ ,  $Y_a$  and  $Z_a$ ) and moments ( $L_a$ ,  $M_a$  and  $M_a$ ). The mechanisation representing

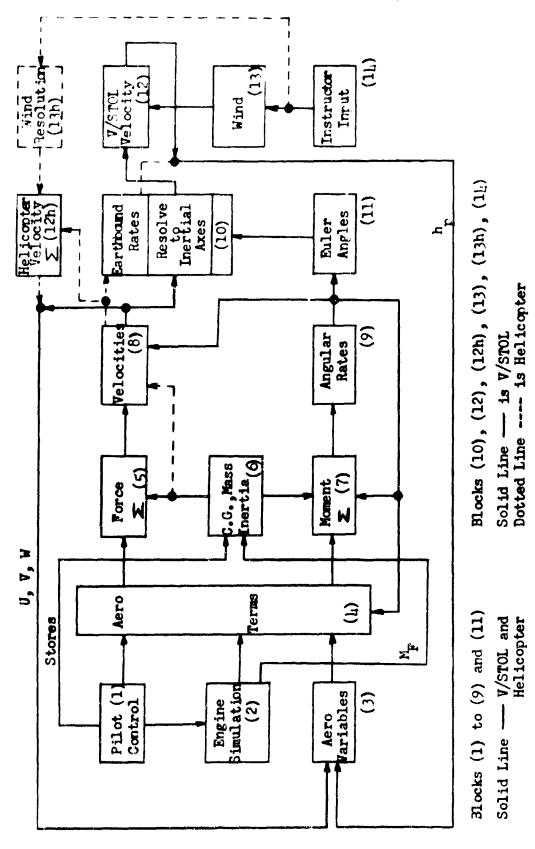


Figure 1. General Block Diagram

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HELICOPTER		V/STOL AIRCRAFT		
(1)	Pilot Control	Pilot Control		
(2)	Eng_ne Simulation	Engine Simulation		
(3)	Aerodynamic Variables	Aerodynamic Variables		
(4)	Aerodynamic Terms	Aerodynamic Terms		
(5)	Force Summations	Force Summations		
(6)	Center of Gravity (c.g.) Mass, Inertia	Center of Gravity (c.g.) Mass, Interia		
(7)	Moment Summations	Moment Summations		
(8)	Linear Velocities	Linear Velocities		
(9)	Angular Rates	Angular Rates		
(10)	Form Earth Axis Velocities	Resolve Linear Velocities to Inertial Velocities		
(11)	Formation of Buler Angles	Formation of Euler Angles		
(12)	***	Summation of Wind and Aircraft Inertial Velocities		
(12h)	Summation of Wind and Body Axis, True or Ground Velocities	****		
(13)		Wind Inputs from Instructor		
(13h)	Resolution of Wind Imputs to Body Axes			
(14)	Instructor Input	Instructor Input		

Table 2. Riock Terminology

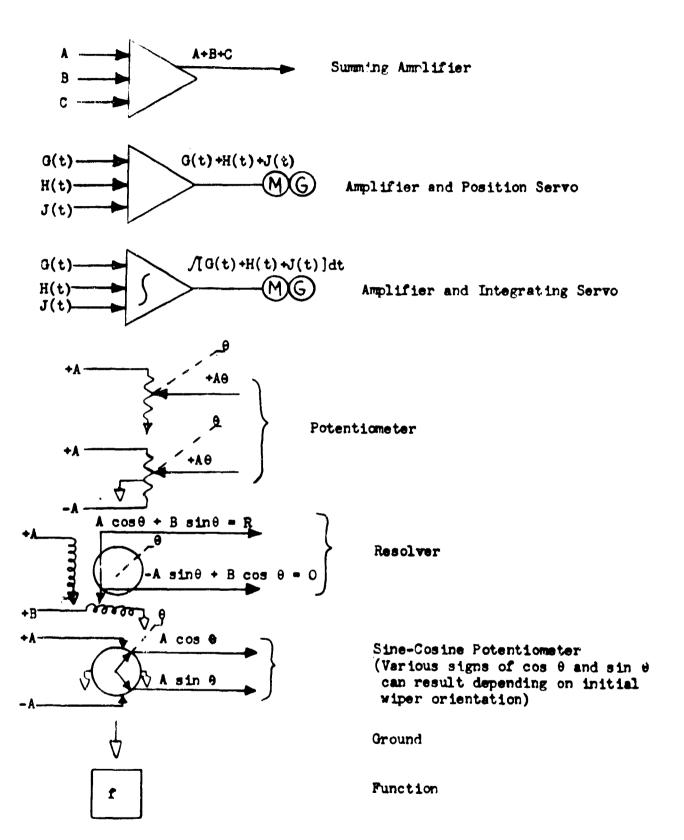


Table 3. Symbols Used in Mechanization

the Aero terms will be shown for each particular aircraft further on in this section.

Block (5) Force. The force summations are basically the same for all aircraft. Each force component  $(X_a, Y_a \text{ and } Z_a)$  has an associated summing amplifier. The inputs from Block (4) are the important portion of the mechanisation.

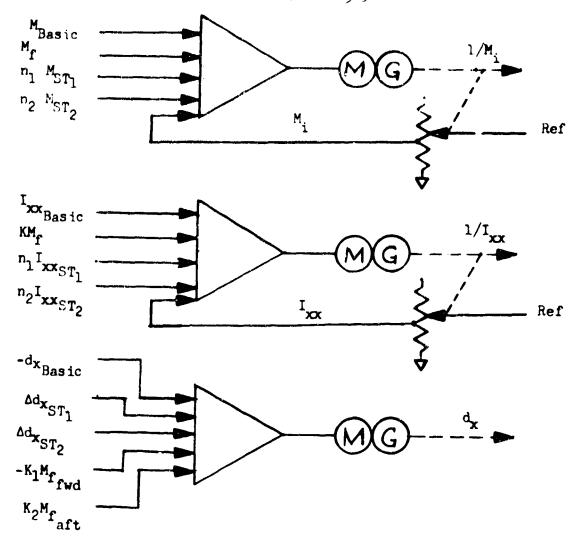
Hock (6) Mass, C.G. Mass (M) and center of gravity (c.g.) location are obtained as servo shaft positions. This mechanisation involves simple summation. In Figure 2 notice that the feedback potentiometer is connected for division operation for mass mechanisation. The shaft position is then an inverse function (1). This is done to avoid the scaling

computations required for potentiometer divisions since M is used as a divisor in its associated equations. Shift in c.g. in Figure 2 is along the x-body axis and is denoted by dx. Usually c.g. shifts along the x-body are the only shifts considered, however if a c.g. shift in the y or z body axis is important for a particular aircraft, it will be mentioned at that time.

Elock (7) Moment. The moment summations are basically the same for all aircraft. Each moment component  $(L_a, M_a, N_a)$  has an associated summing amplifier. The inputs from Block (4) are the important portion of the mechanization.

Block (8) Velocities. In block (8) the interest is in developing the linear velocities (U, V and W). These are computed by summing the respective force (X, Y or Z) divided by the mass of the aircraft with the appropriate gravity and angular rate effects and then integrating. Figure 3 shows the three integrations to get  $V_G$ ,  $U_G$  and  $V_G$  with associated inputs. Servo shaft positions are not required to mechanise these velocities but since Figure 3 is for an AC mechanisation, servo shafts are required for the integrators. The integrations could have been done DC just as well and more economically. Choice of AC or DC should not be made at the subsystem level—but for large computation areas. This will be done in the summary.

Elock (9) Angular Rates. Having computed the moments in Hlock (7), the calculation of the respective angular rate (p, q, or r) is accomplished by the integration of the respective moment which has been divided by the proper inertia term. Integrations can be performed by AC servo, DC servo or DC resistive capacitance circuits. Hlocks (4) and (7) are the important determinants as to whether to use AC or DC in mechanisation. Consequently, the development of Aero Terms as well as the summary mechanisation considerations of Section III will have a decisive influence on the way in which the integration is performed.



Where:

K = distance from c.g. to centroid of fuel mass

M = Mass

Subs:

Basic - based on design weight empty

n<sub>1</sub> or n<sub>2</sub> = number of stores of Type 1 or 2

ST<sub>1</sub>, ST<sub>2</sub> = stores, Type 1 or 2

Figure 2. Center of Gravity (c.g.) Mass, and Inertia

forward and aft, respectively

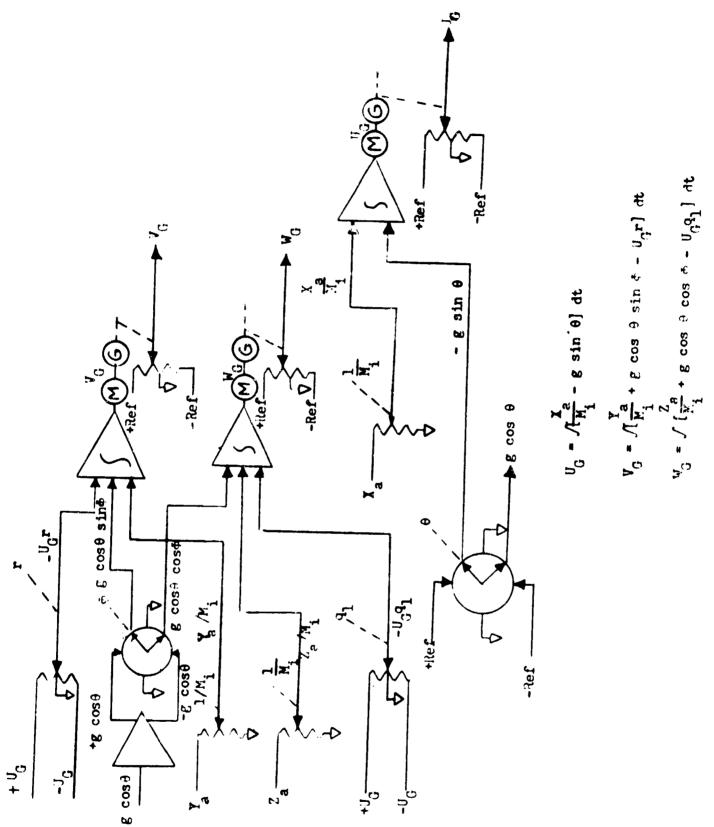


Figure 3. Velocity Integration AC Mechanization

Block (10) Resolve to Inertial. Body axis velocities (U, V, W) for V/STOL aircraft are resolved to the inertial frame through the Euler angles ( $\theta$ ,  $\theta$ ,  $\psi$ ) then added to instructor inputs to give the earthbound rates. For the helicopter, ground velocities (U<sub>G</sub>, V<sub>G</sub>, W<sub>G</sub>) are resolved in Block (10) to form earthbound rates. Figure 4 shows an optimum mechanisation for this resolution. Resolvers have been chosen to perform the coordinate resolution to the inertial frame since it is necessary to provide the accuracy to insure reliable integration for position. The integrators in Figure 4 must have the capability of long integration times, since these outputs are generally used for plotting boards and altimeters.

Block (11) Euler Angles. The computation of Euler angles is a combination of coordinate resolution and integration. Figure 5 is an AC mechanisation using resolvers and AC servos for integration. Figure 6 is a DC mechanisation using DC amplifiers, sine-cosine potentiameters and DC electronic integrators followed by DC position servos.

	AC		DC	
Component	No.	Wt.	No.	Wt.
Amplifier	7	7	12	24
Servo	3	21	3	21
S-C Pots	2	1/2	LL LL	1
Resolvers	1	1/2		
Complexity	13	29	19	46

Table 4. Buler Angle Tabulation

The weight factor, (Wt.) of components, in Table 4 are those used by Connelly in references 3 and 4. The weighting of components will be used for later evaluation of mechanisations. The weight factors are as follows: an AC amplifier is one (1), a DC amplifier is two (2), AC and DC servos are seven (7), a potentiometer is one-fourth (1/4), a resolver is one-half (1/2) and function generation is unspecified as to weight, but is specified by number (no.). Any function generation is assumed to be done by potentiometers which would be equal in number in an AC or DC system.

Elock (12) V/STOL Velocity. At this point inertial velocities  $v_1$ ,  $v_1$  and rate of climb (R/C) are mixed with instructor wind inputs ( $\hat{N}_{u}$  and  $\hat{E}_{u}$ ) to yield the earthbound rates ( $\hat{N}_{v}$ ,  $\hat{E}_{r}$ , R/C). This is a simple process and consequently requires two summing amplifiers.

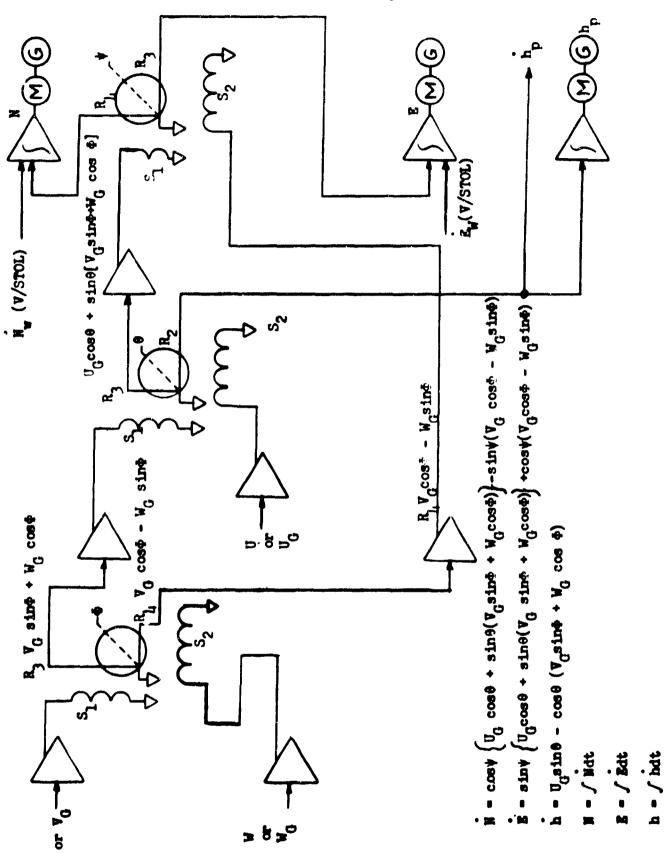


Figure L. Block (10) AC Mechanisation

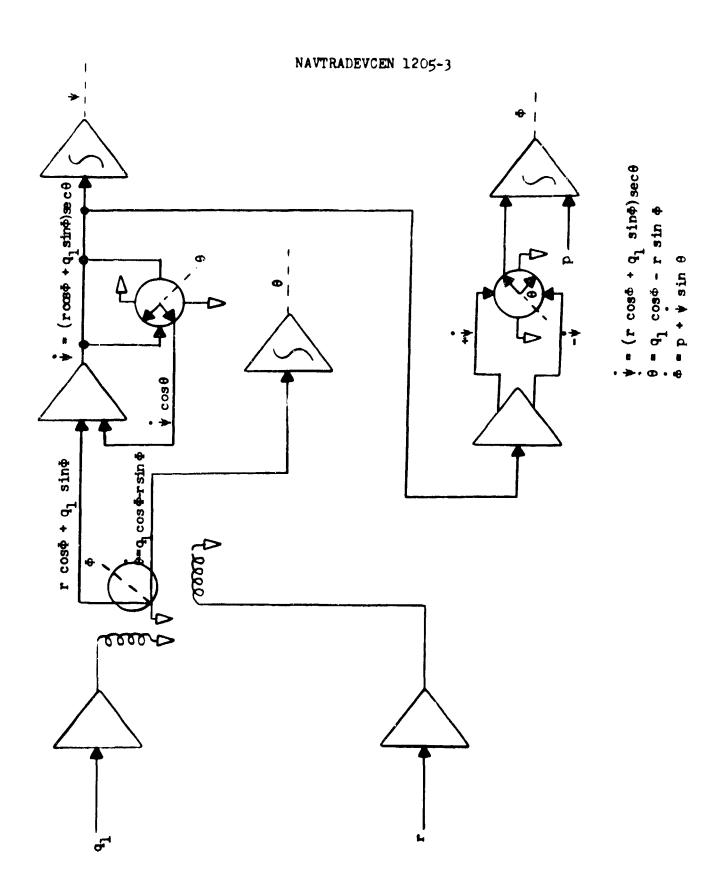


Figure 5. Euler Angle AC Mechanization

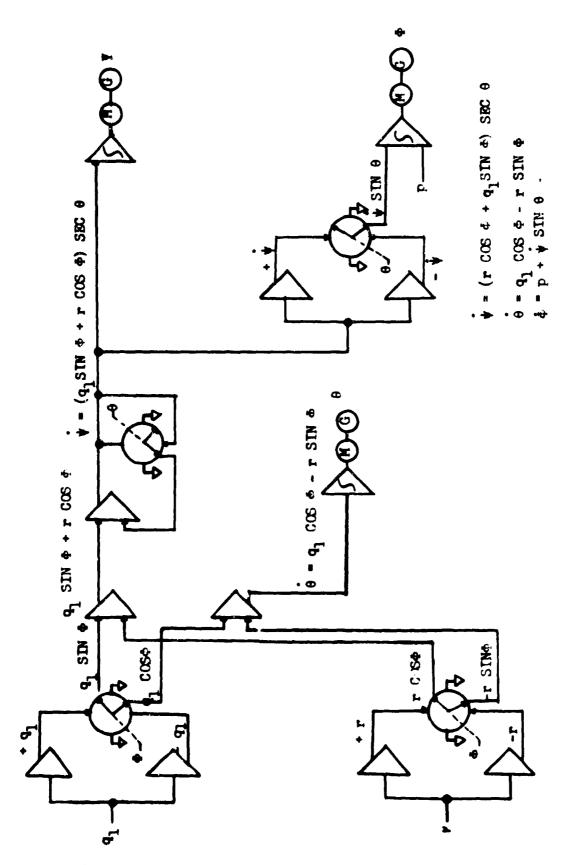


Figure 6. Buler Angles DC Mechanisation

Block (12h) Helicopter Velocity. In the helicopter simulation the velocity outputs  $(U_G, V_G, W_G)$  from Block (8) are summed with the wind velocities  $(U_M, W_M, V_M)$  from the instructor in order to give body axes velocities in the air mass (U, V, W). This operation is a simple summing process and consequently requires three summing amplifiers. This summing is done in Figure 7 by amplifiers (7-2), (7-3), and (7-4). However, if DC computation is used, a serve is indicated for W and both signs are necessary for U and V so that two more amplifiers are needed for generating (+V, -V) and (+V, -V).

Block (13) Wind. These are simply signal inputs from the instructor so that no equipment is specified.

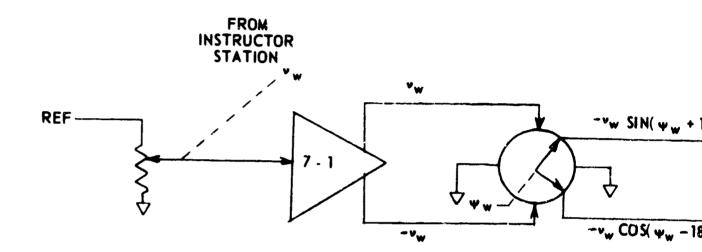
Block (13h) Wind Resolution. In Block (13h) instructor inputs representing wind direction ( $\psi_w$ ) and velocity ( $\gamma_w$ ) are transformed to components  $U_w$ ,  $V_w$  and  $W_w$  for the helicopter simulation. In the AC mechanisation of Figure 7,  $\gamma_w$  is the input to amplifier (7-1). By the use of a sine-cosine (S-C) potentiometer and resolvers, the velocities  $U_w$ ,  $V_w$  and  $W_w$  are obtained. Figure 8 is the DC representation of Figure 7.

	AC		D	C
Component	No.	Wt.	n.	Wt.
Amplifier	6	6	זונ	28
Servo	_1_	7	1	7
S-C Pots	1	1/4	6	1-1/2
Resolvers	3	1-1/2		
Complexity		14-3/4		36-1/2

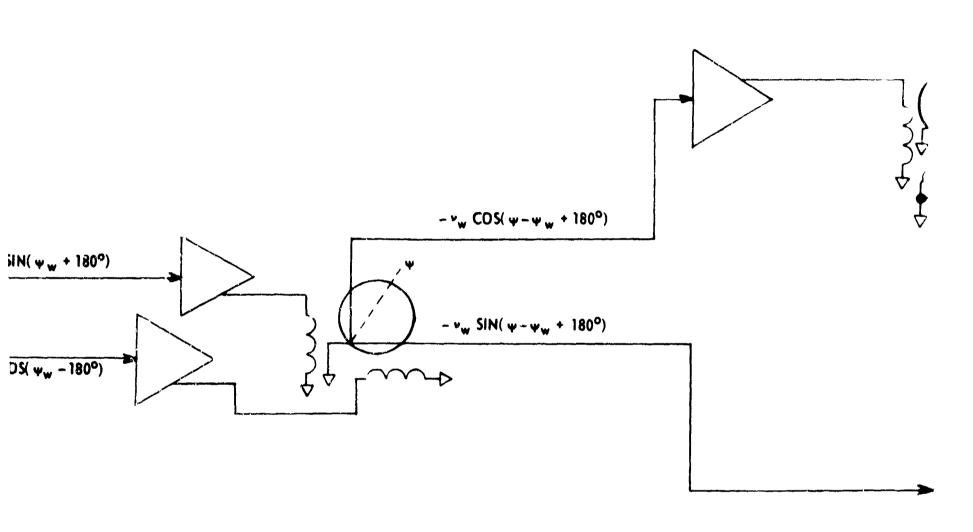
Table 5. Wind Resolution Tabulation

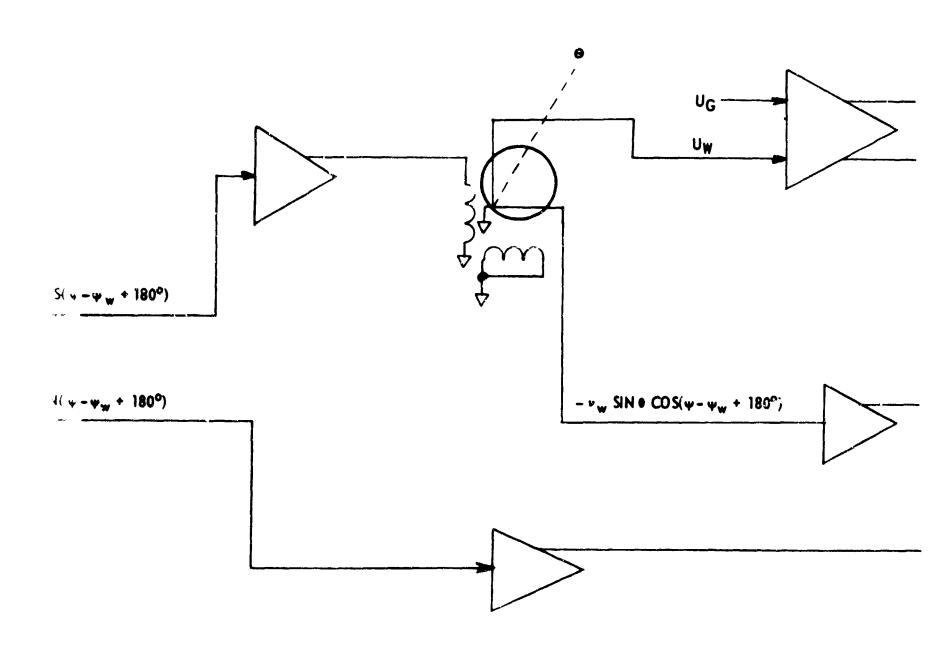
Table 5 is a comparison of the AC and DC mechanisations of equations shown in Figures 7 and 8.

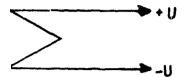
Block (lk) Instructor's Inputs. These inputs are signals controlled by potentiometers at the instructor's console. There is no associated equipment for this operation. This is the last block to be considered in Figure 1. The next task is to consider mechanisation of specific aircraft of which the single rotor helicopter will be the first.

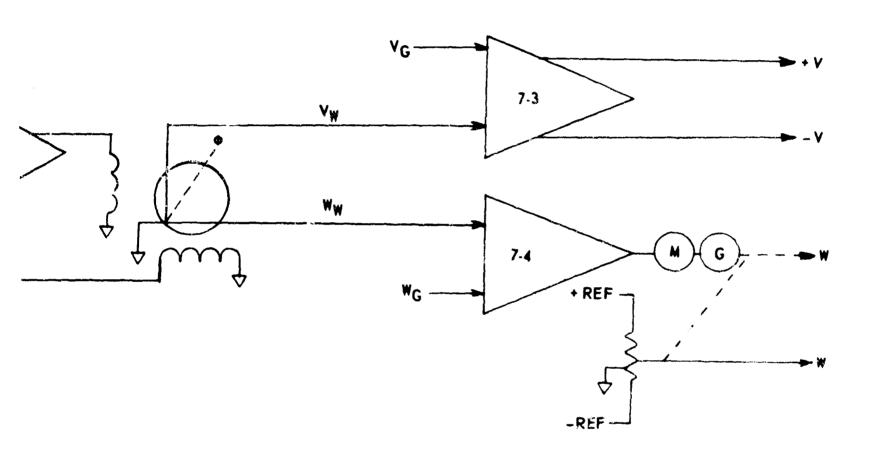












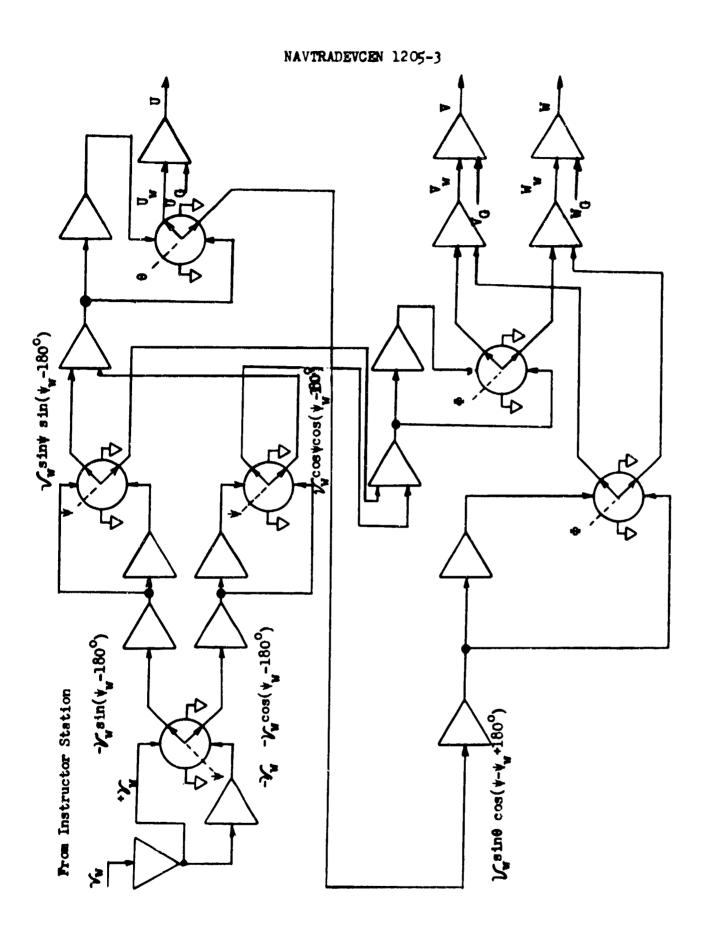


Figure 8. Velocity Summation and Wind Resolution DC Mechanization

Wind blows from  $\psi_W$  heading (true) at  $\gamma_W$  ft./sec.

$$U_W = (-)/(\cos \theta \cos(\tilde{x} - \tilde{x}_W + 180^\circ))$$

$$V_W = (-)V_W \left\{ \sin \theta \sin \phi \cos(Y - Y_W + 180^\circ) - \cos \phi \sin(Y - Y_W + 180^\circ) \right\}$$

$$W_W = (-)_{yW} \left\{ \sin \theta \cos \phi \cos(Y - Y_W + 180^\circ) + \sin \phi \sin(Y - Y_W + 180^\circ) \right\}$$

$$u = u_{c} + u_{w}$$

$$W = W_G + W_W$$

Figure 8. (Cont'd.) Velocity Summation and Wind Resolution DC Mechanisation

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#### B. HELICOPTER MECHANIZATION

Mechanisations for two helicopters are considered—the single rotor helicopter represented by the HSS-2 and the tandem rotor helicopter represented by the CH-46A. The major portion of the mechanisation discussed is for the single rotor equations of motion. In Volume I of this report (NAVTRADEVCEN 1205-1) it was shown that the tandem rotor could be simulated by considering one rotor as a function of the other rotor—that is to say that a single rotor simulation is sufficient for the tandem rotor simulation.

1. SINGLE ROTOR HELICOPTER. Figure 9 is a block diagram for the HSS-2, Davice 2F6h, single rotor helicopter which is similar to Figure 1. Again each block in the flow diagram will be considered separately. On each mechanisation drawings are the applicable equations from Section VI. Mechanization drawings are for AC carrier except in a few cases where it was necessary to include DC mechanizations for the sake of clarity. These drawings may be used for 60 or 400 cycle AC as well as DC with slight modification. Each block in Figure 9 will now be considered and the mechanizations discussed with regard to optimisation. Definitions of helicopter symbols are outlined in Section VI.A.1.

Block (1) Pilot Control. Block (1) of Figure 9 produces the outputs  $(A_{os}, A_{ls}, B_{ls})$  as a result of control movement. Definitions of these terms are contained in Section VI.

Block (2) Engine Simulation. Block (2) of Figure 9 has as outputs the torques ( $C_{EL}$ ,  $C_{ER}$ ) of the two engines in the HSS-2. These are considered as available signals since no engine simulation is considered here.

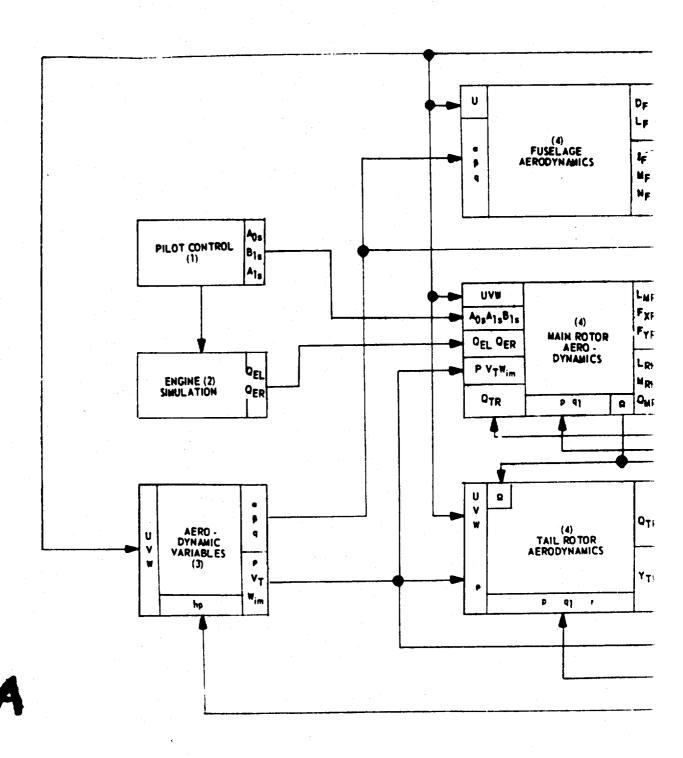
Elock (3) Aero Variables. The AC mechanisation of Elock (3) of Figure 9 is shown in Figure 10. Equations 61, 6.2, 66 and 6.82 are mechanised to produce the outputs  $\alpha$ ,  $\beta$ , q,  $\rho$ ,  $V_T$  and  $W_I$ . The mean

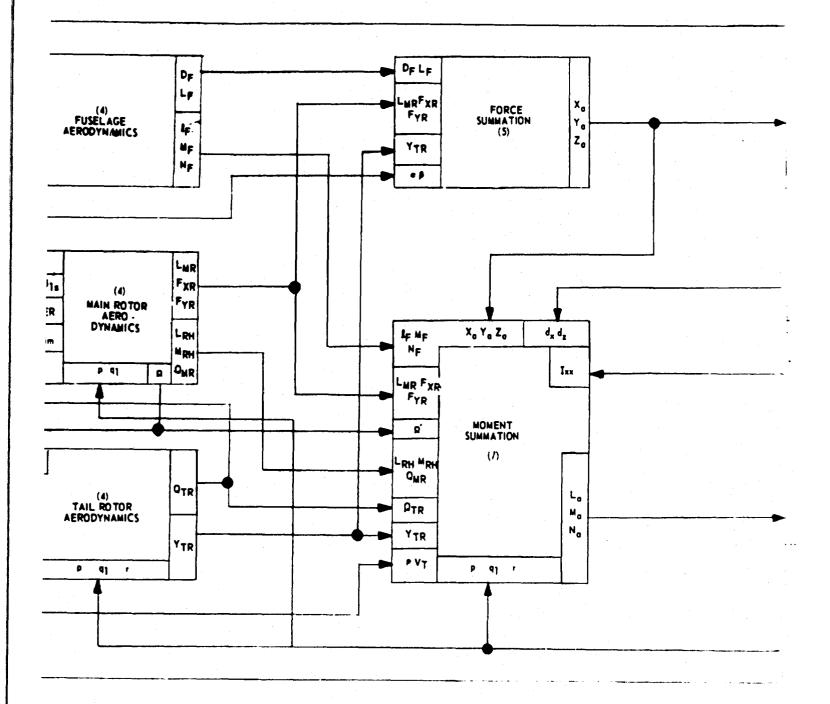
mechanisation of W<sub>i</sub> is included in Figure 10 since it is directly mean

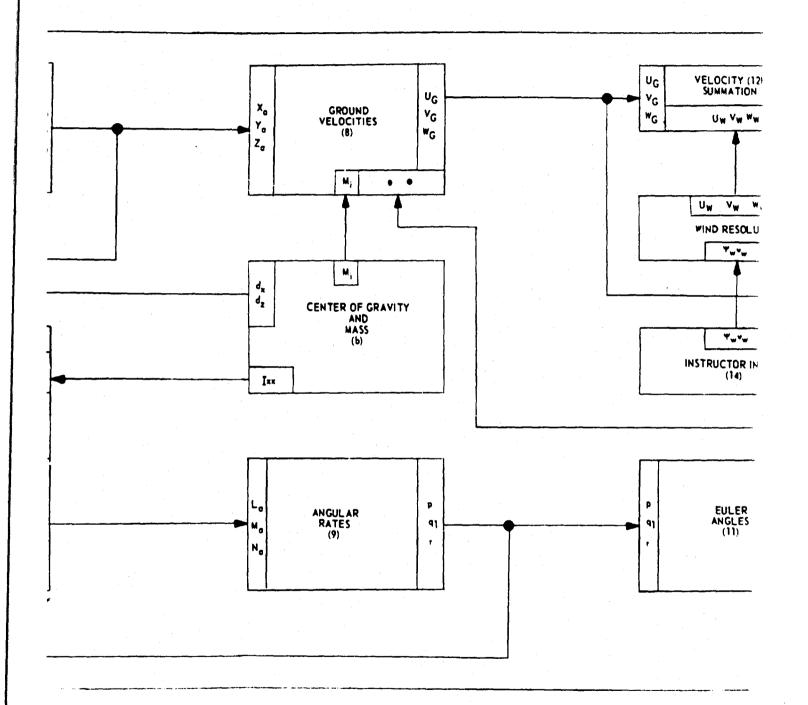
related to the generation of the aerodynamic variables. A literal step-by-step discussion of Figure 10 will now be given. This will not be done for many of the remaining drawings since the methods of mechanisations in Figure 10 are repeated throughout the report, and such a continuous literal discussion when the equations are on each drawing and each line in the drawing is labeled would be laborious, redundant and difficult to read.

In Figure 10 W<sub>i</sub> is formed by dividing main rotor lift over air mean density  $(-I_{MR}/\rho)$  by the total velocity of the helicopter  $(V_T)$ . This signal  $(-KI_{MR}/V_T)$  is fed into a servo amplifier whereby W<sub>i</sub> is mean generated by a servo shaft. W<sub>i</sub> is used as position feedback and the rate feedback is W<sub>i</sub>.

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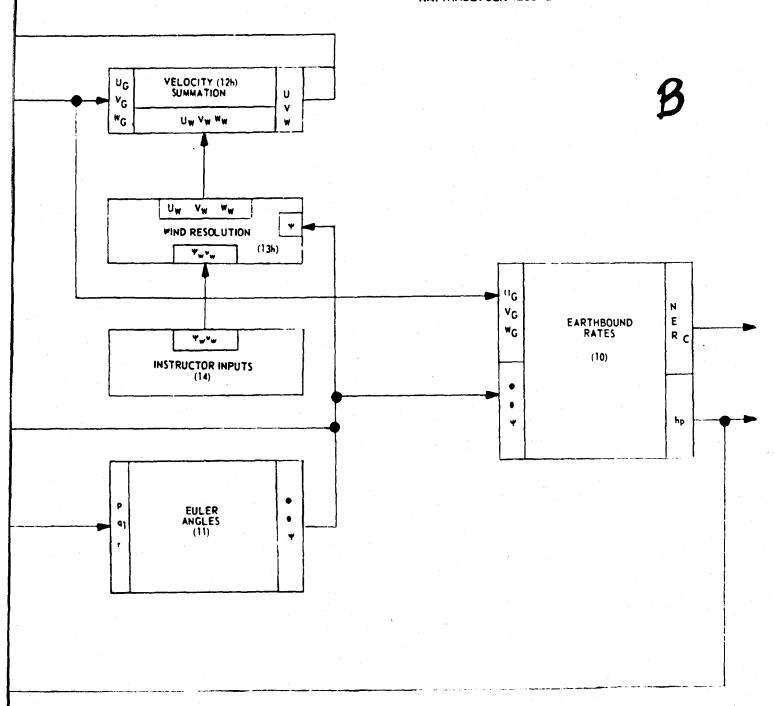
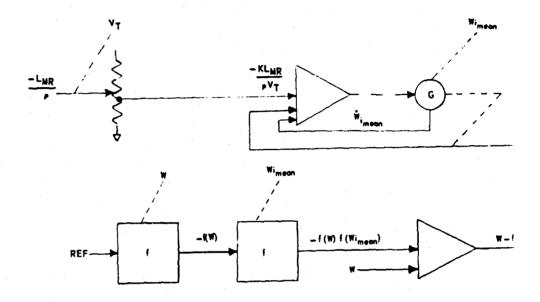
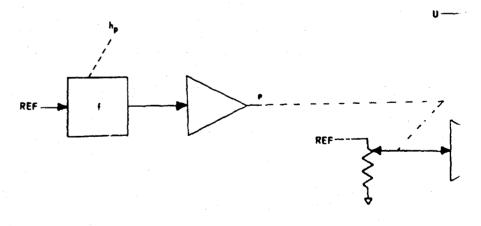


Figure 9. Simplified Block Diagram Single Rotor Helicopter







A

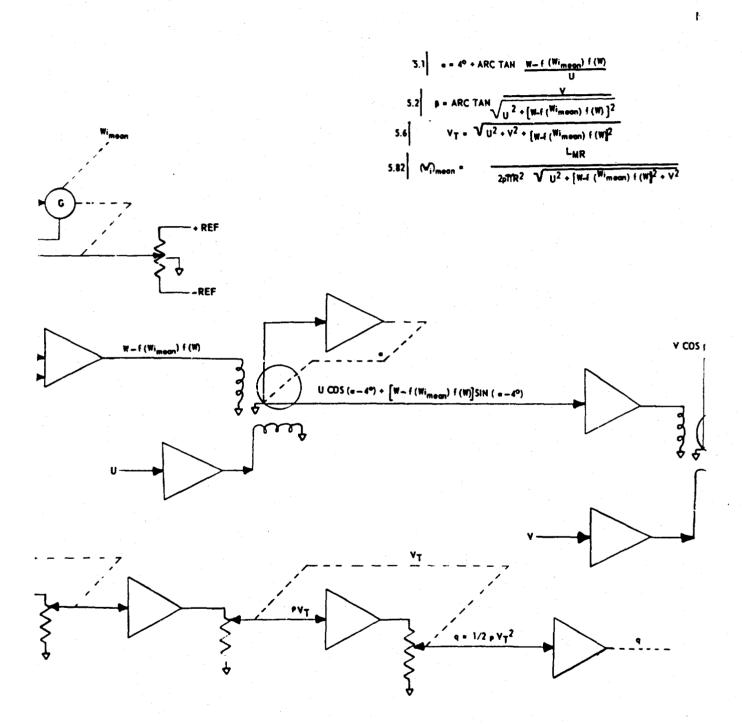


Figure IQ Aero

3.1 = 4° + ARC TAN 
$$\frac{W=f(Wi_{magn}) f(W)}{U}$$

5.2 = ARC TAN  $\frac{V}{U^2 + [W-f(Wi_{magn}) f(W)]^2}$ 

5.6 =  $V_T = \sqrt{U^2 + V^2 + [W-f(Wi_{magn}) f(W)]^2}$ 

5.82 |  $V_{il}_{magn} = \frac{U_{il}}{2p\pi R^2} \sqrt{U^2 + [W-f(Wi_{magn}) f(W)]^2 + V^2}$ 

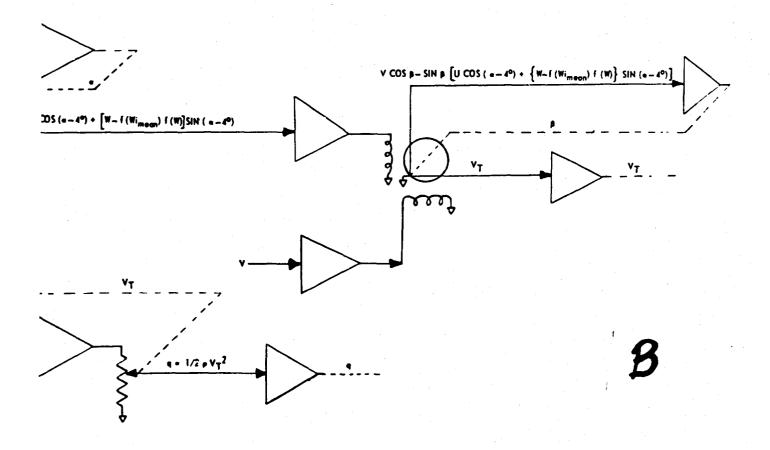


Figure IQ Aerodynamic Variables AC Mechanization

V<sub>T</sub> is formed next in Figure 10. A function of vertical velocity,

-f(W), is developed first. This is then multiplied by a function of
W<sub>1</sub> to give -f(W)f(W<sub>1</sub> ). The functions are generated by shaped
mean

potentiometers, f<sub>1</sub> and f<sub>2</sub>. Next, -f(W)f(W<sub>1</sub> ) is added to vertical
mean

velocity, W, in a summing amplifier to form the output [W - f(W)f(W<sub>1</sub> )
mean

which is then fed into the stator winding of a resolver on the α servo
shaft. The other stator winding of the resolver is driven by the helicopter forward velocity, U, through a resolver drive amplifier. The output of one rotor forms the function [W - f(W)f(W<sub>1</sub> )] cos α - U sin α

mean

which is fed to motor amplifier of the α servo shaft. Now, since output
of the resolver is the driving source of the servo shaft, the servo
shaft will continue to drive the resolver until the resolver output is
sero. When this occurs, then

$$[W - f(W)f(W_{\underline{1}})] \cos \alpha - U \sin \alpha = 0$$

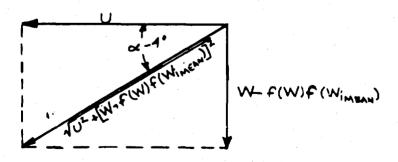
and 
$$\frac{\sin \alpha}{\cos \alpha} = \tan \alpha = \frac{[W - f(W)f(W_1)]}{W - f(W)f(W_2)}$$
.

If the resolver is seroed such that  $(\alpha - \mu^0) = 0$  when  $\alpha = \mu^0$  then equation 5.1 will have been mechanised,  $[W - f(W)f(W_1)] \cos (\alpha - \mu^0) = 0$ 

U sin  $(\alpha - \mu^0)$  will be identically equal to zero and the zervo shaft will form the function  $\alpha$ . Since the shaft of the resolver is now positioned automatically to  $\alpha$  and the resolver is zeroed so that its shaft positions to  $(\alpha - \mu^0)$  the remaining rotor winding forms the function U cos  $(\alpha - \mu^0)$  +  $[W - f(W)f(W_{\underline{max}})]$  sin  $(\alpha - \mu^0)$ , which is easily seen

to identically equal  $\sqrt{U^2 + [W - f(W)f(W_i)]^2}$  if one considers U mean

and the W function as legs of a right triangle and the hypotenuse as the sum of the projections of the legs as shown in the sketch below.



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In a manner similar to the above the helicopter sideward velocity, V, and  $U^2 + [W - f(W)f(W_1)]^2$  are used to drive a resolver on the  $\beta$  mean serve shaft. The relation  $V\cos\beta - \sin\beta [U\cos(\alpha - l_1^0) + \{W - f(W)f(W_1)\} \sin(\alpha - l_1^0)]$  is used to drive the serve shaft so that the mean shaft positions to the angle equal to  $\beta$  and equation  $\delta.2$  is mechanised. The remaining roter output is conveniently found to be the helicopter total velocity,  $V_T$ , since it forms the square root of the sum of the squares of the resolver inputs in the same manner as the  $\alpha$  resolver. The output,  $V_T$ , is fed to a motor amplifier to drive the  $V_T$  serve shaft.

The last mechanization in Figure 10 is that of dynamic pressure (q). Initially, functions of pressure altitude (h<sub>p</sub>) are fed into an amplifier as air density ( $\rho$ ) to form a  $\rho$  servo. A  $\rho$  servo shaft potentiometer wiper output is fed into a buffer amplifier whose output drives a potentiometer located on a V<sub>T</sub> servo shaft. The wiper output of this potentiometer is  $\rho$ V<sub>T</sub> which is fed into a buffer amplifier whose output is 1/2  $\rho$ V<sub>T</sub> and drives a potentiometer located on a V<sub>T</sub> servo shaft. The wiper output of this potentiometer is 1/2  $\rho$ V<sub>T</sub> which is equal to q. In turn, q is fed into an amplifier which drives the q position servo.

DC mechanisation of Figure 10 involves sine-cosine potentiometers and additional amplifiers for buffer and sign inversion purposes to replace resolvers. If resolvers are used with DC, modulators and demodulators would be necessary. This component complexity is due to the interfacing of AC and DC equipment. Table 6 is a comparison of AC and DC components.

	4	rc	DX.	
Component	No.	Wt.	No.	Wt.
Amplifier	12	12	18	36
Servo	6	42	6	Ц2
Pots	5	1 1/4	5	1 1/4
S-C Pots			<u> </u>	1
Resolvers	2	1		
Complexity		56 1/4		80 1/4

Table 6. Aerodynamic Variables Single Rotor Helicopter

For each resolver in the AC mechanization two sine-cosine potentiometers and three additional amplifiers are necessary for a DC mechanization.

Block (4) Aero Terms. The AC mechanization of Block (4), Figure 9 is divided into three parts-Tail Rotor Aerodynamics, Fuselage Aerodynamics and Main Rotor Aerodynamics.

a. Tail Rotor Aerodynamics. In Figure 11 is shown the AC mechanization of the tail rotor equations (6.7 through 6.17 and 6.26). The component tabulation is in Table 7. A literal discussion would be similar to that of Block (3) Aero Variables, Figure 10.

	A	C	r	C
Component	No.	Wt.	No.	Wt.
Amplifier	19	19	25	50
Servo	7	49	7	49
Pcts	8	2	8	2
S-C Pots			1	1
Resolvers	2	1	( · · · · · · · · · · · · · · · · · · ·	
Function (f) Generation	10	_	10	V
Complexity		71		102

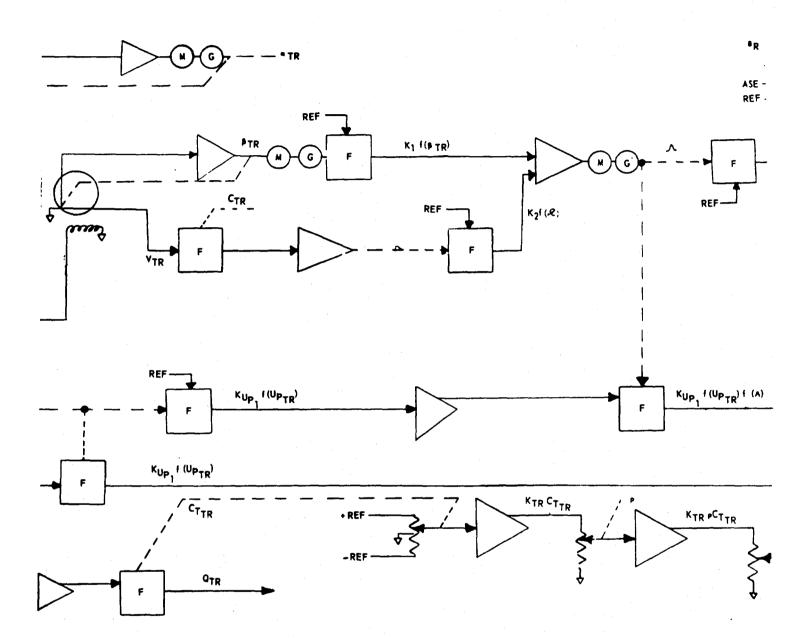
Table 7. Tail Rotor Aerodynamics

The function generators (f) are composed of potentiometers either in AC or DC mechanization. It is conceivable that more buffer and sign inversion amplifiers may be necessary to achieve function generation for the DC mechanization.

b. Fuselage Aerodynamics. The mechanization of fuselage aerodynamics is simply a summing operation of function generator outputs. Figure 12 is the recommended AC mechanization. The DC mechanization would be dependent on the relationship of the components with the remainder of the mechanization, however TC mechanization should be the same as that shown in Figure 12. Table 8 is a list of components showing the similarity between a DC mechanization and the AC mechanization of Figure 12.

U SIN  $= TR - (W + K_q + 1) \cos = TR = 0$ 3334 U COS + TR + ( (MG 41) SIN + TR  $f(V,r,p) = V - K_{\gamma}r + K_{pp}$ KUP1 FC KUP, (UPTR) QTR





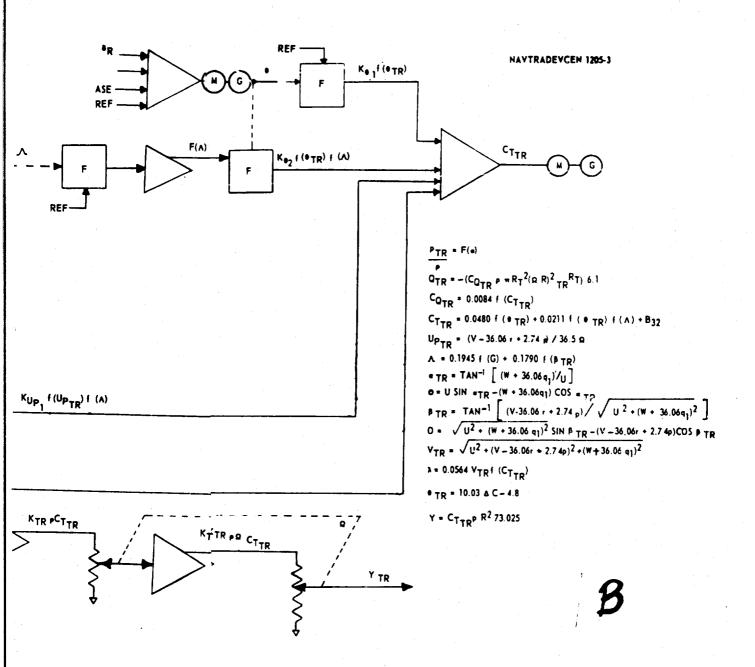


Figure 11. Tail Rotor Aerodynamics AC Mechanization

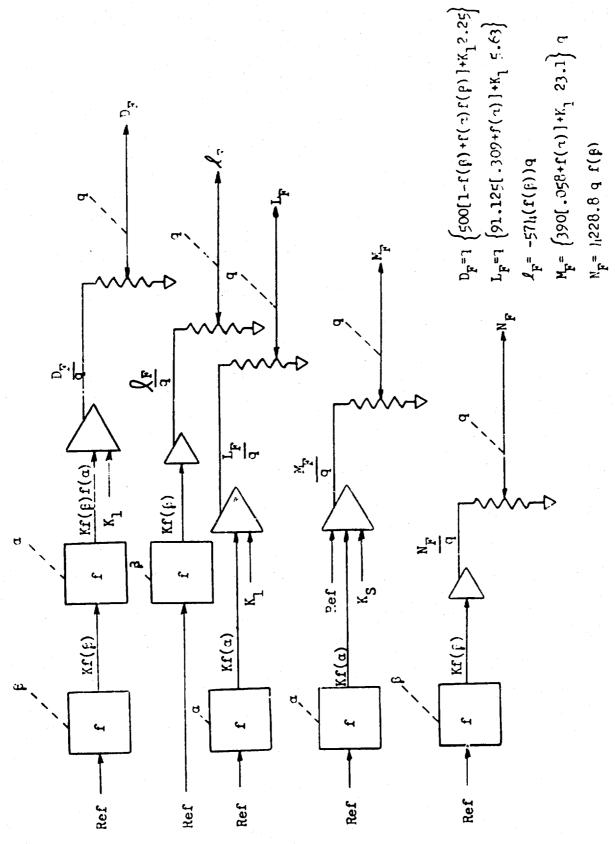


Figure 12. Fuselage Aerodynamics AC Mechanization

	A	vc	X	
Component	No.	Wt.	No.	Wt.
Amplifier	5	5	5	5
Pots	5	1 1/4	5	1 1/4
Complexity		6 1/4		6 1/4

Table 8. Fuselage Aerodynamics

c. Main Rotor Aerodynamics. The main rotor aerodynamics mechanization of the blade element equations involves more computing equipment than that required to generate all other functions in the mechanization of the equations of motion. For this reason the main rotor aerodynamic mechanization is divided into several smaller mechanizations to facilitate discussion and insertion in the report.

Figure 13 is a simplified block diagram showing the interconnection and function flow between these subsections.

(1) Block (1) Local Vertical Velocity. Consider first the mechanization of the local vertical velocity, Up , in Hlock (1) of Figure 14. Eighteen Up functions of both polarities must be developed from external imputs U, V, W, W, ,11, p and q and internally generated feedback inputs  $a_{1s}$ ,  $b_{1s}$  and  $\beta \psi$ . This involves the basic operations of potentiometer multiplying and amplifier summing. Since these are such simple operations the optimization decision is entirely decided on the economics and complexity aspects. The DC mechanisation differs from the AC only in the number of amplifiers required for the positive and negative functions. The DC mechanization required 36 amplifiers instead of 18. From the standpoint of economy the AC mechanization with less amplifiers seems optimum. The complexity of the equipment is certainly in proportion to the number of components. Consult Table 9 for tabulation of components.

		C	DC.	
Component	No.	Wt.	No.	Wt.
Amplifier	18	18	36	36
Pots	17	3 3/4	17	3 3/4
Complexity		21 3/4		39 3/4

Table 9. Local Vertical Velocity

βψ als bls Ω 91 LOCAL VERTICAL VELOCITY (1) U Up W.Y ٧ mean UP<sub>W-y</sub>  $\delta_{ heta}$  c BLANG ANG AT  $\delta_{ heta}$ L  $\delta_{\theta\,\mathsf{F}}$ TANGENTIAL UTW-Y (2) Ω

A

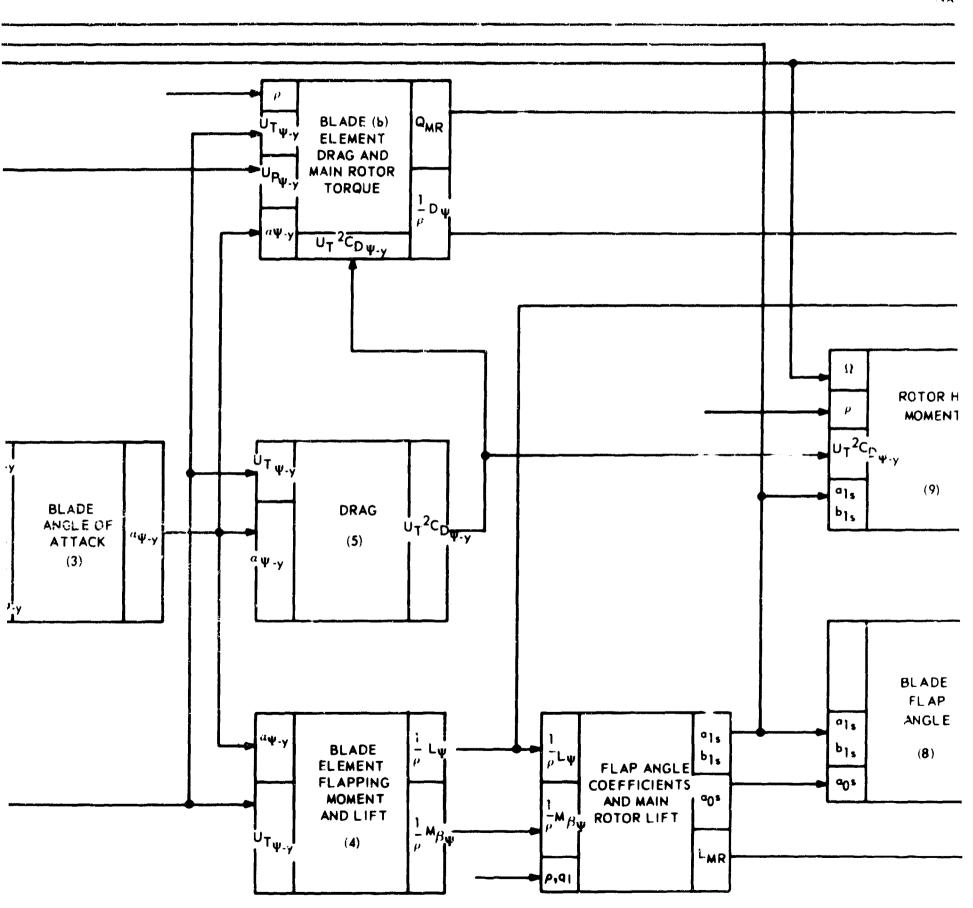


Figure 13 SIMPLIF

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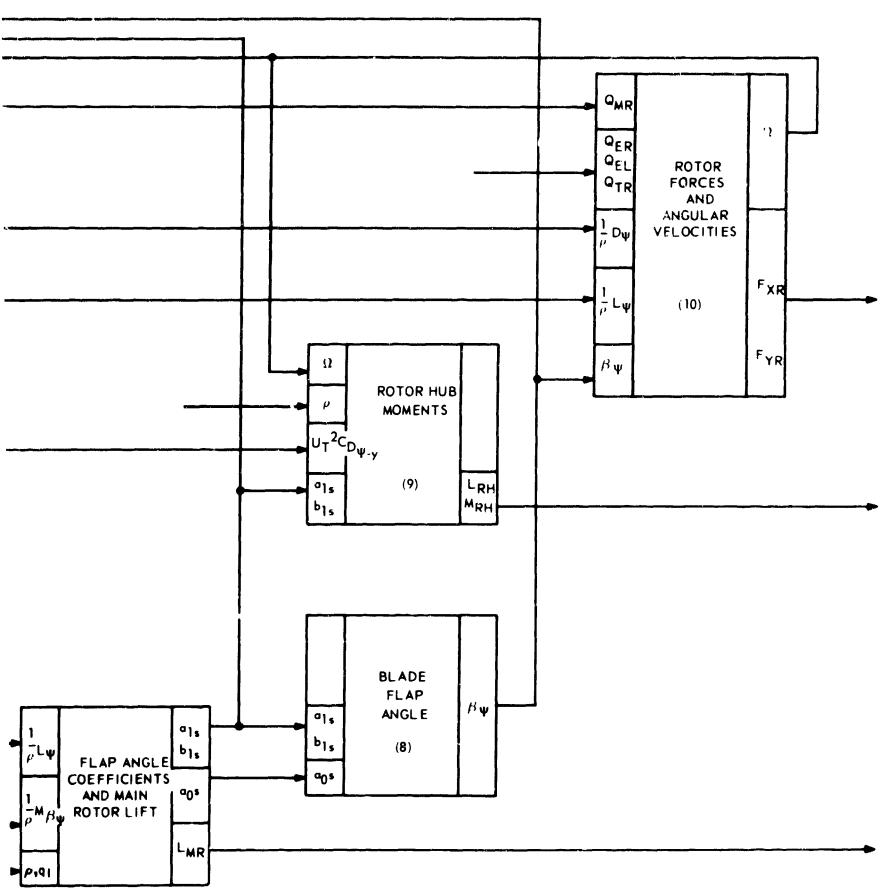
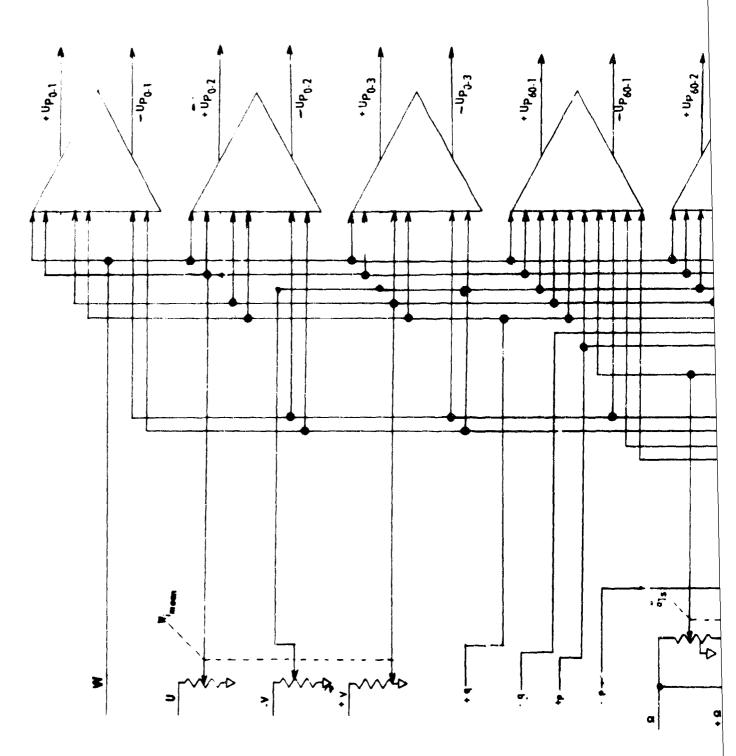
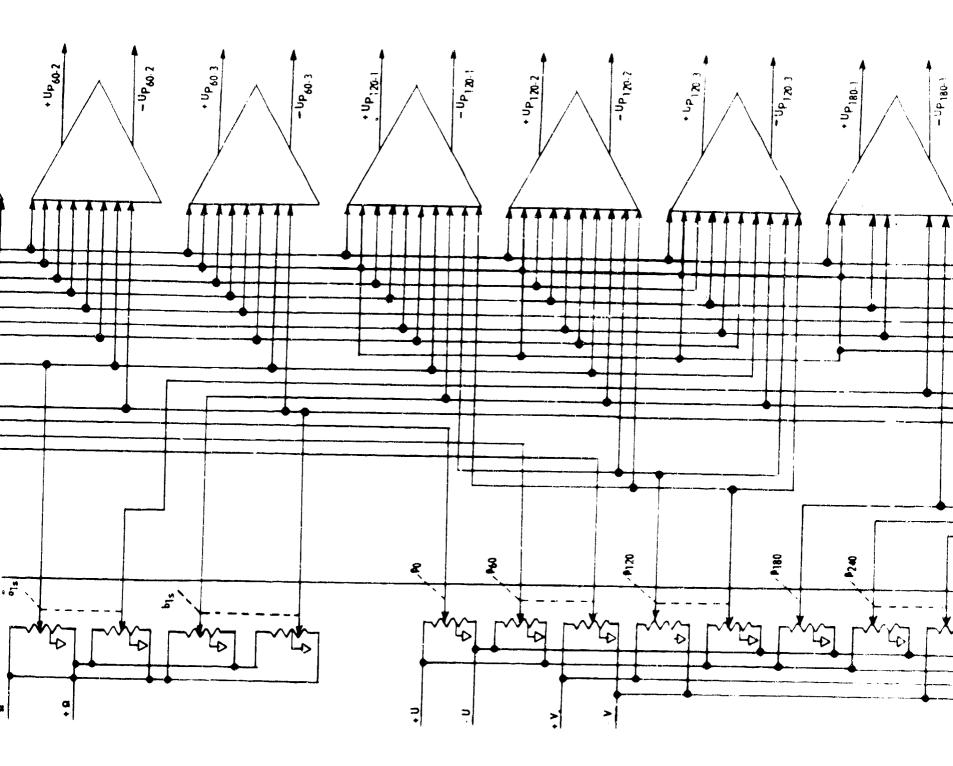


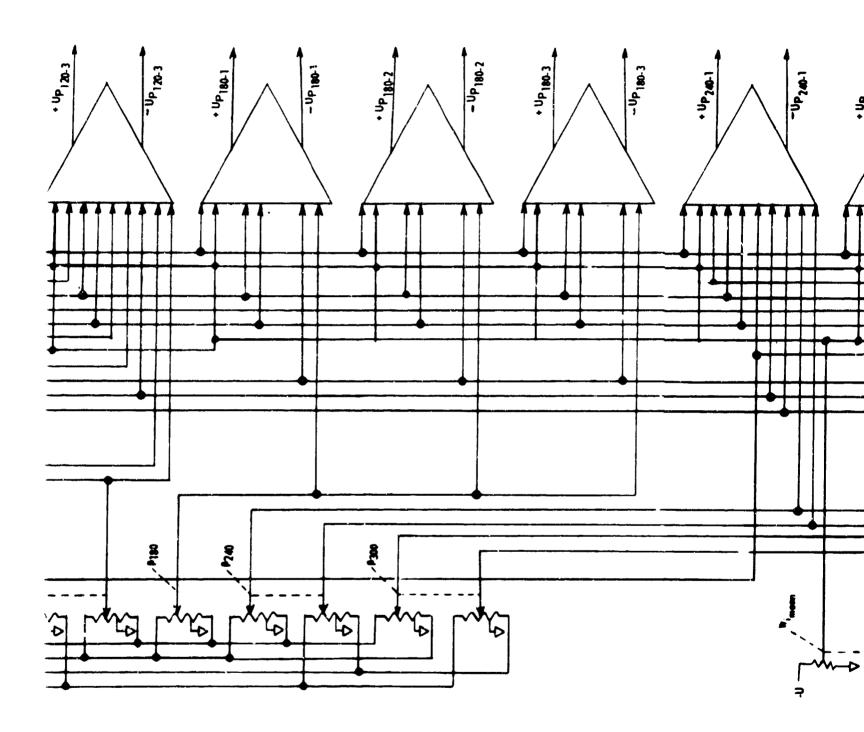
Figure 13 SIMPLIFIED BLOCK DIAGRAM ROTOR AERODYNAMICS

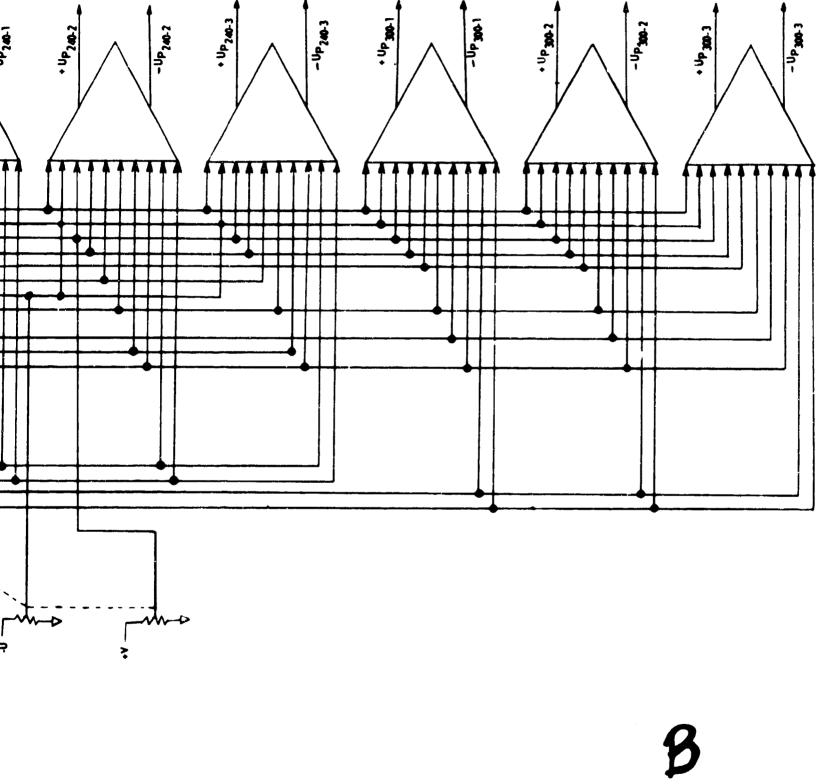












(2) Block (2) Tangential Velocity.— The tangential rotor velocity, shown in Figure 15 is a sum of functions of U, V and  $\Omega$  to obtain the 18 blade element tangential velocities, U,

Since succeeding functions are formed by taking functions of  $\mathbb{U}_T$  , the outputs of this mechanization must be shaft positively

tions. Optimisation of this mechanization involves the selection of function generation methods to form the functions of  $U_T$ . The present analog state-of-the-art does not furnish  $\Psi$ -y

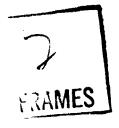
any more simple and straightforward method than padded potentiometers. Hence, since servo shafts are required for the potentiometers, the mechanization is equally optimum by either AC or DC methods. Table 10 is the summary of component complexity derived from Figure 15.

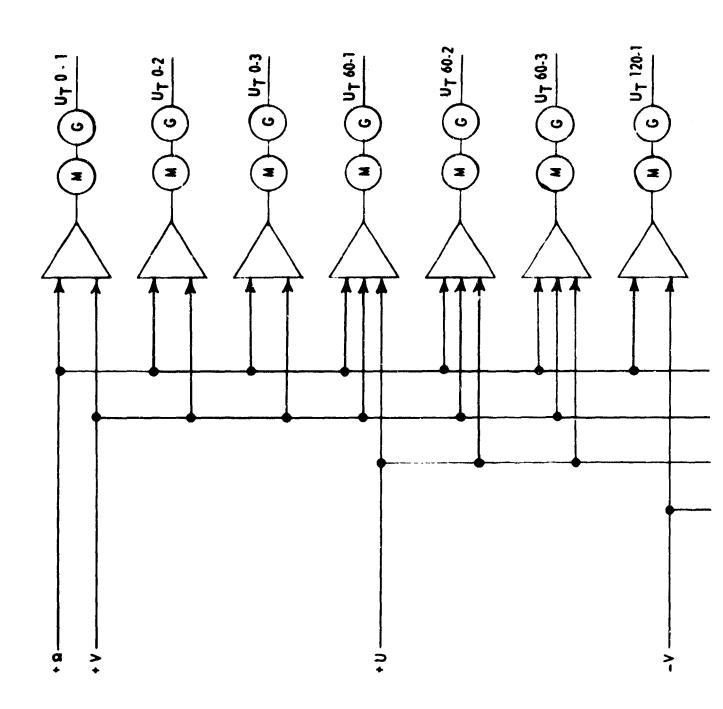
		AC	DC		
Component	No.	Wt.	No.	Wt.	
Amplifier	18	18	18	36	
Servo	18	126	18	126	
Complexity		244		162	

Table 10. Tangential Velocity

(3) <u>Block (3) Blade Angle of Attack.</u> The eighteen blade element angles of attack,  $\alpha_{\psi-y}$ , are also required as shaft positions to form functions of angle of attack for later use. Also each  $\alpha_{\psi-y}$  is a function of  $U_p$ . Then the mechanisative  $U_T$ 

tion in Figure 16 follows logically since  $U_{\chi}$  exists as  $V_{\chi}$  a shaft position and it is a simple procedure to divide two functions using potentiometers. Considering the AC mechanization shown in Figure 16 for optimising purposes it can be seen that the only area that would differ significantly from a DC mechanisation would be the requirement of positive and negative functions of  $\delta_{\theta}$ . Hence the DC mechanisation would require three more amplifiers than the AC mechanisation. Table 11 reflects component complexity of Figure 16.







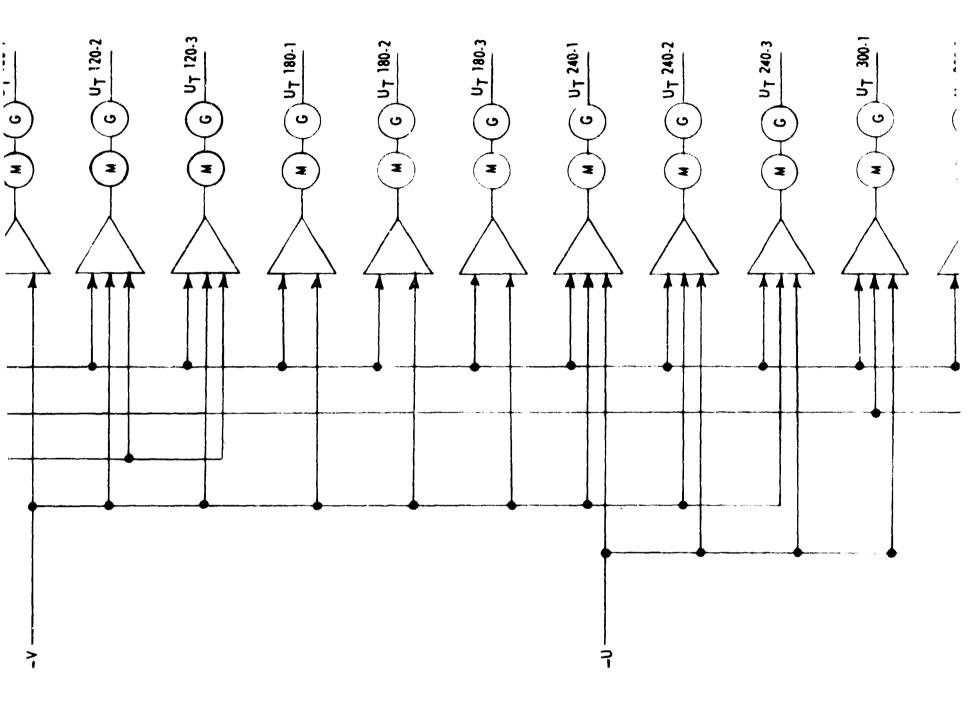
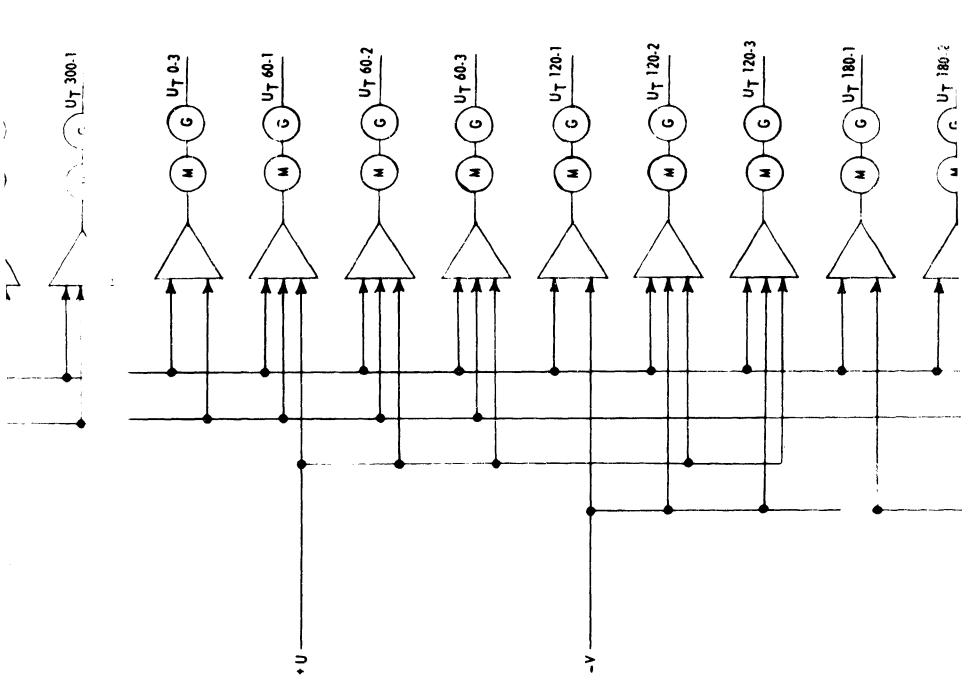
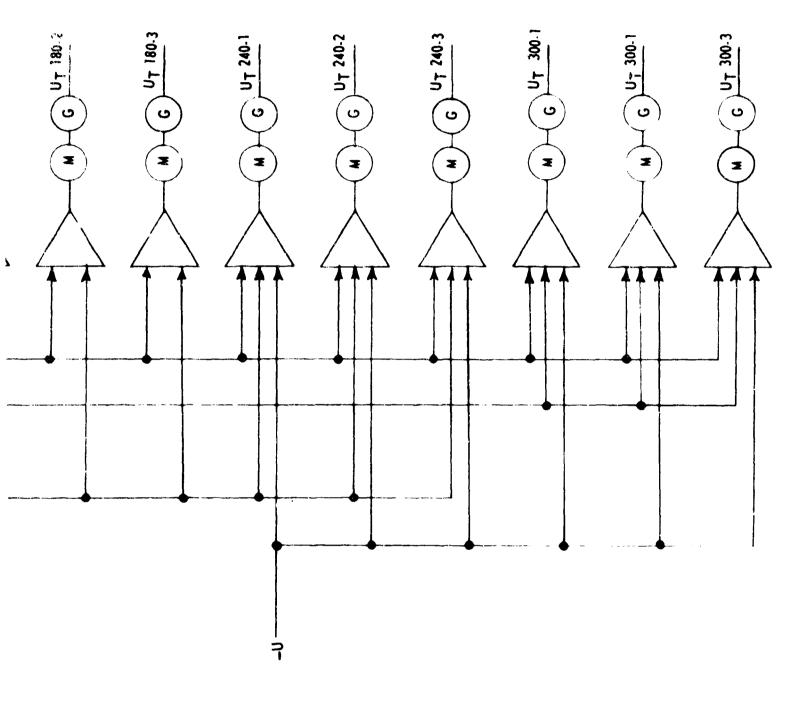


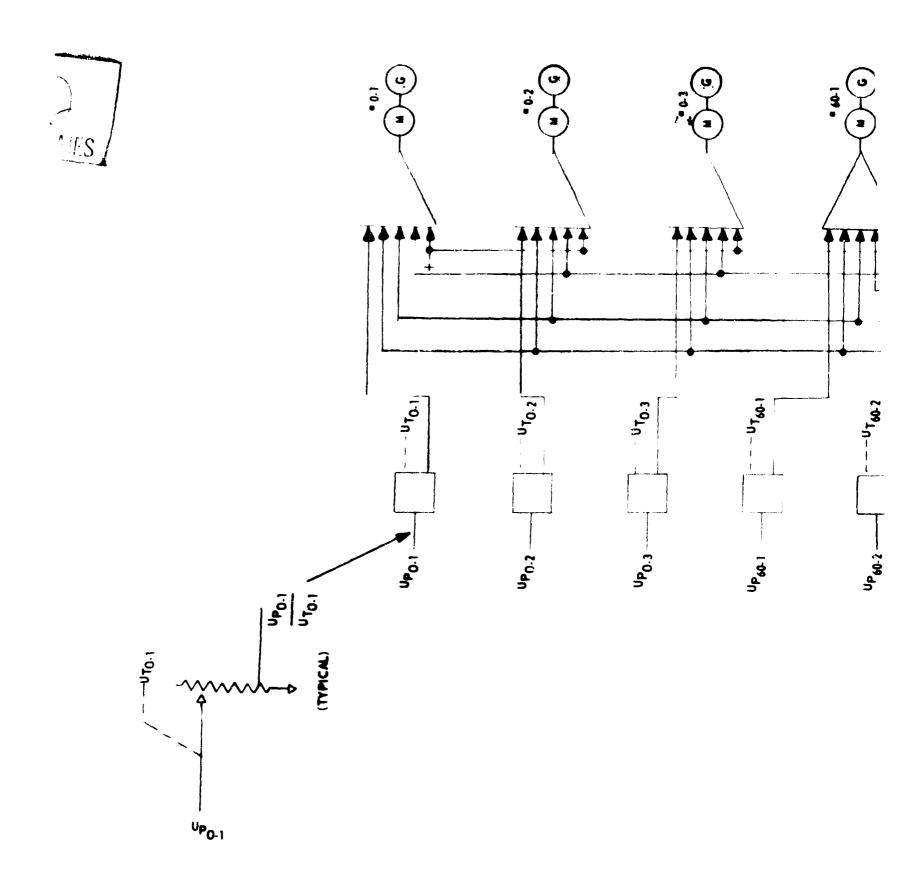
Figure 15. Tangential Velocity AC Mechanization



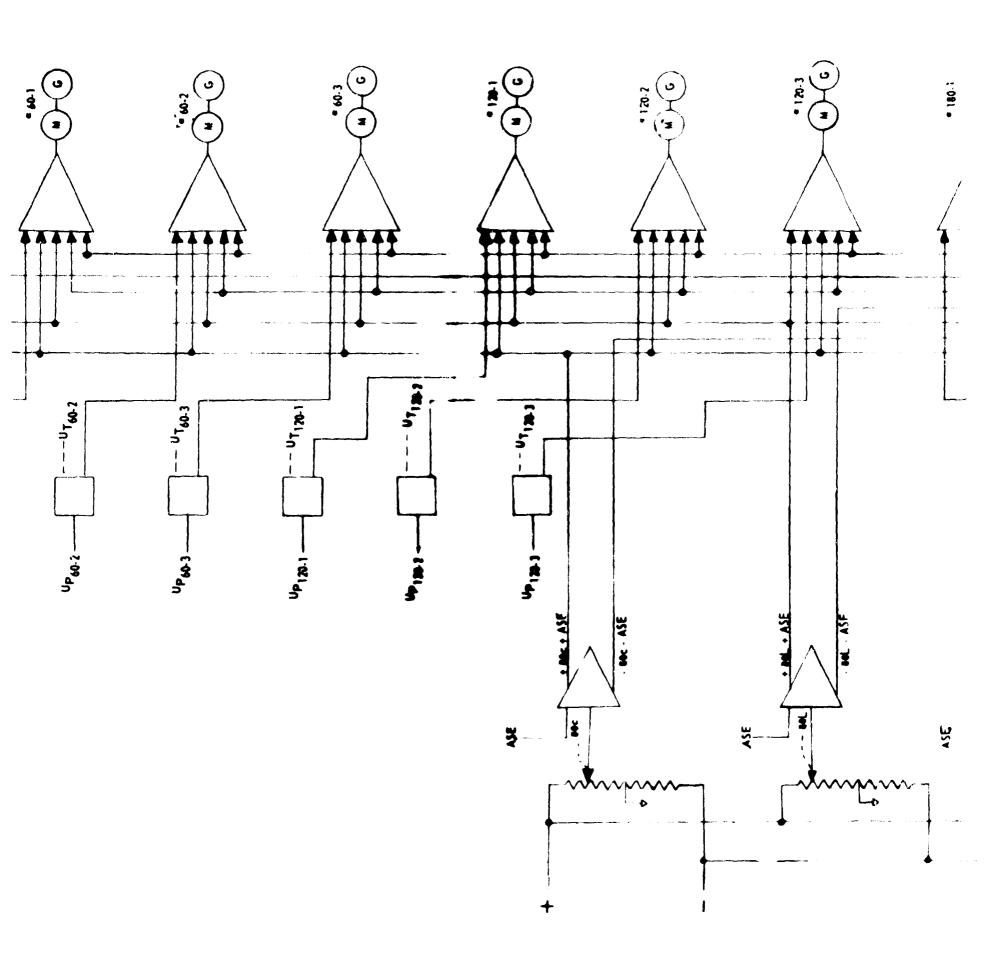


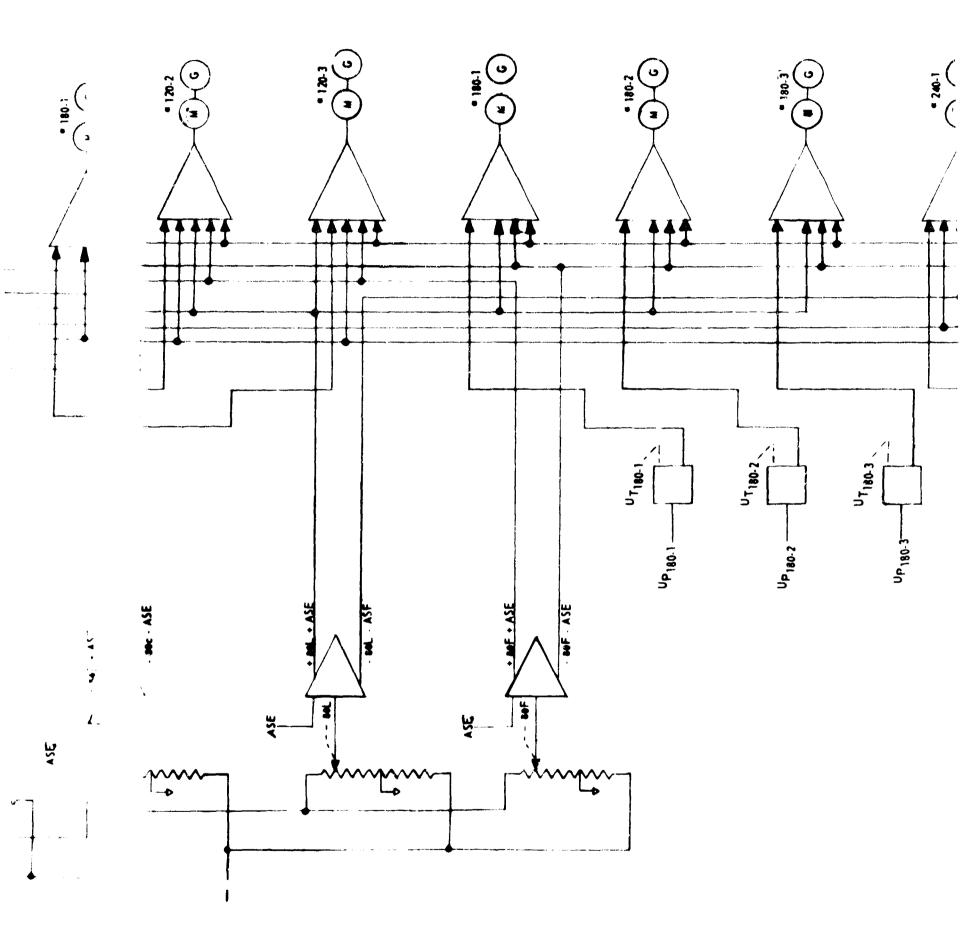
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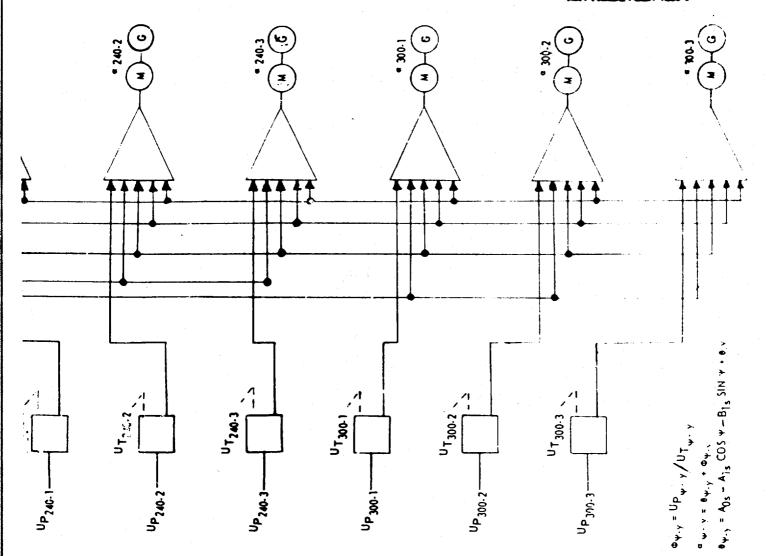
Figure 15. Tangential Velocity AC Mechanization











B

	A	rc	D	
Component	No.	Wt.	No.	Wt.
Amplifier	21	21	24	48
Servo	18	126	18	126
Pots	21	5 1/4	21	5 1/4
Complexity		152 1/4		179 1/4

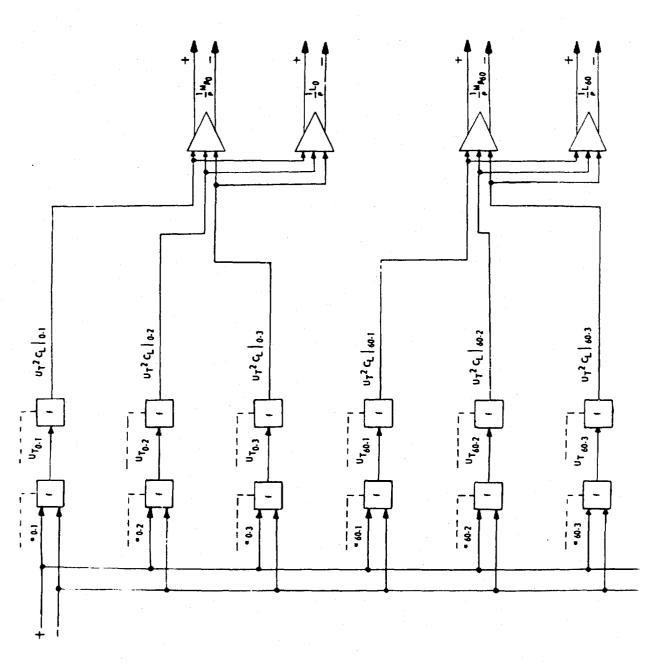
Table 11. Blade Angle of Attack

Block (4) Blade Element Flapping Moment and Lift. The blade element flapping moment (M<sub>B</sub>) and the blade element lift (L<sub>V</sub>) are formed from the sums of functions of a<sub>V-Y</sub> and U<sub>T</sub> as very can be seen in Figure 17. Here again both positive and negative output functions are required which results in the only difference between the AC and DC mechanizations. In this case 12 additional amplifiers are required in the DC mechanization to give both signs of M<sub>B</sub> and L<sub>V</sub>. Table 12 reflects component complexity of Figure 17.

Component	AC		nc	
	No.	Wt.	No.	Wt.
Amplifier	12	12	24	24
Function (f) Generation	36	<u>.</u>	36	
Complexity		12		24

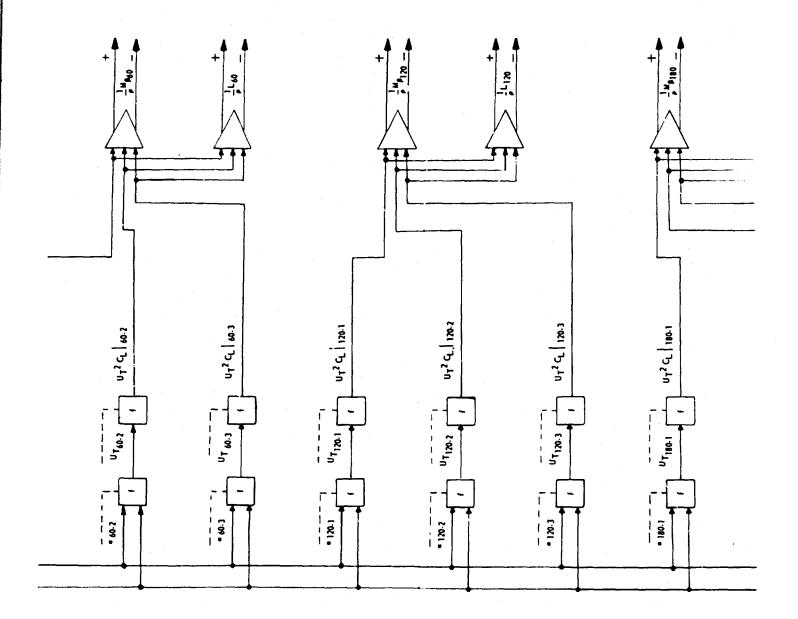
Table 12. Blade Element Flapping Moment and Lift

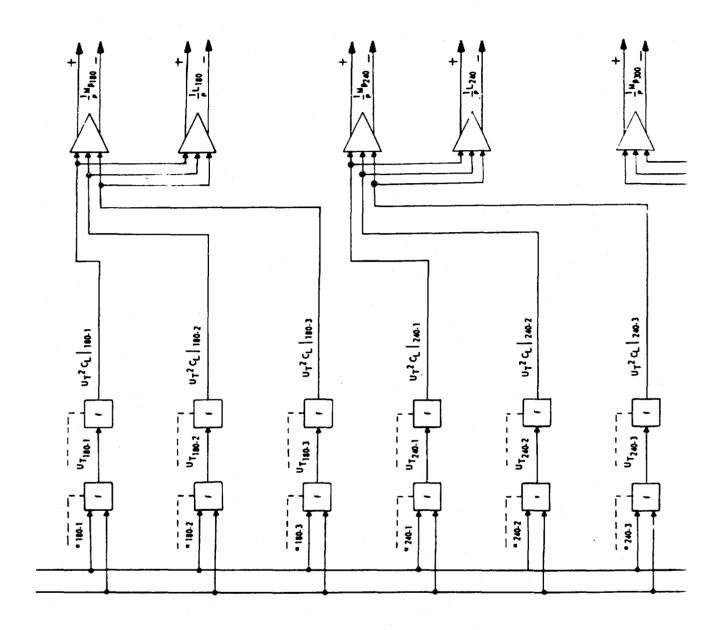
- (5) Blade Element Drag. Figure 18 is the mechanization of the blade element drag computation. This mechanization in itself can be equally optimum in either AC or DC methods. This is evident since the entire mechanization is simply a combination of potentiometer function generators on servo shafts.
- (6) Block (6) Blade Element Drag and Main Rotor Torque. The computation of blade element drag and main rotor torque is the same type of summation of potentiometer function generations as in Figure 19. Here again the only difference



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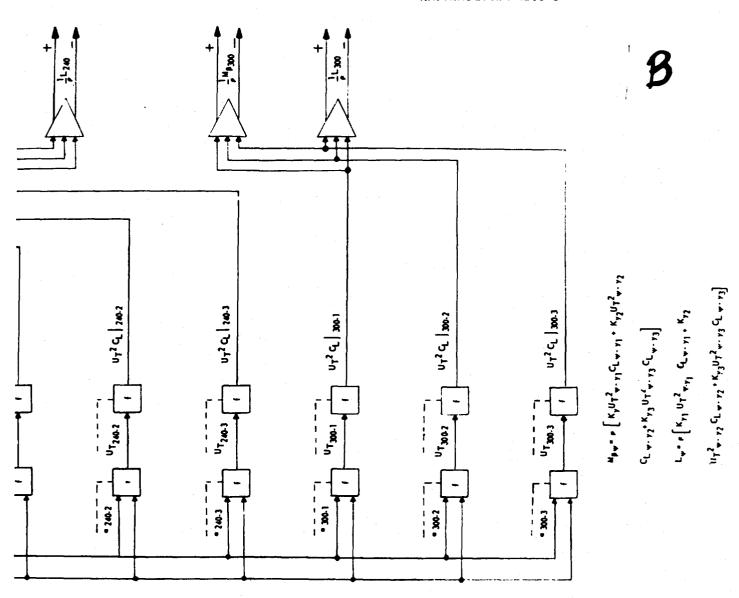
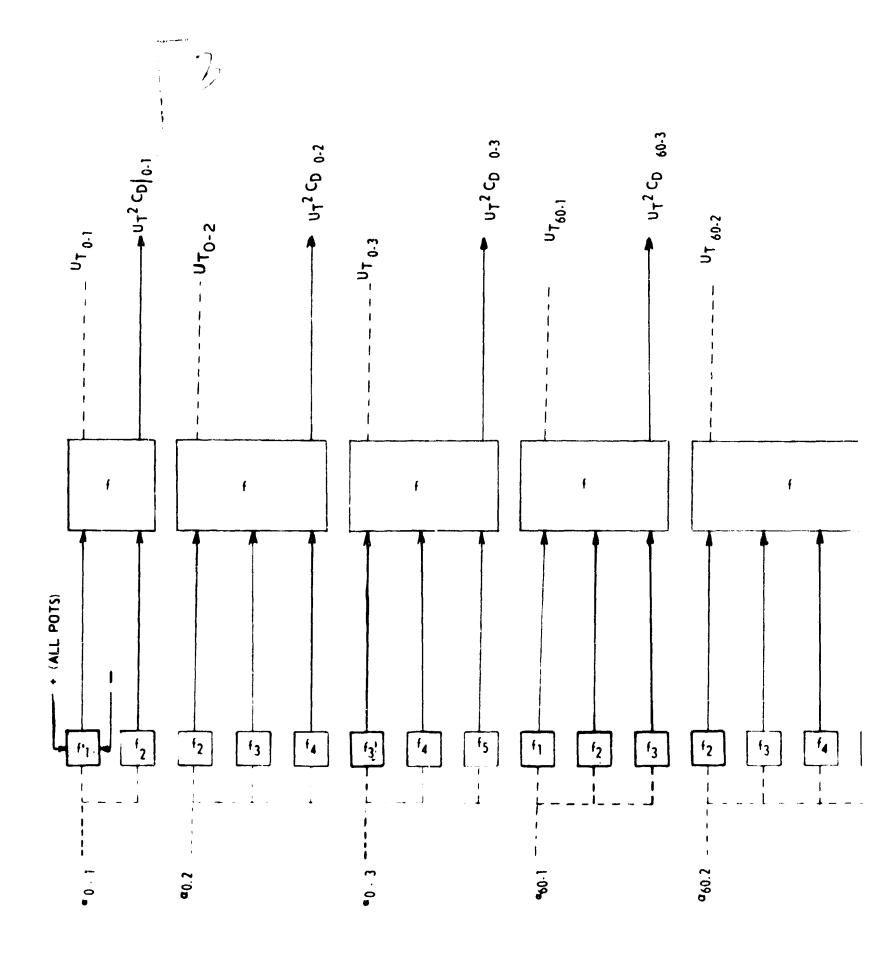
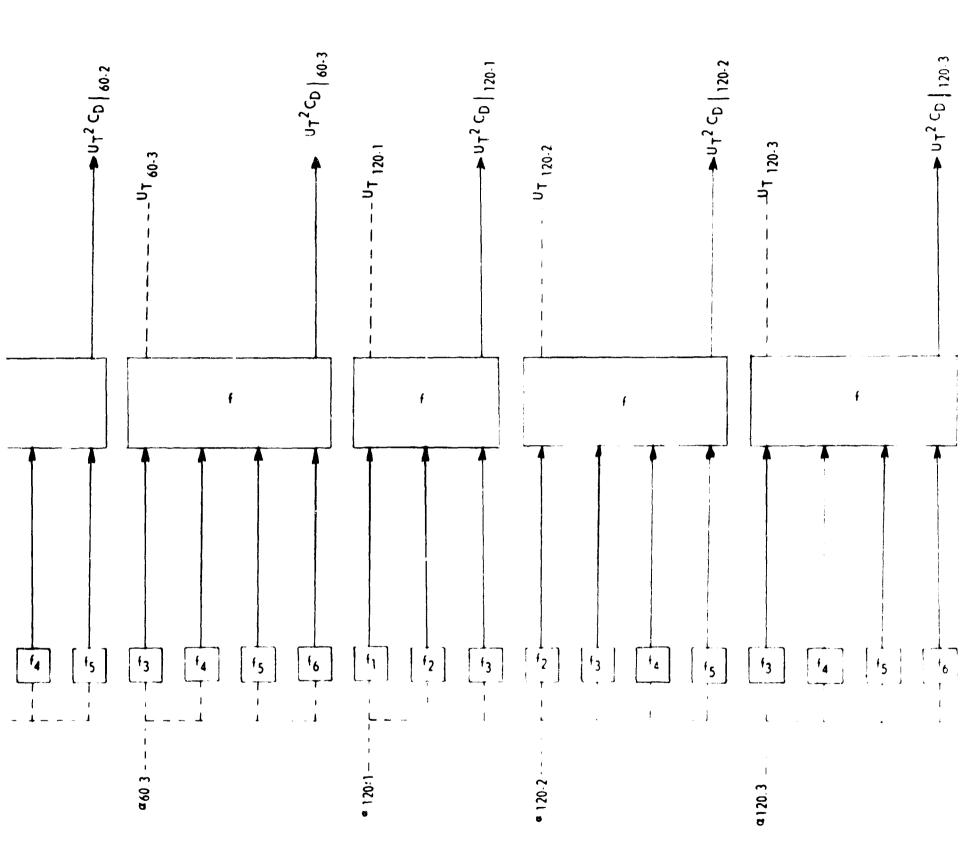
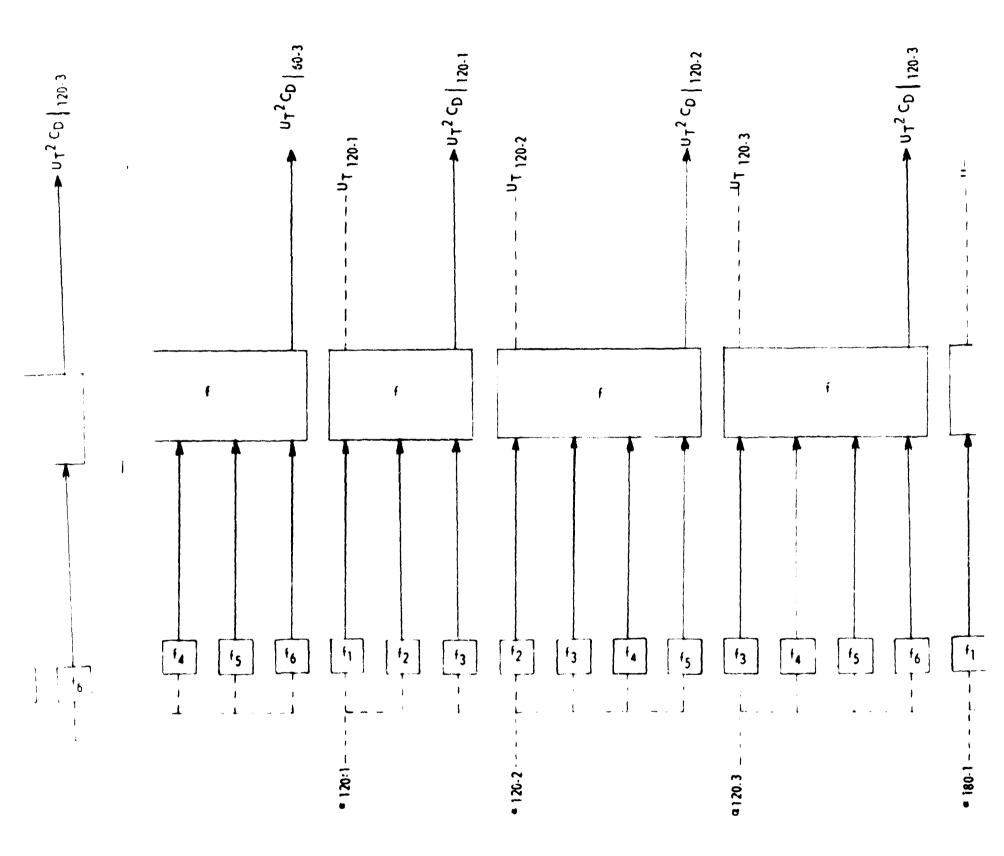


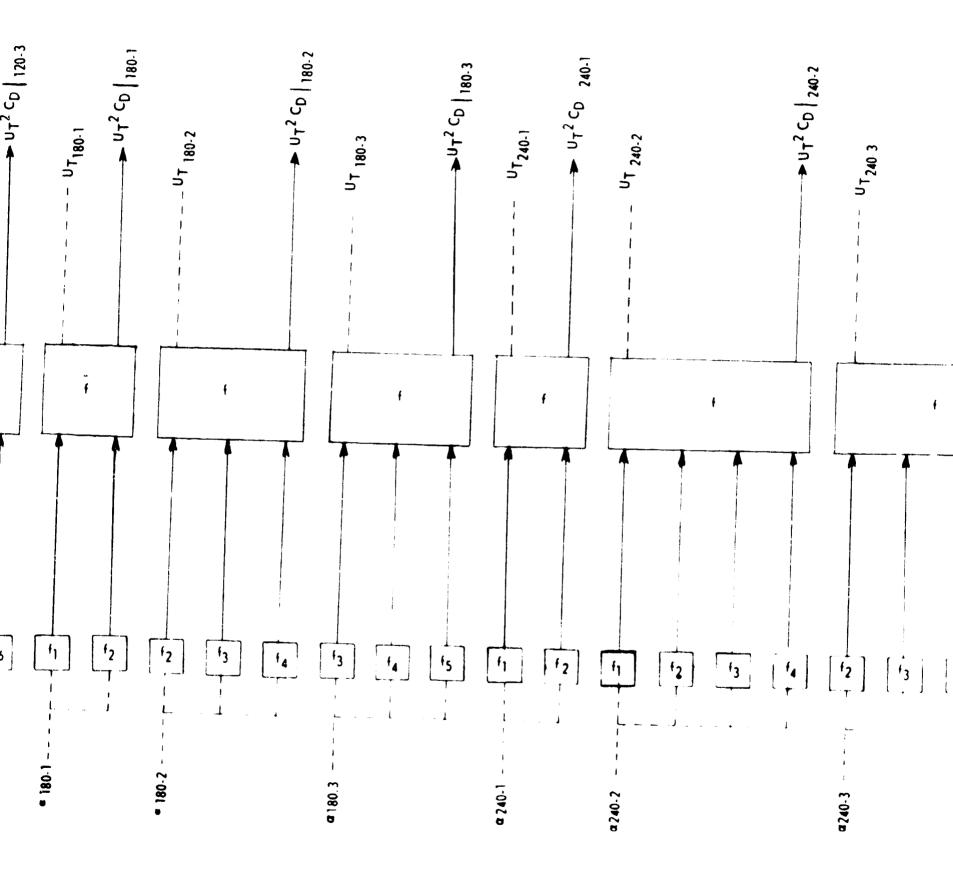
Figure 17. Blade Element Flapping Moment and Lift AC Mechanization

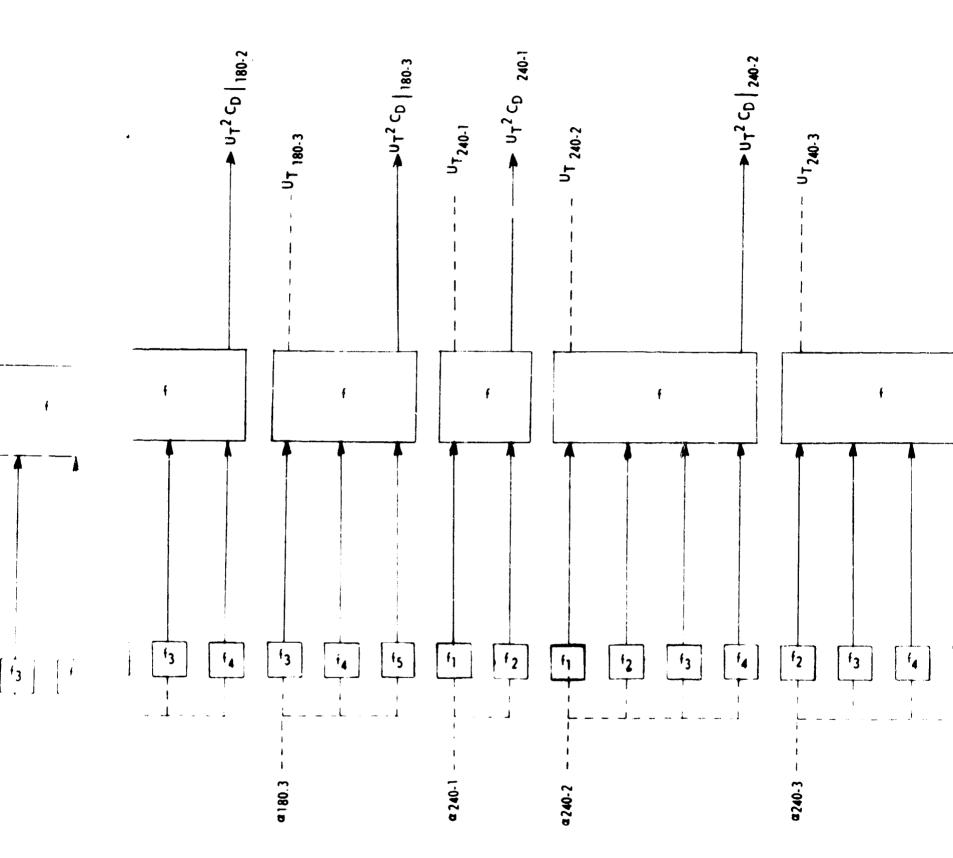












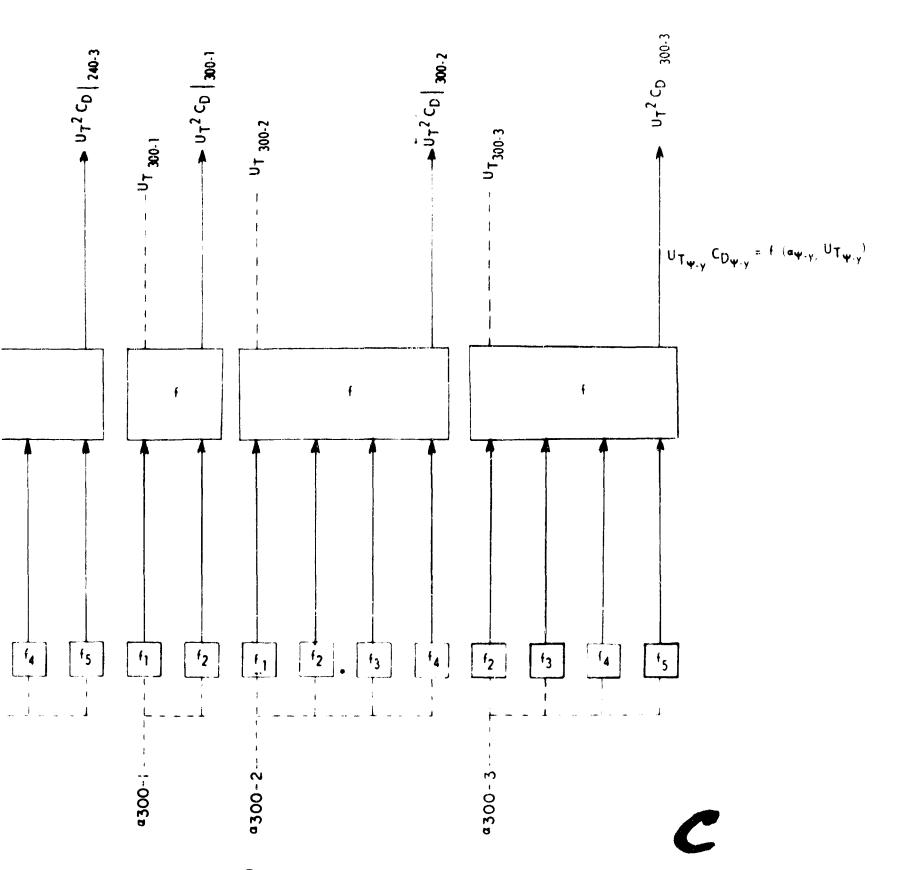
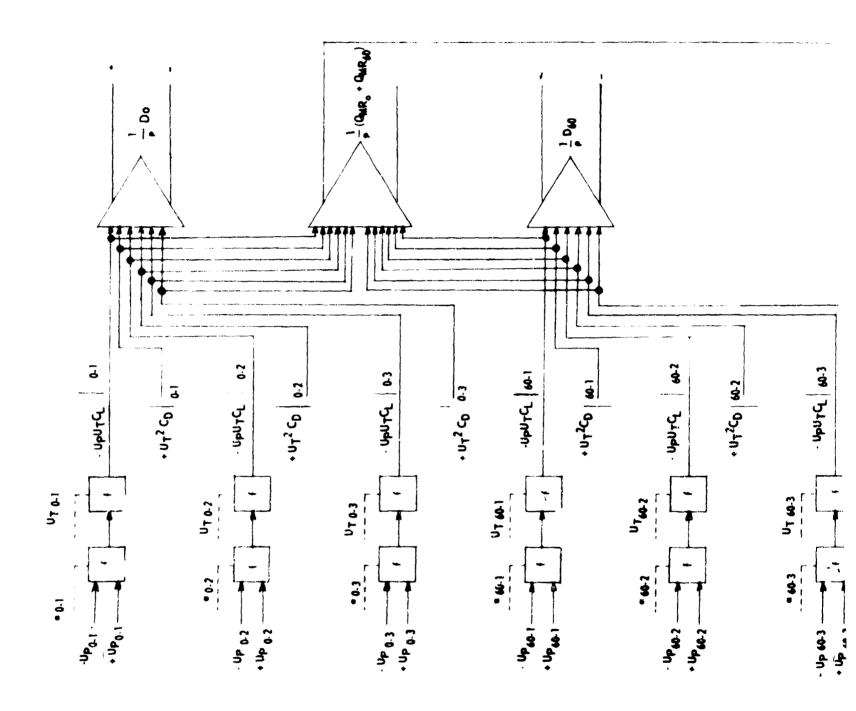
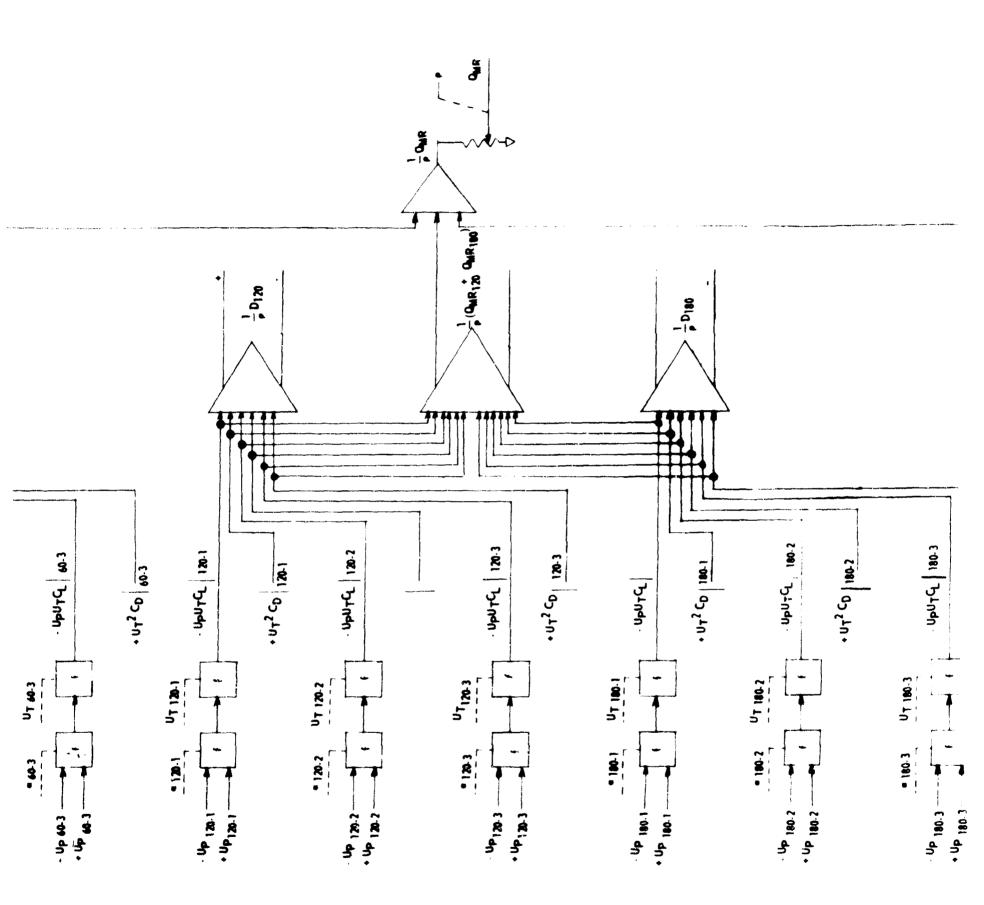
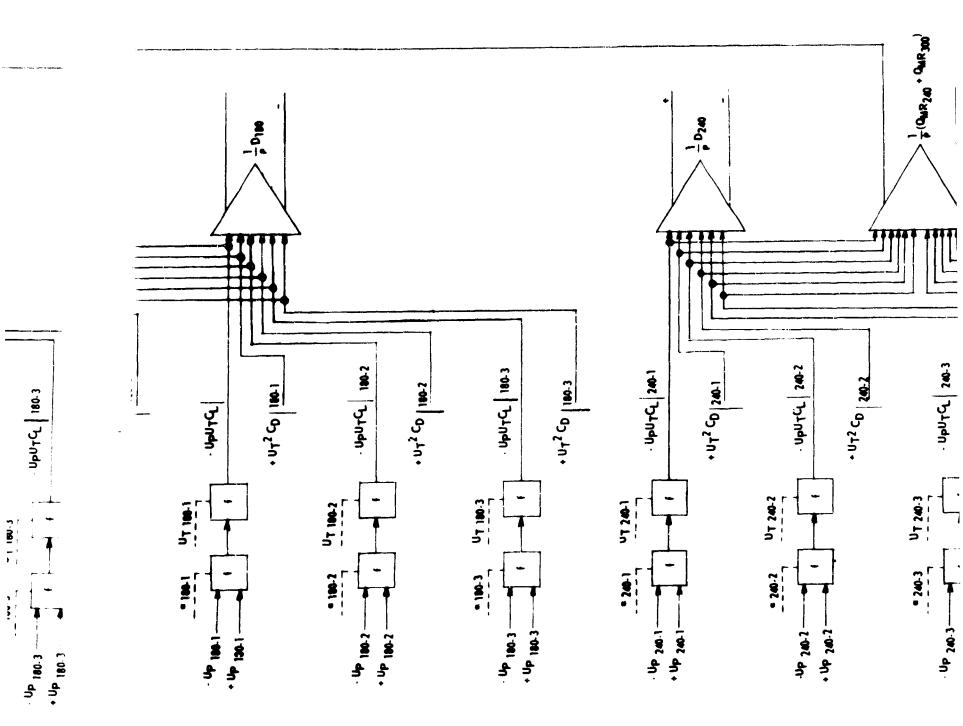


Figure 18 Blade Element Drag AC Mechanization









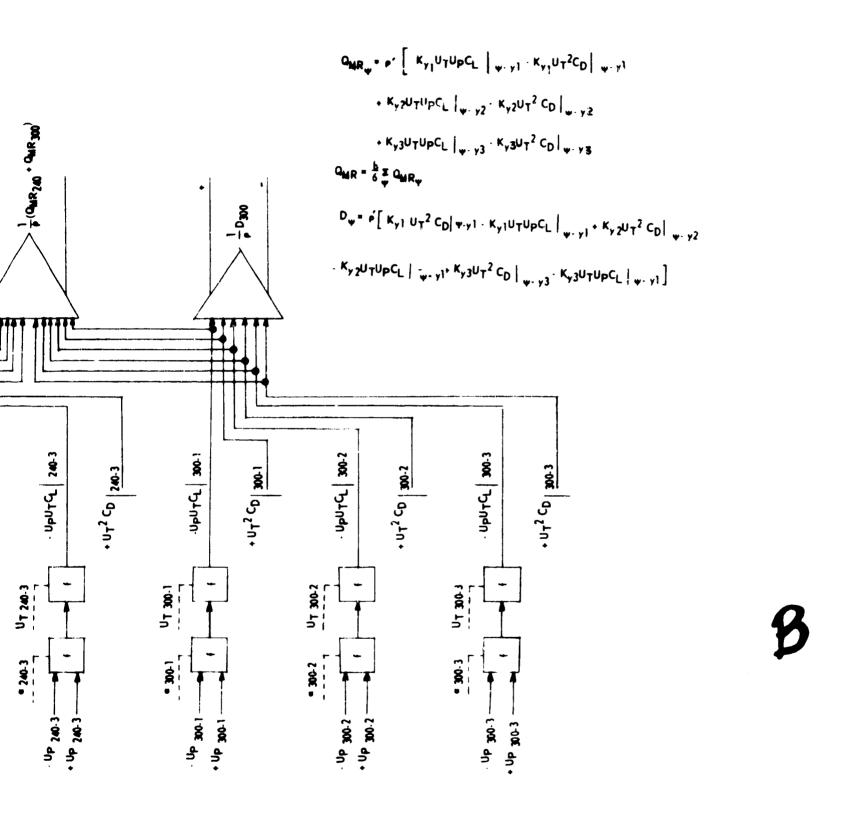


Figure 19 Blade Element Drag and Main Rotor Torque AC Mechanization

## NAVTRADEVCEN 1205-3

between AC and DC optimum mechanizations is the number of amplifiers required in the DC mechanization to provide both positive and negative functions. There are 9 amplifiers used in developing blade element drag and main rotor torque in Figure 19. Plus and mimus functions are available from each of these 9 amplifiers for the AC mechanization. In order to do the mechanization with DC components, 9 additional amplifiers are necessary for sign purposes. Table 13 reflects the component complexity of Figure 19.

	AC		D	С
Component	No.	Wt.	No.	Wt.
Amplifier	10	10	19	38
Function (f) Generation	36	-	36	-
Complexity		10		38

Table 13. Blade Element Drag and Main Rotor Torque

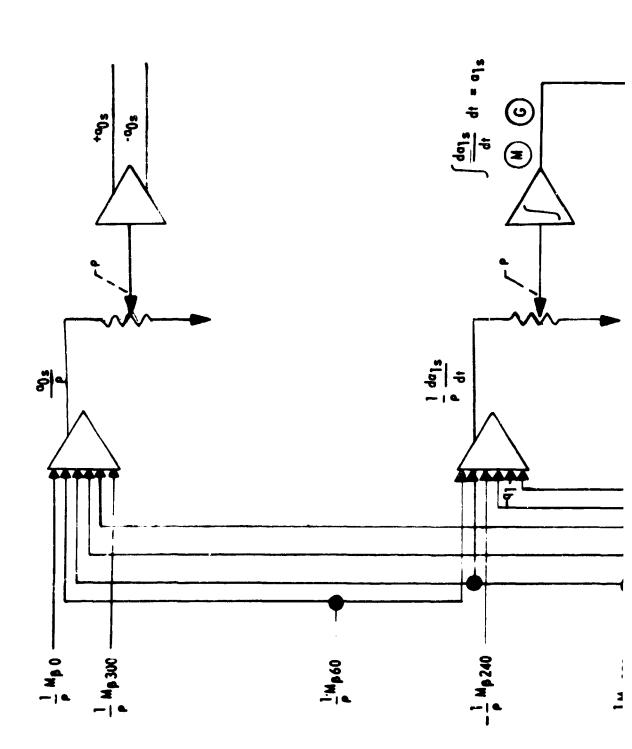
(7) Block (7) Flap Angle Coefficient and Main Rotor Lift. Figure 20 is the mechanization for flap angle coefficients and main rotor lift. The critical area in the optimization consideration is the requirement of positive and negative a os. DC methods in this mechanization require 1 additional amplifier. Table 14 reflects component complexity of Figure 20.

Component	<b>A</b> C		DC	
	No.	Wt.	No.	Wt.
Amplifier	8	8	9	18
Servo	2	υļ	2	14
Pots	_6	1 1/2	6	1 1/2
Function (f) Generation	2	•	2	-
Complexity		23 1/2		33 1/2

Table 14. Flap Angle Coefficients and Main Rotor Lift

(8) <u>Block (8) Blade Flap Angle</u>. The blade flap angle computation is the difference between flap angle coefficients to form the β outputs in the form of servo shaft positions. It is seen in Figure 21 that this mechanization would be equivalent in either an AC or a DC mechanization.







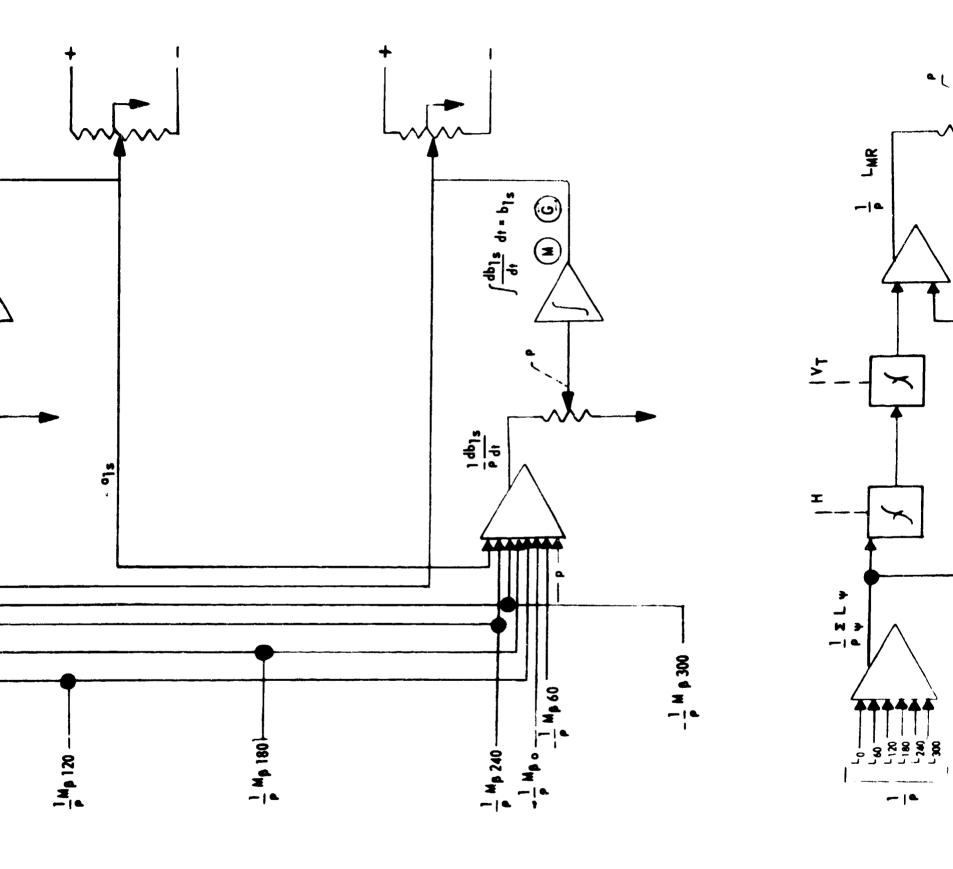
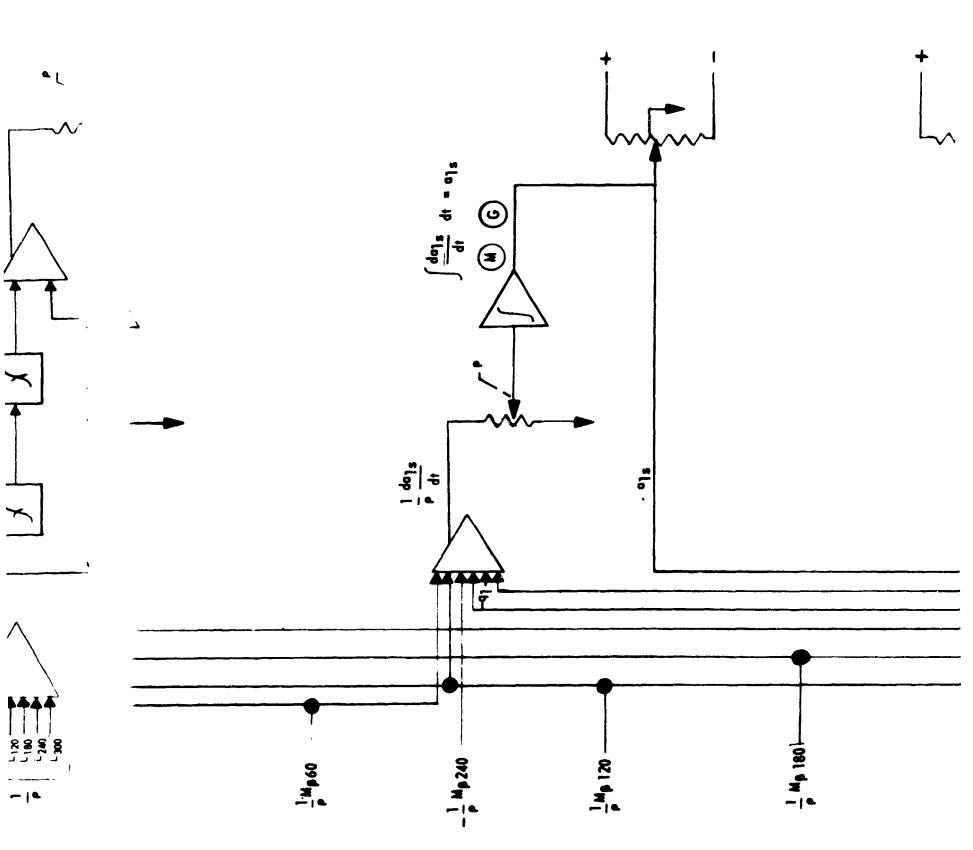


Figure 20. Flap Angle Coefficients and Main

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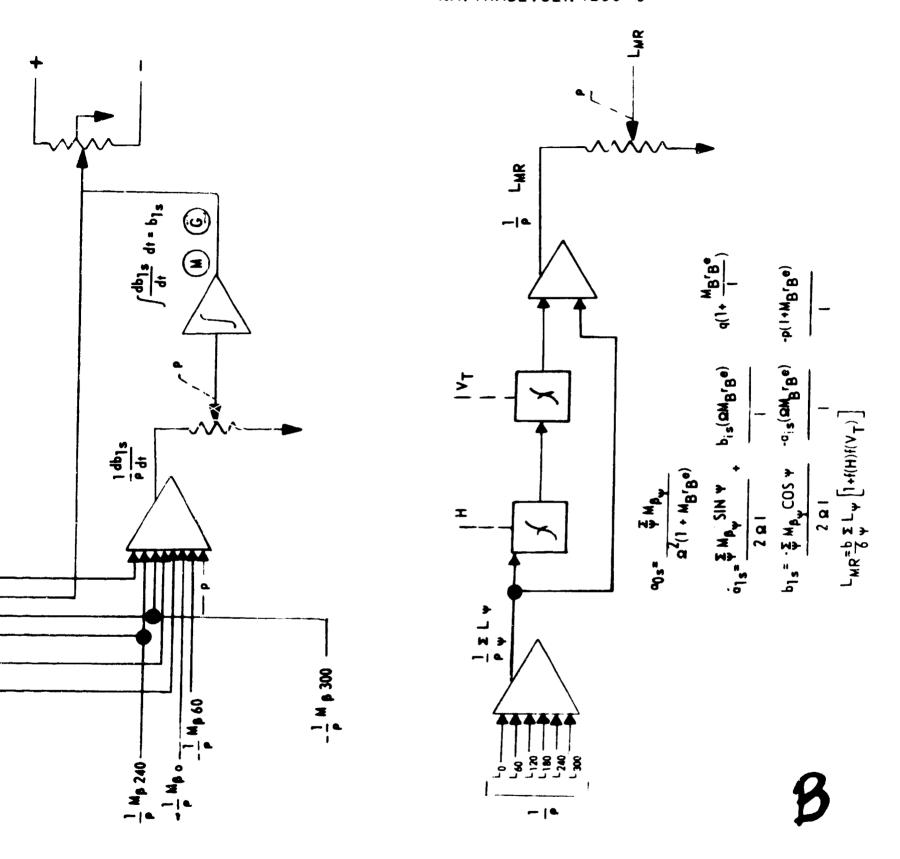


Figure 20. Flap Angle Coefficients and Main Rotor Lift AC Mechanization

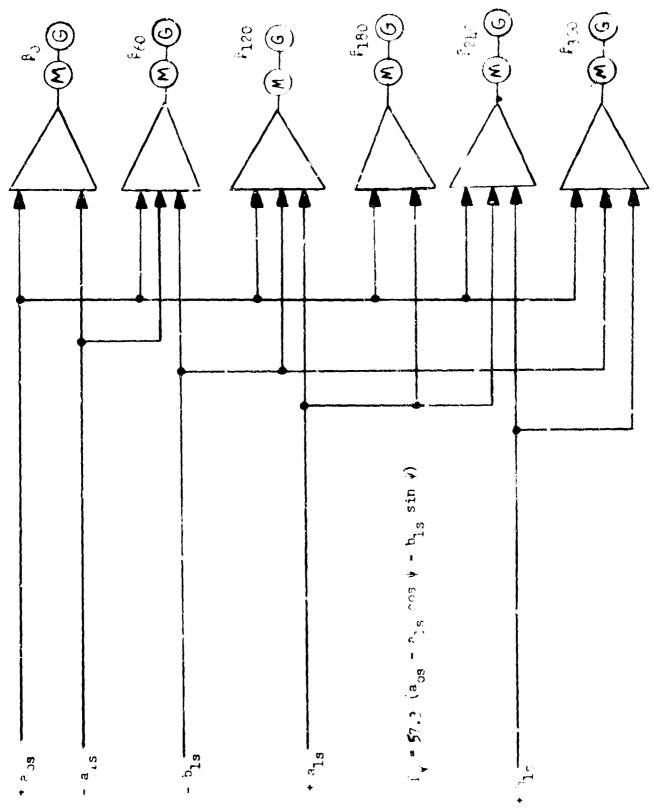


Figure 21. Blade Flap Angle AC Mechanization

## NAVTRALEVCEN 1205-3

(9) Block (9) Rotor Hub Moments. As seen in Figure 22, the rotor hub moments are functions of the sums of functions of blads element lift (L<sub>ψ</sub>), rotor angular velocity (Ω), flapping angle coefficients (a<sub>1s</sub>, b<sub>1s</sub>) and air density (ρ). The mechanization is a simple straightforward summation of functions and does not require a positive and negative output. Consequently, this method would also be equally optimum in either a DC or an AC system. Table 15 reflects component complexity of Figure 22.

	AC		nc	
Component	No.	Wt.	No.	Wt.
Amplifier	<u>i</u>	4	4	8
Pots	6	1 1/2	6	1 1/2
Complexity		5 1/2		9 1/2

Table 15. Rotor Hub Momenta

(10) Block (10) Rotor Forces and Angular Velocity. Figure 23 is the mechanization for the rotor forces. There is no area in the mechanization that will cause the AC to differ from the DC mechanization. The integration of the torque summation to obtain rotor angular velocity could be accomplished by an electronic DC integrator, but rotor angular velocity  $(\Omega)$  is required as a serve shaft position for multiplication  $(\Omega^2)$ . The mechanization as shown in Figure 23 can be done with the same amount of equipment in either a DC or AC system. Table 16 reflects the component complexity of Figure 23.

	AC		D	C
Component	No.	Wt.	No.	Wt.
Amplifier	3	3	3	6
Servo	1	7	1	7
Pots	10	2 1/2	10	2 1/2
Complexity		12 1/2		15 1/2

Table 16. Rotor Forces and Angular Velocity

This completes the rotor aerodynamics. The discussion will continue with Block (5) of Figure 23.

- 1 L 120 -+ 1 L240 -+ 1 L 300 -· 1 L0 + 1 L 120 -+ 1 L 180 -- 1 L 300 -

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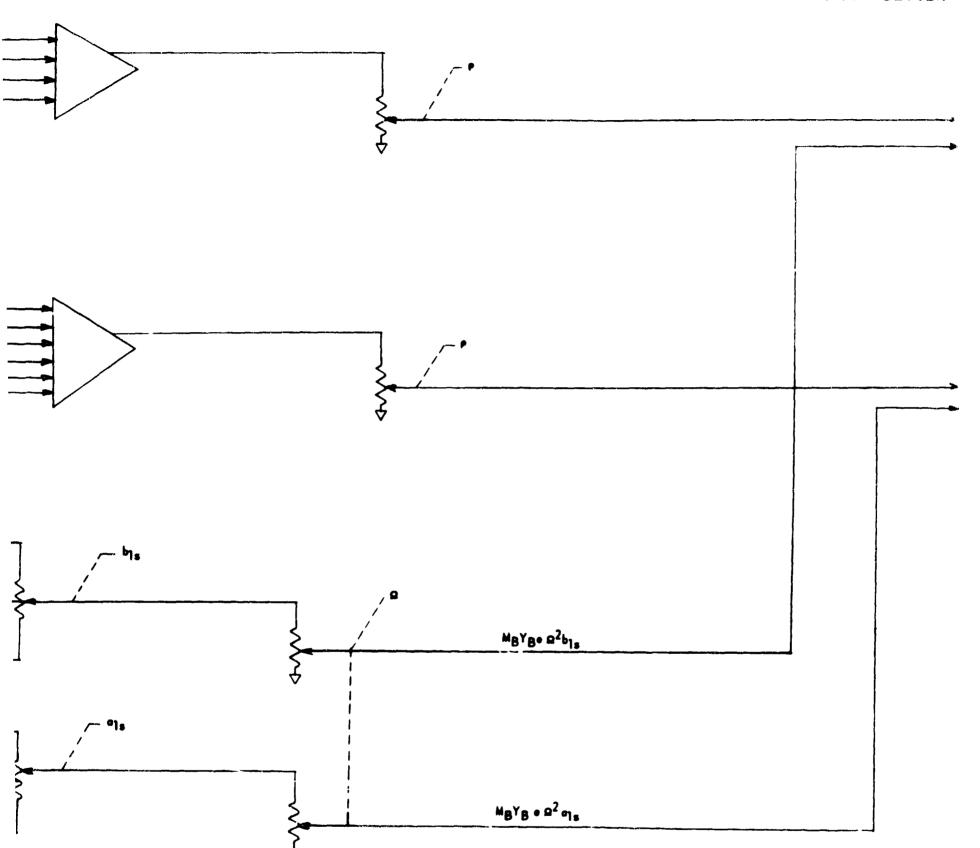
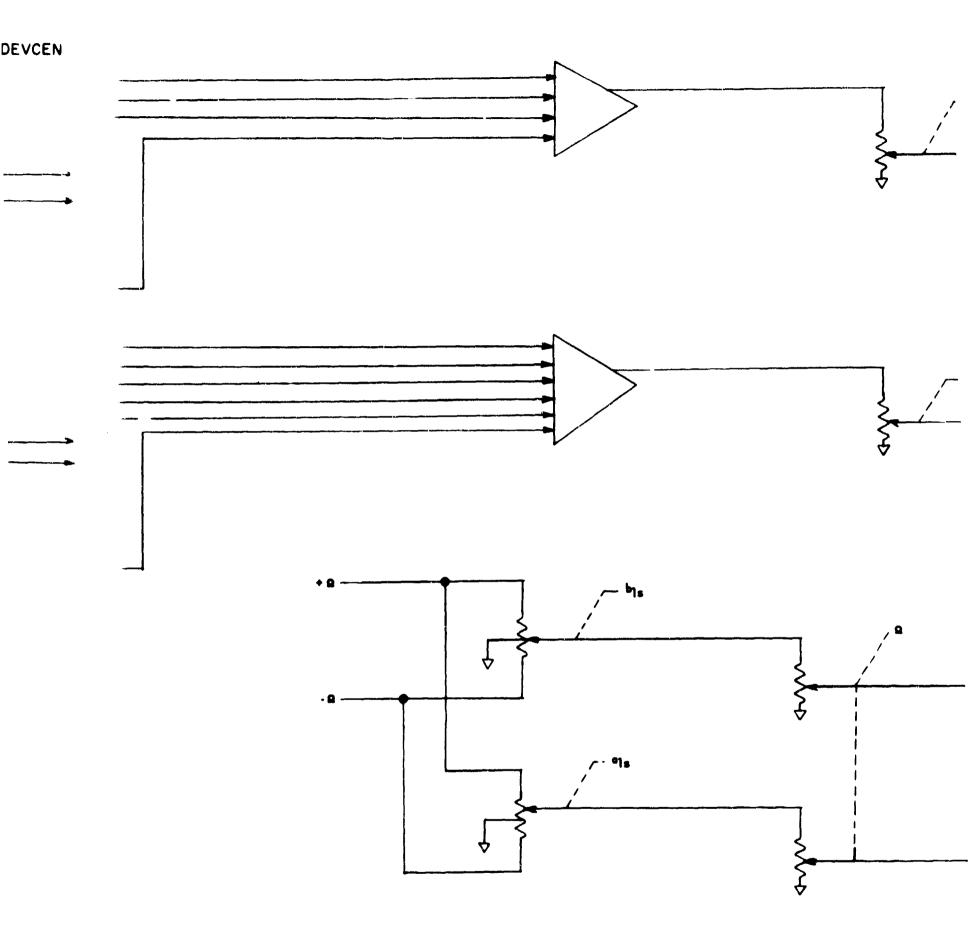


Figure 22. Rotor Hub Moments



loments

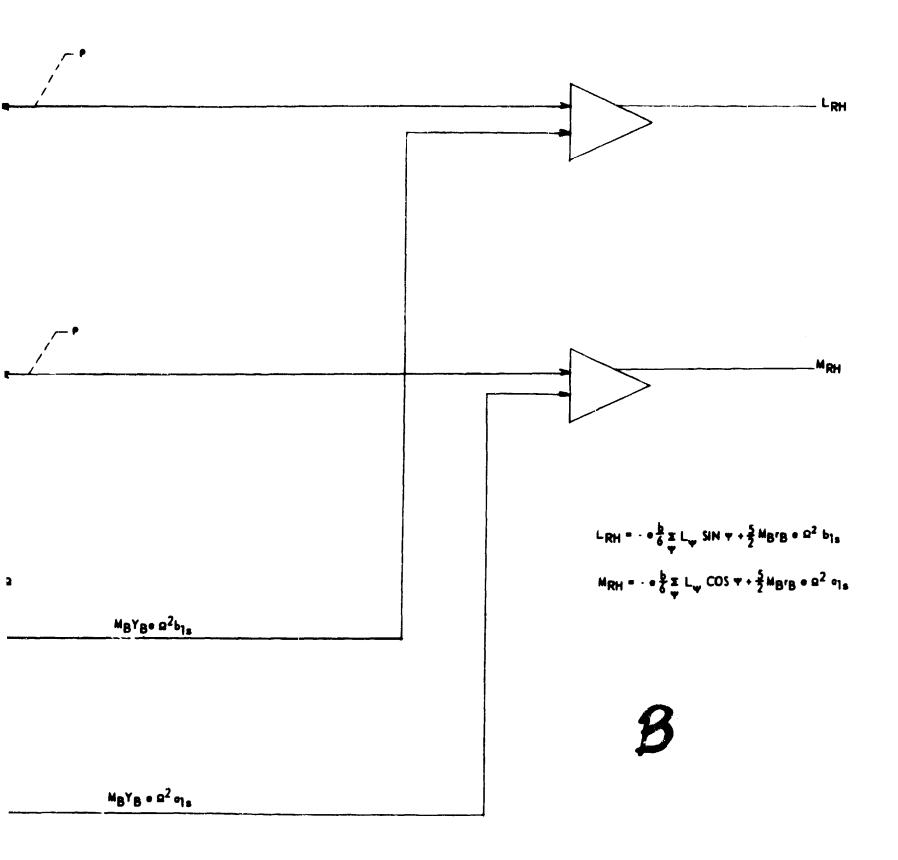
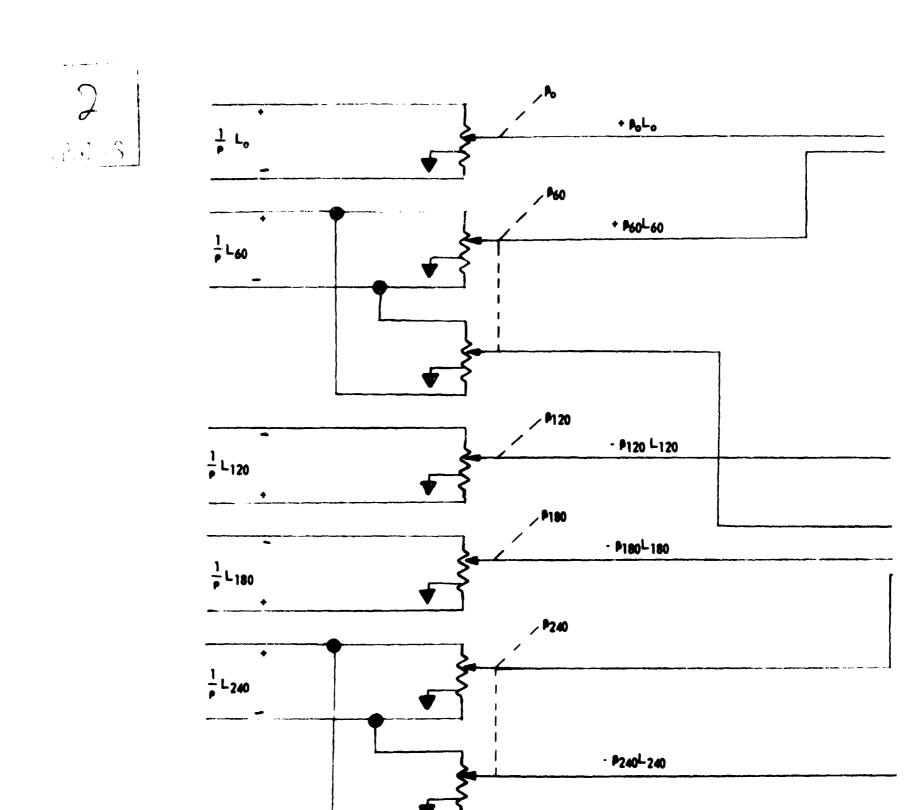


Figure 22. Rotor Hub Moments AC Mechanization

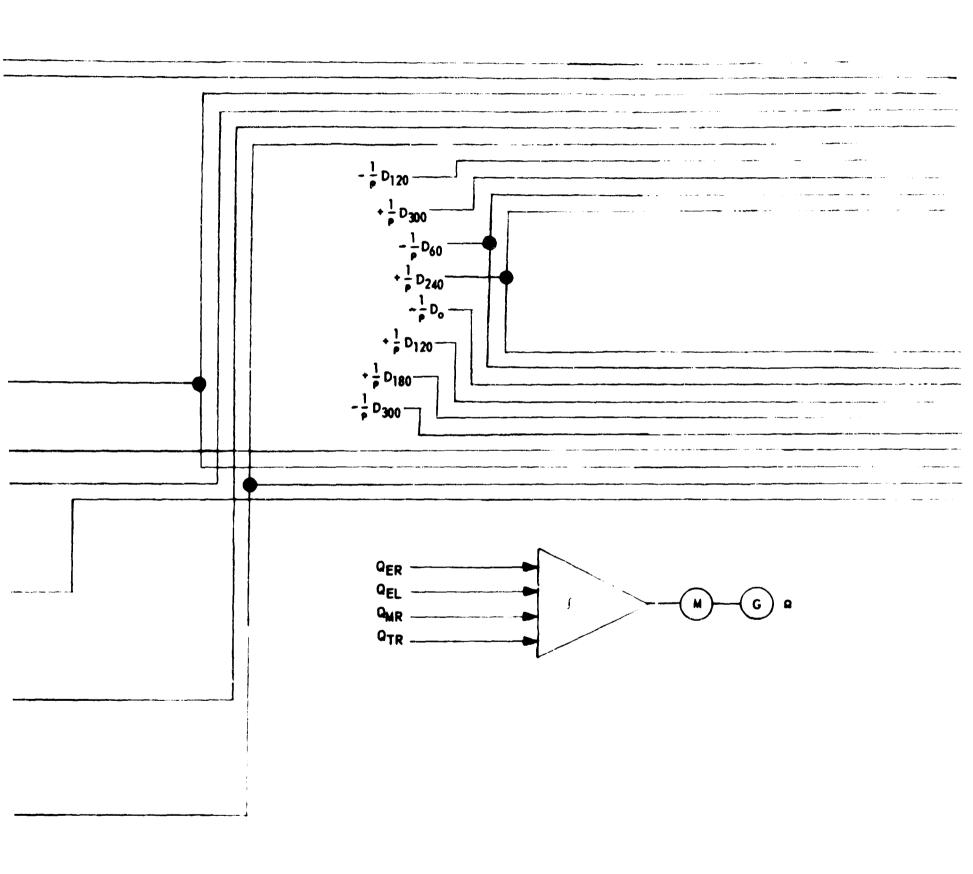


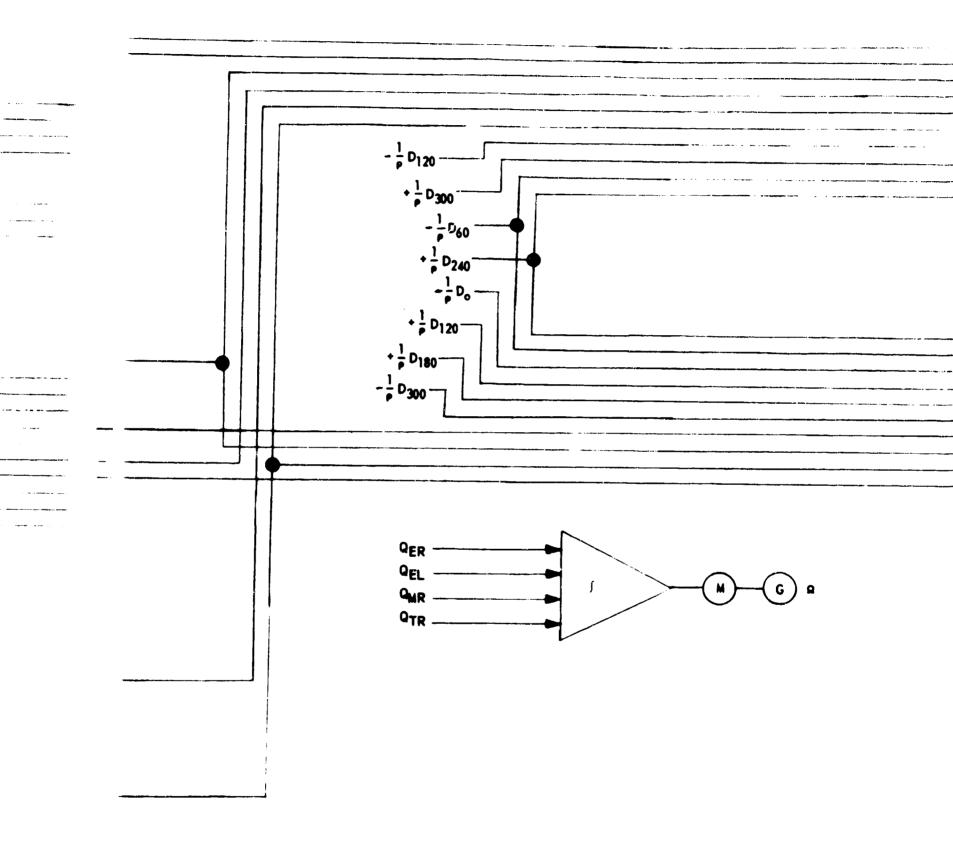
/ P300

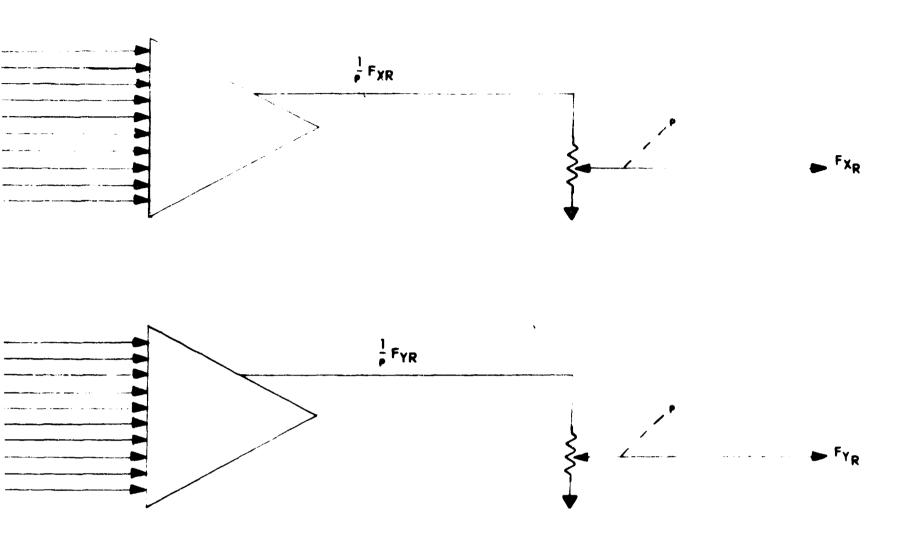
+ \$300<sup>L</sup> 300



 $\frac{1}{p}$  L<sub>300</sub>







## REFER TO EQUATIONS

$$F_{XR} = \frac{b}{6} \frac{\pi}{\Psi} (.0173 \, \mu_{\Psi} \, L_{\Psi} \, COS \, \Psi - D_{\Psi} \, SIN \, \Psi)$$

$$F_{YR} = \frac{b}{6} \frac{\pi}{\Psi} (..0173 \, \mu_{\Psi} \, L_{\Psi} \, SIN \, \Psi - D_{\Psi} \, COS \, \Psi)$$

$$\dot{\Omega} = \frac{Q_{MR} + Q_{TR} + Q_{ER} + Q_{EL} + Q_{RB} - 1700}{10, 275}$$

B

## NAVTRADEVCEN 1205-3

Block (5) Force  $\Sigma$ . The AC mechanisation of Block (5), Figure is shown in Figure 24. Equations 6.21, 6.24 and 6.27 are mechanised to give the force outputs ( $X_a$ ,  $Y_a$ ,  $Z_a$ ). Table 17 reflects the component complexity of Figure 24.

Component	<b>A</b> C		מ	C
	No.	Wt.	No.	Wt.
Amplifier	12	12	16	16
Servo				
S-C Pots	4	1	<u>L</u>	1
Complexity		13		17

Table 17. Force Summations

Four extra amplifiers are necessary for DC mechanisation so that both signs of a function are available for operation of the sine-cosine potentiometers in Figure 21.

Elock (6) Mass, c.g. Elock (6) of Figure 9 is mechanised as in Section III.A.

Hock (7) Moments and Block (9) Angular Rates. The AC mechanization of Blocks (7) and (9) Figure 9 is shown in Figure 25. Equations 6.30, 6.34 and 6.39 are mechanised to give outputs  $(L_a, H_a, H_a)$  and then each moment is integrated after dividing by the appropriate inertia term to give the angular rates  $(p,q_1, r)$ . The DC mechanisation is essentially the same as the AC mechanisation.

Blocks (8) through (14). These blocks of Figure 9 have been discussed in Section III.A. The correspondence between Figure 9 and Figure 1 is as follows:

Block (8), Figure 9 mechanised by Figure 3.

Flock (10), Figure 9 mechanised by Figure 4.

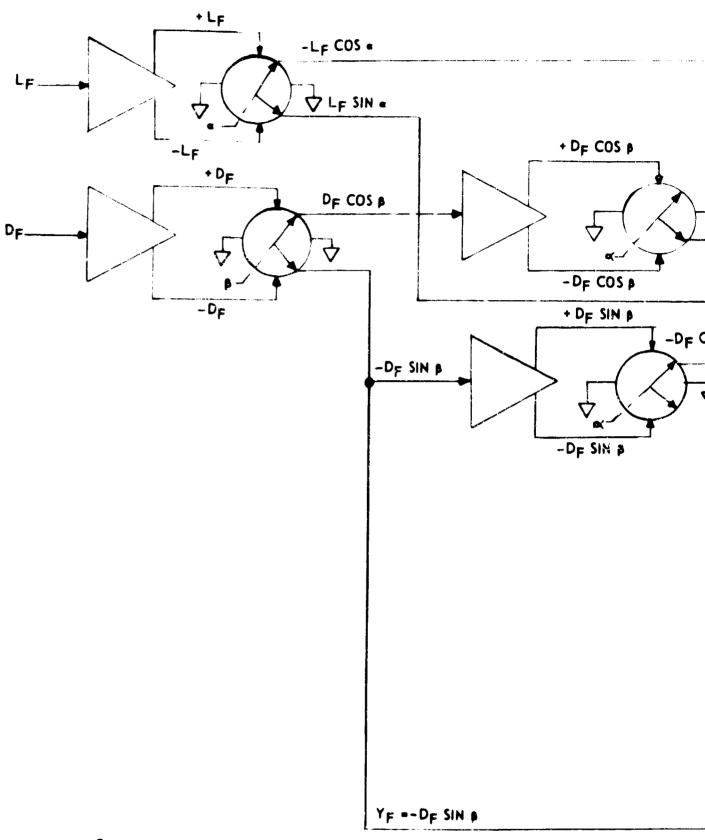
Block (11), Figure 9 mechanised by Figure 5.

Block (12h), Figure 9 mechanised by Figure 7.

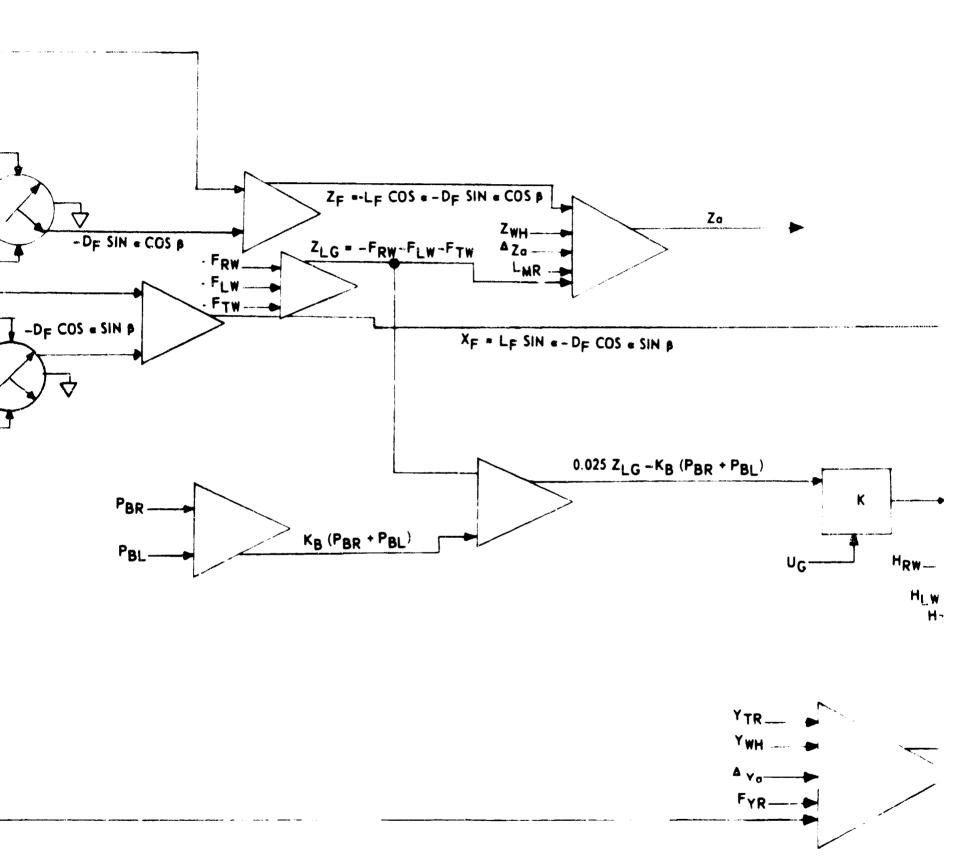
Mock (13h), Figure 9 mechanised by Figure 7.

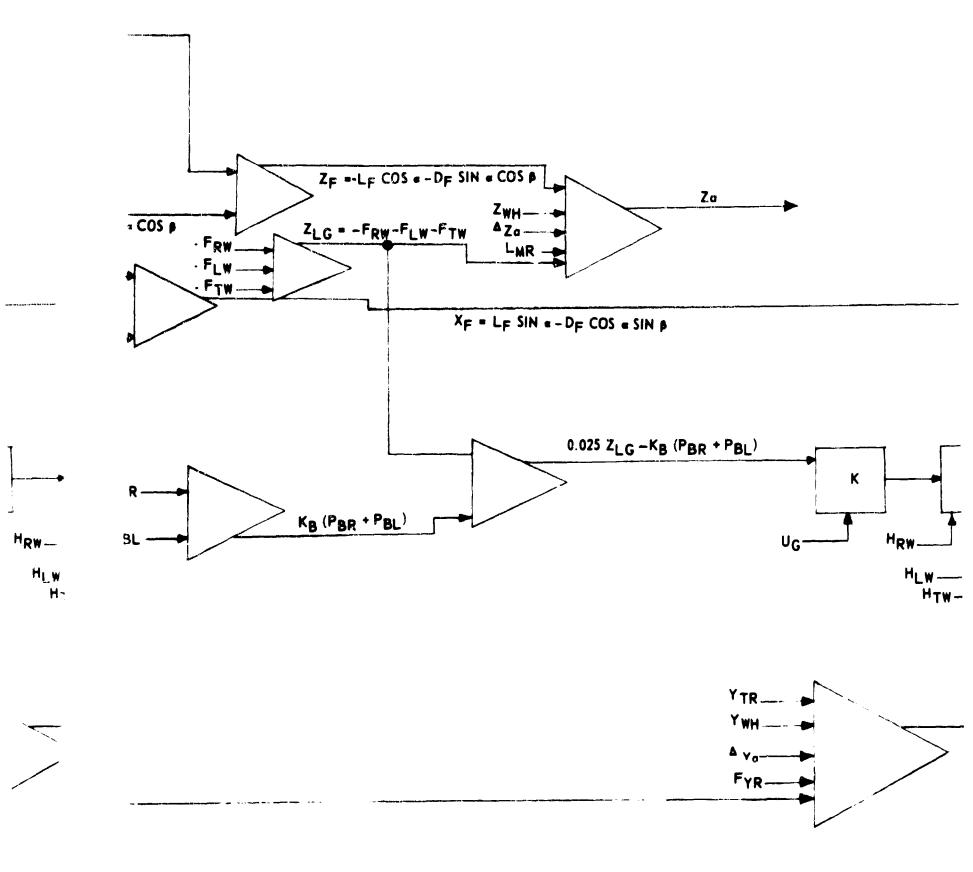
Block (14), Figure 9 instructor imputs as noted in Section III.A.

This completes the mechanisation of the single rotor helicopter.



A





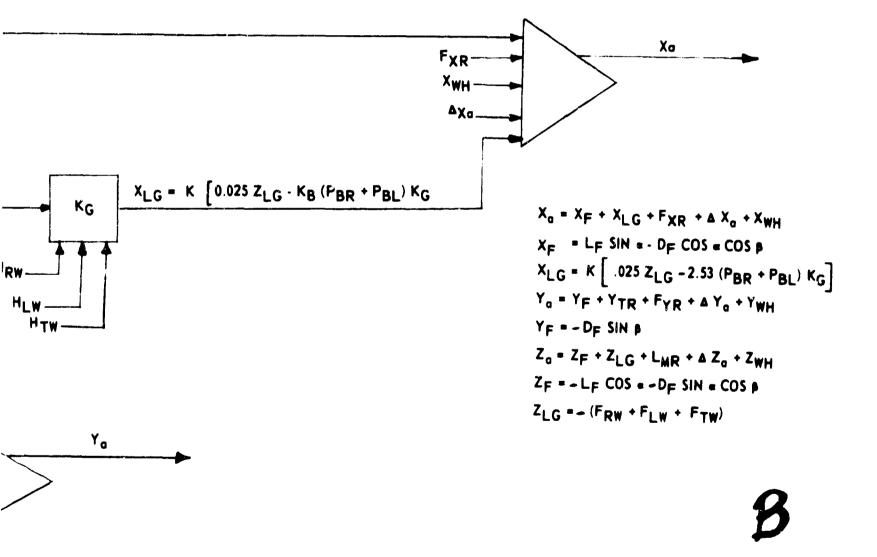
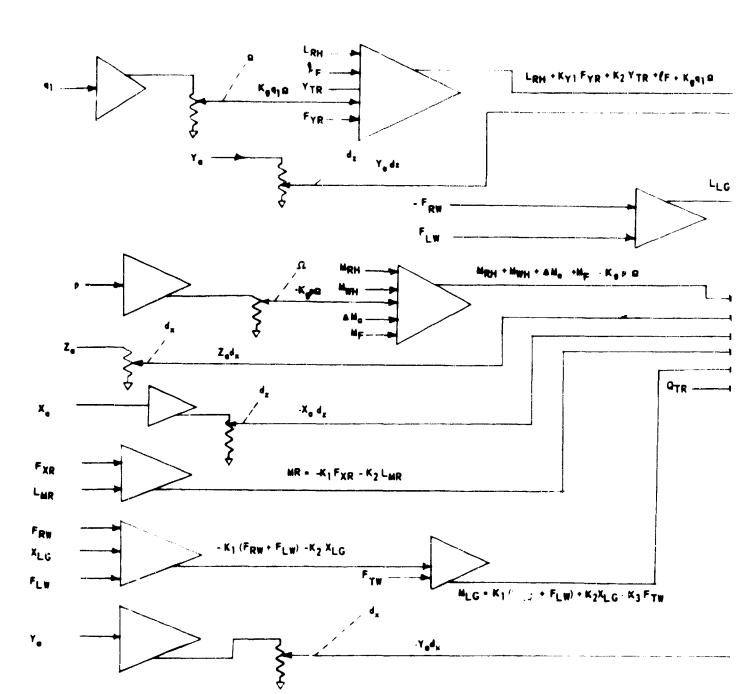
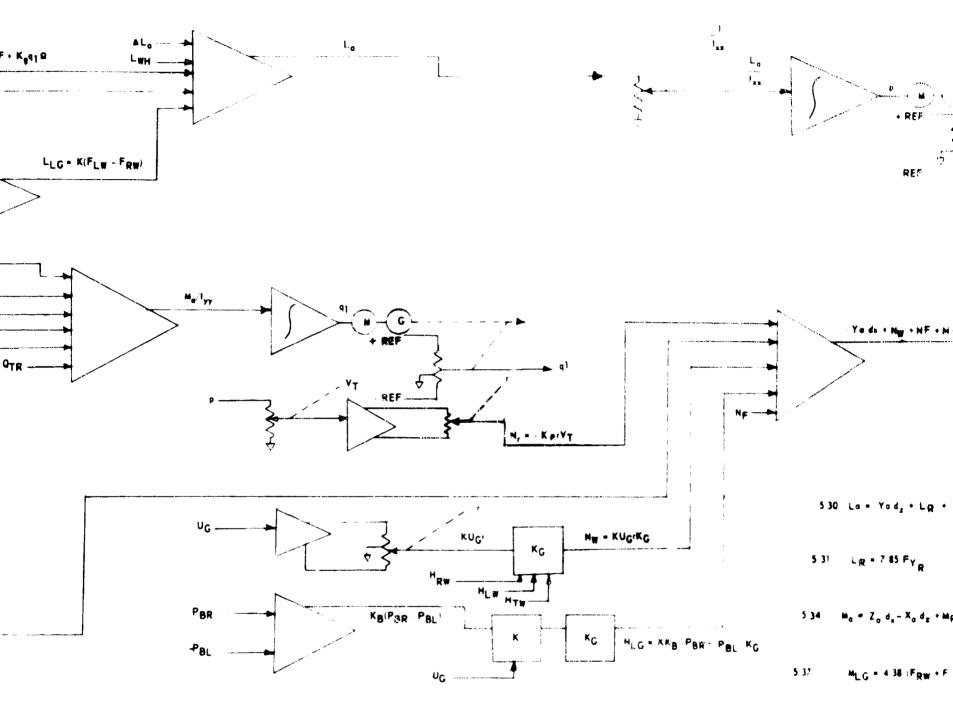
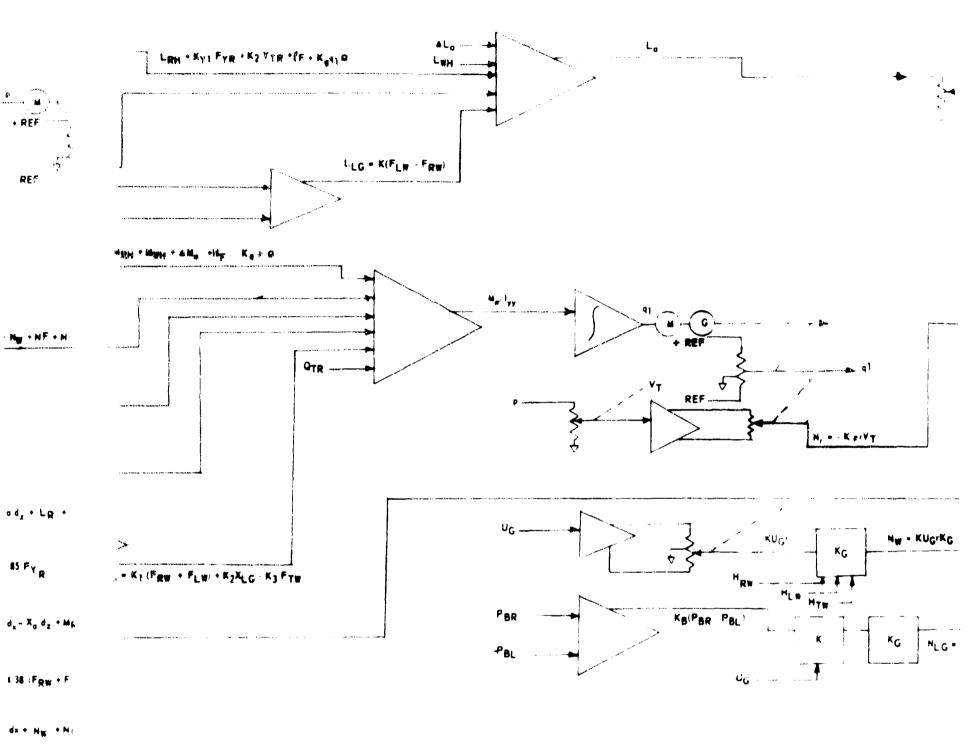


Figure 24. Force Summations AC Mechanization

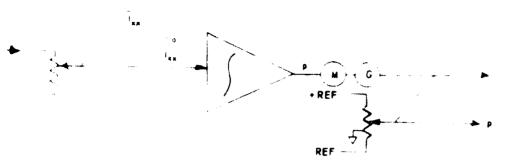


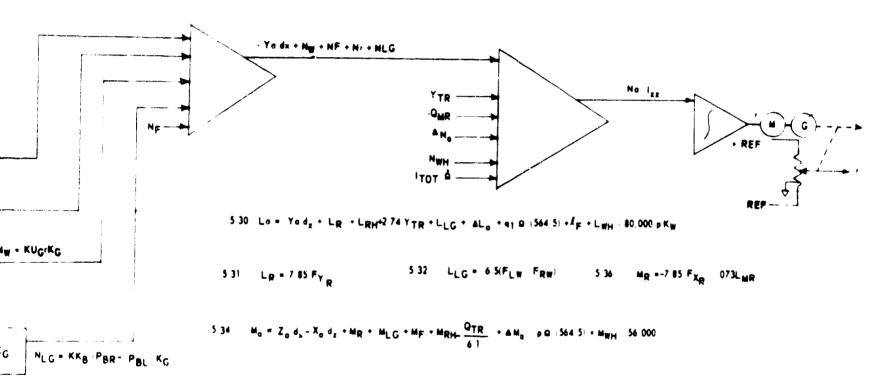






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$$5.80 \qquad q_1 = \frac{M_0}{I_{yy}} \quad dr \qquad 5.81 \qquad r = j \frac{N_0}{I_{zz}} \quad dr$$

B

Summary Single Rotor Helicopter. Figure 1, the general block diagram of the equation solution of the single rotor helicopter, has been developed block by block. Table 18 is a tabulation of the various components (amplifier, servo, potentiometer, sine-cosine potentiometer, and resolver) for the single rotor helicopter. It should be noted that items specified as functions generated in the mechanization have not been included in Table 18 since they are assumed to be potentiometer derived and the same for both AC and DC mechanizations. In order to compare AC and DC systems the weight factors used by Mark E. Connelly in reference 4 are applied to the totals which result in Table 18. The weights resulting from each component are tabulated in Table 19. The summary in Table 19 gives the complexity of the single rotor helicopter for AC and DC systems. The AC system has a complexity of 751-3/4 versus 1106-1/2 for the DC system. This is a marked difference. The difference is primarily due to using a weight factor of two (2) for the DC amplifier and one (1) for the AC amplifier.

	Ampl	ifiers	Ser	70	Po	ts	S-C	Pots	Reso.	ver
	AC	x	AC	Œ	<b>A</b> C	DC	AC	nc	AC	Œ
Block (1)										
Block (2)										
Block (3)	12	18	6	6	5	5	4		2	
Block (4)	118	167	52	52	73	73		1,	2	
Block (5)	12	16			4	4				
Block (6)	3	3	3	3	2	2				
Block (7)(9)	20	20	3	3	12	12				
Block (8)	4	5	3	3	7	7	2	2		
Block (10)	9	15	3	3				6	2	
Block (11)	7	12	3	3			2	4	1	
Block (12)	3	5	1	1	1	1				
Block (13)	6	ı).	1	1	1		1	6	3	
Block (14)										
TOTAL	194	275	75	75	10li	104	9	22	10	

Table 18. Single Rotor Tabulation

NAVTRADEVCEN 1205-3

	A	С	D	С
	No.	Wt.	No.	Wt.
Amplifier	194	194	275	550
Servo	<u>75</u>	525	75	525
Pot	104	26	104	26
S-C Pots	9	1 3/4	22	5 1/2
Resolver	10	5		
Complexity		751 3/4		1106 1/2

Table 19. Single Rotor Summary

Suppose that both AC and DC emplifiers both have weight one (1), then the DC complexity is 831-1/2 which is closer but still larger than the AC complexity. This difference (751-3/4 and 831-1/2) is primarily due to the increased umber of DC amplifiers necessary to solve the mechanization problem. Consequently, unless DC amplifiers can be redesigned to be competitive in complexity with AC amplifiers or the choice for a DC system is based on reasons other than component complexity, the AC system is favored.

TANDEM ROTOR HELICOPTER. The mechanization of a tandem rotor helicopter simulation equations can be accomplished by again considering Figure 9 which is the block diagram of the single rotor helicopter. The difference in mechanization between single and tandem rotor helicopters is contained in Block (4) Figure 9 -- the aerodynamic terms. The aerodynamic terms for the single rotor helicopter were considered in three parts -- tail rotor aerodynamics, fuselage aerodynamic and main rotor aerodynamics. For the mechanization of the tandem rotor the merodynamic terms are in two parts--fuselage aerodynamics and rotor aerodynamics. In reference 1 it was shown that the rotor equations of motion of the tandem rotor helicopter could be developed by using a set of equations similar to the single rotor helicopter. The essence of this development in reference 1 is that equations describing the main rotor of the single rotor helicopter are used to describe the forward rotor of the tandem rotor helicopter. Rear rotor effects in the tandem rotor helicopter are mechanized by ratios of the swash plate angles of front and rear rotor. Only the front rotor is simulated. Since this is an overlap tandem rotor helicopter (CH-46A), effects of rotor interference are also mechanized.

In Section VI, equations 6.91 through 6.169 for a tandem rotor helicopter—the CH\_L6A are presented. These equations are directly analogous to equations 6-1 through 6-90 of the single rotor helicopter. Table 20 is a comparison of single and tandem rotor equations and associated figures used in the single rotor mechanization. Table 20

	Single Rotor Equation Nos.	Mechanized by Figure(s)	Comparable Tandem Rotor Equation Nos.	Mechanized by Figure(s)
Block (1)	N/A	N/A	N/A	N/A
Block (2)	N/A	n/a	N/A	N/A
Block (3)	6.1, 6.2, 6.6 6.82	10	6.91, 6.92, 6.95 6.161	10
Block (4)				
Tail Rotor	6.7 to 6.17, 6.26	11	None	N/A
Fuselage	6.4, 6.5, 6.33, 6.38, 6.41	12	6.94, 6.93, 5.108 6.112, 6.116	12
Aft Rotor	None	N/A	6.107, 6.111, 6.115, 6.126, 6.129, 6.132, 6.134, 6.143, 6.145	26, 27
Rotor	(Main) Rotor		(Front) Rotor	
Block (1)	6.45	υl	6.119	זאָו
Block (2)	6.hh	15	6.118	15
Block (3)	6.46, 6.47, 6.48	16	6.120, 6.121, 6.122	16
Block (4)	6.49, 6.52	17	6.123, 6.127	17
Block (5)	6.58	18	6.136	18
Block (6)	6.50, 6.51, 6.54	19	6.124, 6.125, 6.130	19
Block (7)	6.53, 6.61, 6.62 6.63	20	6.128, 6.139, 6.140 6.141	20
Block (8)	6.59	21	6.137	21
Block (9)	6.64, 6.65	22	6.142, 6.144	22
Block (10)	6.55, 6.56, 6.83	23	6.131, 6.133, (6.162)	23 28
Hlock (5)	6.21, 6.22, 6.23 6.24, 6.25, 6.27 6.28, 6.29	2և	6.99, 6.100, 6.97 6.101, 6.102 6.103, 6.104, 6.96	5 ft

Table 20. Single Rotor - Tandem Rotor Comparison

	Single Rotor Equation Nos.	Mechanised by Figure(s)	Comparable Tandem Rotor Equation Nos.	Mechanised by Figure(s)
Block (6)	6.90	2	6.169	2
Block (7) and (9)	6.30, 6.31, 6.32 6.34, 6.36, 6.37 6.39, 6.40, 6.42 6.43, 6.79, 6.80 6.81	25	6.105, 6.106, 6.98 6.109, 6.110 6.113, 6.117 6.158, 6.159, 6.160	25
Block (8)	6.67, 6.68, 6.69	3	6.146, 6.147, 6.148	3
Block (10)	6.70, 6.71, 6.72 6.84, 6.85, 6.86	4	6.149, 6.150, 6.151 6.163, 6.164, 6.165	4
Block (11)	6.87, 6.88, 6.89	5	6.166, 6.167, 6.168	5
Block 12h and 13h	6.73, 6.74, 6.75 6.76, 6.77, 6.78	7	6.152, 6.153, 6.154 6.155, 6.156, 6.157	7
Block (14)	N/A	n/a	N/A	N/A

Table 20. Single Rotor - Tandem Rotor Comparison (Cont'd.)

thus enables the identification of figures used in the single rotor mechanization with tandem rotor equations and a consequent count of electronic components. Note that the particular imputs to some of the amplifiers may increase or decrease in the tandem rotor helicopter as compared to the single rotor but the components associated with the figures listed in Table 20 will be the same.

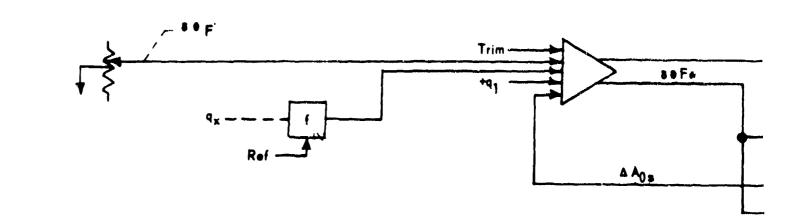
In order to describe the aft rotor, a few additional equations are necessary. The additional equations needed are 6.107, 6.111, 6.115, 6.126, 6.129, 6.132, 6.134, 6.143 and 6.145. Before mechanising these equations, the aft rotor swash plate angles will be mechanised.

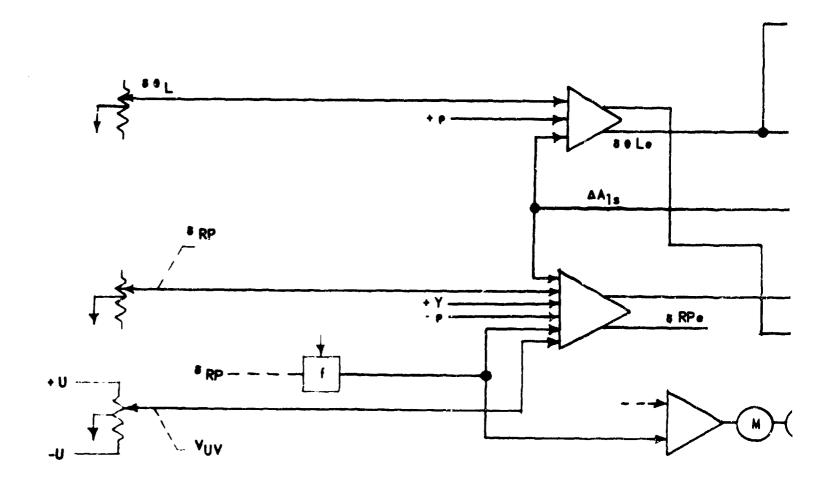
The swash plate angles and SAS mechanisation considered for the tandem helicopter simulation is an addition to the rotor aerodynamics of the single rotor device. In this mechanisation the swash plate angles are developed in order that aft rotor terms are written as functions of forward rotor terms. Figure 26 is the mechanisation of these functions. The DC mechanisation would require three additional amplifiers by virtue of the requirement of three functions of both polarities. Servo integrators are used to obtain the delta swash plate functions. A DC mechanisation using electronic integrators would require follower position servos.

Figure 27 shows the AC mechanisation of the aft rotor equations. There are 12 amplifiers and 4 potentiomsters used in the AC mechanisation plus functions not specified as to equipment. The DC mechanisation would require 15 amplifiers and 4 potentiomsters plus the functions. The additional amplifiers in the DC mechanisations are due to polarity of functions.

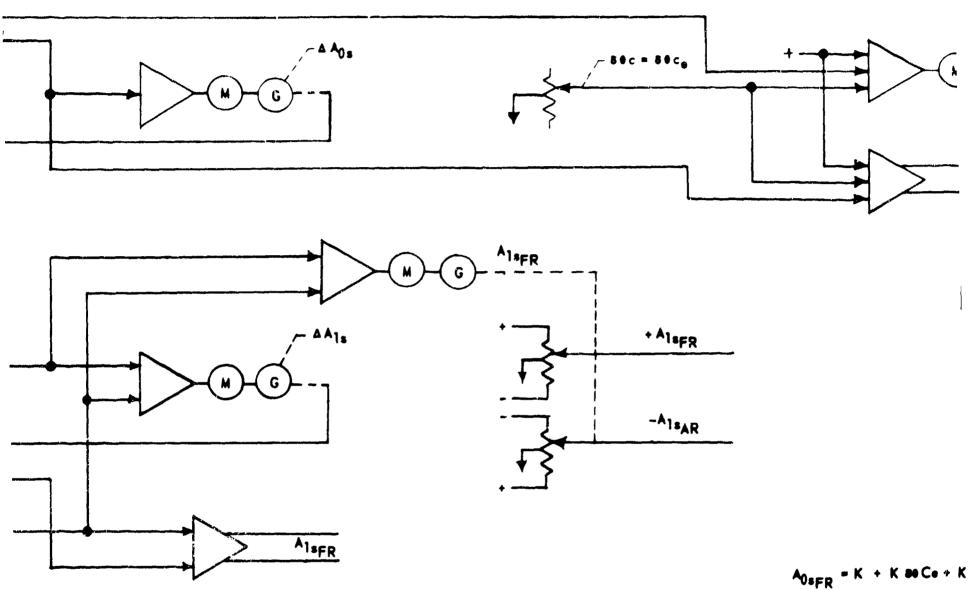
One further area is of interest in the tandem rotor simulation—angular velocity. The mechanisation of the dual rotor angular velocity computation is shown in Figure 28. In comparison to the single rotor angular velocity mechanisation, Figure 23, it is seen that  $\Omega$  is computed essentially the same way as in Figure 23 but there are now two rotor torque terms. One is the torque contributed by the forward rotor. The other term is the torque contributed by the aft rotor.

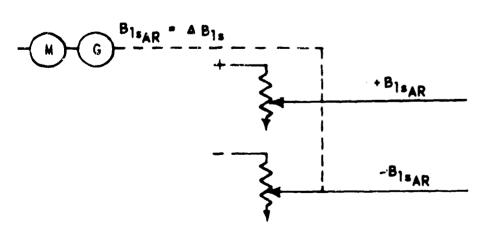
Table 21 is a summary of the components necessary to mechanise the tandem rotor helicopter in addition to those necessary for the single rotor helicopter less tail rotor as reflected in Figures 26, 27 and 28. The numbers under function generation in Table 21 would actually be mechanized by potentiometers. It is assumed that where functions (f) are used in the mechanization drawings, the mechanisation can be accomplished by the same amount of equipment—AC or NC.





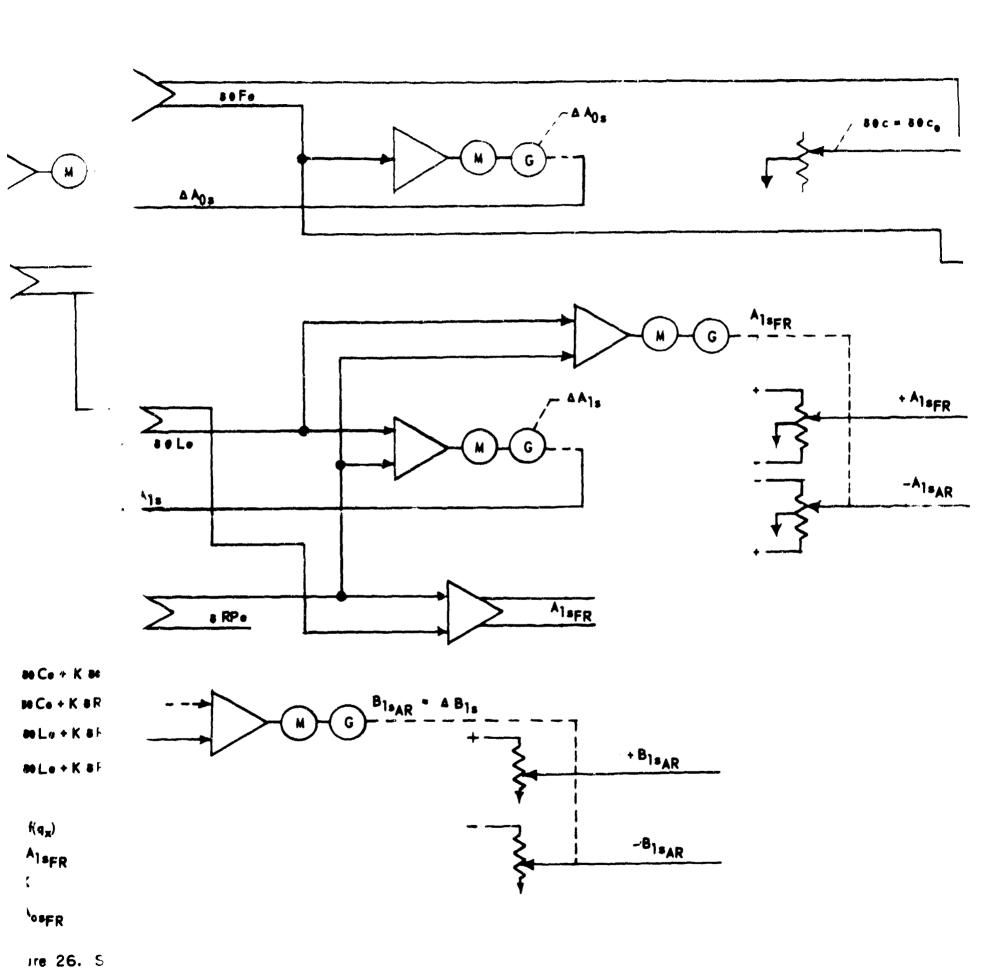


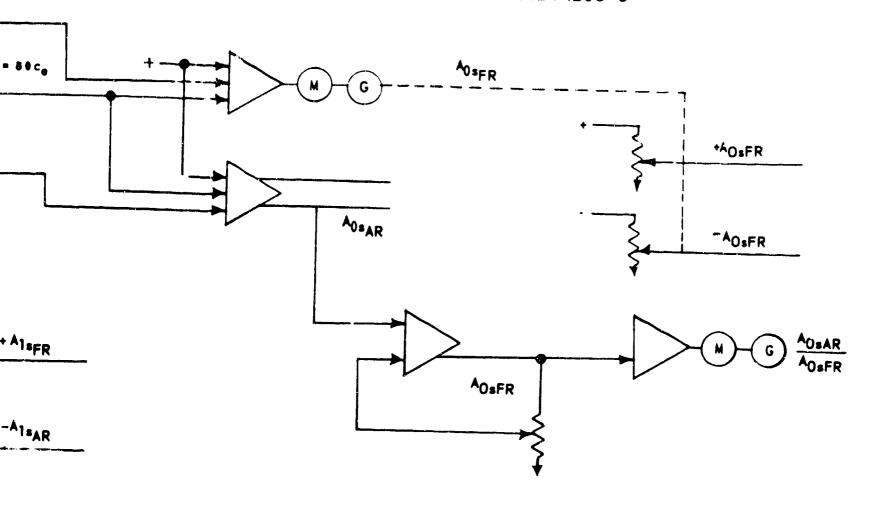




A0sAR = K + K seCe + K
A1sFR = + seLu + K
A1sAR = - seLu + K
B1sFR = K
B1sAR = -K + K f(q<sub>x</sub>)
AA1s = A1sAR - A1sFR
AB1s = B1sAR - K
AA1s = A0sAR - AosFR

Figure 26.





$$A_{0sFR} = K + K \sec Ce + K \sec Fe$$

$$A_{0sAR} = K + K \sec Ce + K \sec Fe$$

$$A_{1sFR} = + \sec Ee + K \sec Fe$$

$$A_{1sFR} = + \sec Ee + K \sec Fe$$

$$A_{1sFR} = - \sec Ee + K \sec Fe$$

$$A_{1sRR} = - \sec Ee + K \sec Fe$$

$$A_{1sRR} = K$$

$$A_{1sRR} = K + K \sec Fe$$

$$A_{1sRR} = K$$

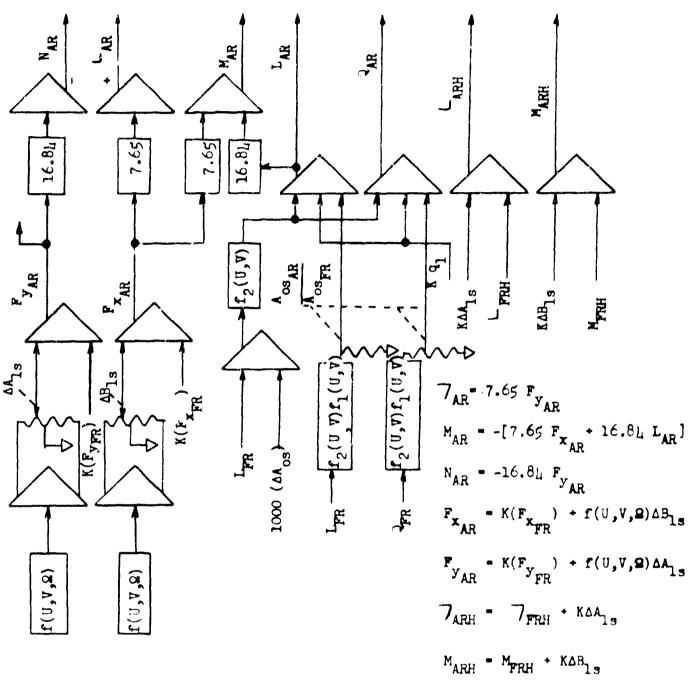
$$A_{1sRR} = K + K \sec Fe$$

$$A_{1sRR} = K$$

$$A_{1sRR} = K + K \sec Fe$$

$$A_{1s$$

Figure 26. Swash Plate Angles & S.A.S. for Tandem Rotor Helicopter



$$Q_{AR} = [f(U,V) \frac{A_{os}}{A_{os}} \frac{AR}{FR}] f_1(U,V) + [L_{FR} + 1000 (\Delta A_{os})] f_2(U,V) + Kq_1$$

$$L_{AR} = [f(U,V)\frac{A_{OS}AR}{A_{OS}FR} L_{FR}]f_{1}(U,V) + [L_{FR} + 1000 (\Delta A_{OS})]f_{2}(U,V) + Kq_{1}$$

Figure 27. Aft Hotor Terms, Tandem Rotor Helicopter AC Mechanization

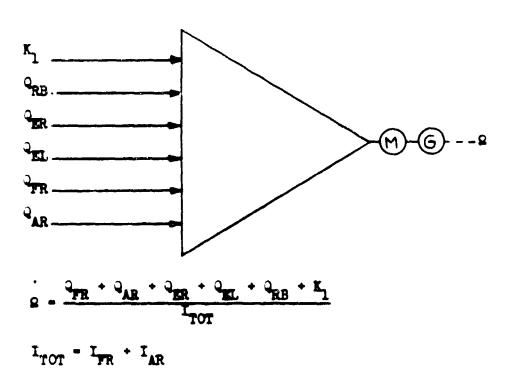


Figure 28. Tandem Rotor Angular Velocities AC Mechanization

		\C		DC
Component	No.	Wt.	No.	Wt.
Amplifier	25	25	31	62
Servo	5	35	5	35
Pots	16	4	16	<u>L</u>
Function (f) Generation	9		9	**
Complexity		64		101

Table 21. Additional Components Tandem Rotor Helicopter

This completes the mechanization of the tandem rotor helicopter.

Summary Tandem Rotor Helicopter. The tandem rotor mechanisation has been developed in terms of the single rotor mechanisation (Section III.B.). The arguments presented in the single rotor summary (Section III.B.) are equally valid for the tandem rotor helicopter. Table 22 is a summary of tandem rotor component complexity. This table is constructed by taking the component totals of the single rotor helicopter (Table 19) and then subtracting out components due to the mechanisation of the tail rotor in the single rotor helicopter (Table 7) and then adding the additional components due to tandem rotor mechanisation (Table 21). The AC system for the tandem rotor helicopter has a complexity of 744-3/4 versus 1105-1/2 for the DC system. This is practically the same as the complexity for the single rotor helicopter AC system-751-3/4, DC system-1106-1/2. Consequently, using the same rationals as in Section III.B., the AC system is favored for the tandem rotor helicopter.

## C. V/STOL MECHANIZATION

Mechanization for the tilt wing aircraft, the XC-ll/2A, of Ling-Temco-Vought, Hiller, Ryan is considered in this portion of the report. In reference 2 the equations of motion for the tilt-wing were developed and the necessary equations for mechanisation of the tilt-wing are reproduced in Section VI. It should be noted that equations of motion were developed for four other V/STOL configurations in reference 2: the tilt-duct represented by the DOAK VZ-LA, the tilt-propeller represented by the Curtiss Wright X-19, the fan-in-wing represented by the General Electric/Ryan XV-5A and the rotating thrust represented by the Hawker Aircraft P.1127. Mechanization of the tilt-duct and tiltpropeller equations of motion would be similar to the tilt-wing mechanisation. Mechanisation of the fan-in-wing and rotating thrust equations of motion would be similar to mechanizations of ordinary jet aircraft taking into account variations in the thrust components. By accounting for these thrust variations in the equations of motion, existing mechanisations for jet aircraft such as those presented in reference 3 are valid for the fan-in-wing and rotating thrust. The mechanisation for the tilt-

	4	ANET IF IER	FIER			SERVO	٥			POT	K		S	S-c Por	<b>E</b>		<b>8 8</b>	RECOLVER	<b>85</b>	TOTAL	At.
		AC	ည		AC		22		AC		20		YC		20		<b>₽</b> C		2	<b>P</b> C	26
	ON	5	NO NO	5	NO	5	NO	5	NO WT		NO	W	NO	4	NO WE	MO	¥.	NO	5	150	5
Single Rotor Welicopter (Table 18)	191	191	194 194 275550		75	75 525 75 525 DOL	75 5	8	70	56	26 10%	26	8	8 13 °	22 5 <del>2</del>	. 10		8		752	751 <mark>2</mark> 1106 <mark>7</mark>
Minus Tail Rotor Contributions-19 -19 -25 -50	-19	-19	-25-	.50	~	61-	- 2-	8-61-		-5	80	2			-17	۲-	-2 -1			η-	-102
Plus Additions From Table 21	56	92	31	62	5	35	2	35	19	77	19	-3								\$	DI.
Tandem Rotor Complexity		201		562		ह	रांगाग	115		28		28		rt.						7117	744 1105

Table 22. Tandem Rotor Summary

wing may not be optimum since the mechanization reflects the equations of motion which could change as data from the manufacturer become available about the particular aircraft. Mechanization of the tilt-wing presented here is based upon the best information available at the time of this report.

References are made to the appropriate tilt-wing equations in Section VI in some of the mechanizations drawings where the equations are lengthy. On other drawings the equations are written explicitly.

1. SIMILARITY OF V/STOL EQUATIONS. Before developing the tilt-wing mechanization in detail consider the similarity of the tilt-duct and tilt-prop equations to the tilt-wing equations and the likeness of the fan-in-wing and rotating thrust equations to existing equations of motion for jet aircraft. In these comparisons which follow only the X-force equations will be compared, the Y-force and Z-force equations contain like similarities.

First consider the tilt-wing, tilt-duct and tilt-prop. X-force equations from Reference 2.

X-Force Equation: Tilt-Wing (XC-142A)

$$m(\mathring{U} + W_{q_{1}} - Vr) + mg \sin \theta$$

$$= (C_{x})_{w} Sq_{w} f(C_{T,S}) + \sum_{n=1}^{U} (T_{n} \cos i_{w} - N_{n} \cos \beta_{n} \sin i_{w})$$

$$(3-1)$$

$$-\left[C_{D_{t}}\cos\left(i_{t}-\alpha_{t}\right)+C_{L_{t}}\sin\left(i_{t}-\alpha_{t}\right)\right]Sq\left(\frac{q_{hs}}{q}\right)-SqC_{D_{0}}$$

X-Force Equation: Tilt-Duct (∇7-4A)

$$m(\dot{U} + Wq - Vr) + mg \sin \theta$$
 (3-2)

= 
$$(C_x)_w Sq_w + q_E S_v (C_x)_{RC} + K_2 \sum_{j=1}^{2} (C_{T_j} \cos i_D - C_{N_j} \sin i_D) + T_r$$

- 
$$[C_{D_t} \cos (i_t - \alpha_t) - C_{L_t} \sin (i_t - \alpha_t)] Sq(\frac{q_{ns}}{q})$$
-  $Sq C_{D_q}$ 

X-Force Equation: Tilt-Prop (X-19)

$$m(\dot{v} + W_{q_1} - Vr) + mg \sin \theta$$
 (3-3)

= 
$$(C_{x})_{wf} SQ_{wf} + \sum_{n=1}^{u} (T_{n} \cos i_{p} - N_{n} \cos \beta_{n} \sin i_{p}) + (C_{x})_{wa} SQ_{wa} - SQC_{D_{0}}$$

Comparing equations (3-2) and (3-3) to (3-1) the only differences are the terms  $q_{\overline{B}}S_{\overline{V}}$  ( $C_{\overline{X}})_{RC}$  +  $K_{\overline{Z}}$   $\sum_{j=1}^{\infty}$  ( $\overline{C}_{T_{j}}$  cos  $i_{\overline{D}}$  -  $C_{N_{j}}$  sin  $i_{\overline{D}}$ ) +  $T_{\underline{T}}$  in (3-2) and

 $(C_x)_{wa} Sq_{wa}$  in (3-3).  $c_x S_v (C_x)_{RC}$  and  $T_r$  are due to the reaction controls in the tilt duct aircraft. The term  $K_2 = \sum_{j=1}^{2} (\tilde{C}_{T_j} \cos i_D - \tilde{C}_{N_j} \sin i_D)$  is thrust expression for the duct fans in coefficient form.

To further illustrate the similarities of the force equations (3-1, 3-2, and 3-3) suppose that the incident angles  $(i_y, i_p \text{ and } i_p)$  are zero. Then there results:

$$m(\ddot{U} + Wq_{1} - Vr) + mg \sin \theta \qquad (3-1a)$$

$$= (C_{x})_{w} Sq_{w} + \sum_{n=1}^{l_{1}} T_{n} - [C_{D_{x}} \cos(i_{x} - \alpha_{x}) + C_{L_{x}} \sin(i_{x} - \alpha_{x})] Sq(\frac{q_{h8}}{q}) - Sq C_{D_{c}}$$

$$m(\ddot{U} + Wq_{1} - Vr) + mg \sin \theta \qquad (3-2a)$$

$$= (C_{x})_{w} Sq_{w} + q_{E}S_{v}(C_{x})_{RC} + K_{2} \sum_{j=1}^{2} \bar{C}_{T_{j}} + T_{r}$$

$$- [C_{D_{x}} \cos(i_{x} - \alpha_{x}) + C_{L_{x}} \sin(i_{x} - \alpha_{x})] Sq(\frac{q_{h8}}{q}) - Sq C_{D_{c}}$$

$$m(\ddot{U} + Wq_{1} - Vr) + mg \sin \theta \qquad (3-3a)$$

$$= (C_{x})_{wf} Sq_{wf} + \sum_{j=1}^{l_{1}} T_{n} + (C_{x})_{wa} Sq_{wa} - Sq C_{D_{c}}$$

Equations (3-la), (3-2a) and (3-3a) are very similar. Mechanisation of the tilt-wing equation (3-l) will therefore demonstrate the simulation technique. The Y and Z force equations for the tilt-wing, tilt-duct and tilt-prop have the same degree of likeness as the X-force equations.

Next, let us compare the fan-in-wing and rotating thrust I-force equations from Reference 2 to simulation equations used for jet aircraft.

Fan-In-Wing: I-Force Equation

$$m(\mathring{v} + Wq_1 - Vr) = qS[C_X(\alpha, Ma) + C_X(\beta) + C_{XSF} \cdot \delta F]$$

$$+ T_j \cos \alpha_T + T_F \sin \theta_L - mg \sin \theta$$
(3-4)

Rotating Thrust: X-Force Equation

$$m(\dot{U} + Wq_1 - Vr) = qS[C_{x_U} + C_{x_G} + C_{x_{\delta F}} \cdot \delta F + C_{x}(\beta)]$$

$$+ T \cos(\theta_j + \alpha_T) - mg \sin \theta$$
(3.5)

Ordinary Simulation: X-Force Equation

$$m(\mathring{U} + Wq_1 - Vr) = qS[C_{\chi}(\alpha, Ma) + C_{\chi}(\beta) + C_{\chi}(\beta) + C_{\chi}(\beta) + C_{\chi}(\beta)] + T \cos \alpha_{\eta} - mg \sin \theta$$
(3.6)

The only difference among equations (3.4), (3.5) and (3.6) is in the thrust terms. Using equation (3.6) as a guide consider (3.4) and (3.5). Equation (3.5) has as a thrust term  $T \cos (\theta_j + \alpha_T)$ .  $\theta_j$  is the rotation of thrust producers. If the aircraft is in normal flight ( $\theta = 0$ ) and  $T \cos (\theta_j + \alpha_T) = T \cos \alpha_T$  which is the same as equation (3.6).

The thrust term in equation (3.4) is  $T_j \cos \alpha_T + T_F \sin \theta_L$ . If the fan-in-wing is in normal flight  $\theta_L = 0$  and consequently equation (3.4) is the same as equation (3.6). The only added term is  $T_F \sin \theta_L$  in equation (3.4) and is of small consequence, though necessary, from the mechanisation viewpoint.

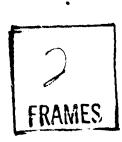
Similar arguments can be applied for the Y-force, Z-force and moment equations.

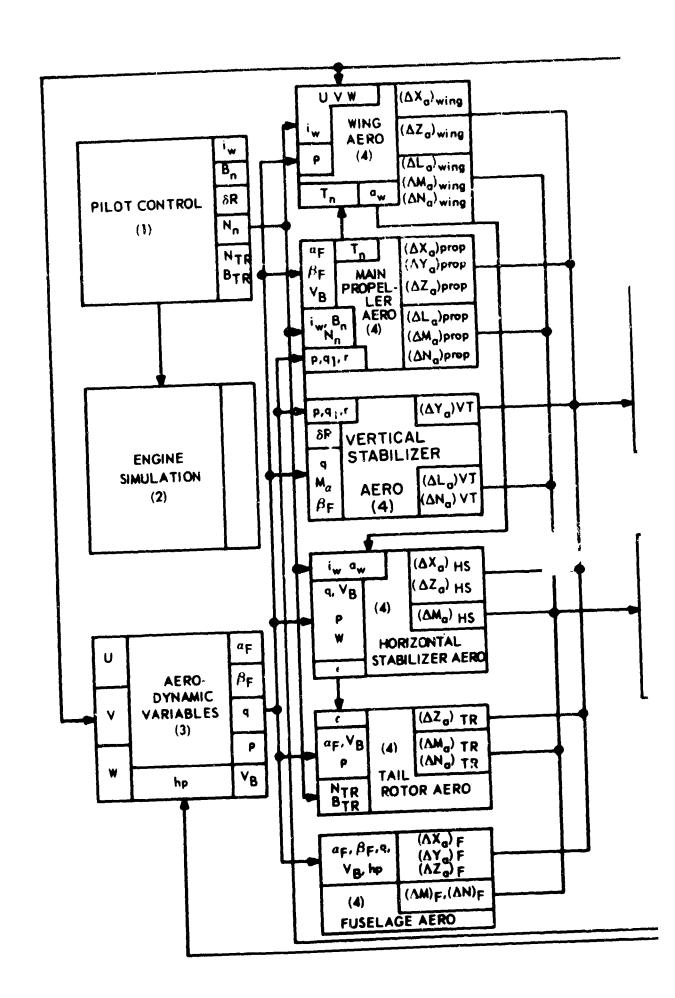
2. TILT-WING MECHANIZATION. Figure 29 is a block diagram for the tilt-wing aircraft similar to Figure 1. Each mechanization drawing refers to the appropriate equations in Section VI. As per the helicopter mechanization, each block in Figure 29 will be considered. A component count will be done in the summary indicating differences in AC and DC mechanization.

Hlock (1) Pilot Control. Block (1) of Figure 29 contains outputs due to control of the pilot.

<u>Mlock (2) Engine Simulation</u>. Block (2) of Figure 29 is not simulated.

<u>Block (3) Aero Variables.</u> The AC mechanisation of Block (3), Figure 29 is shown in Figure 30 in order to give outputs  $\alpha_{F}$ ,  $\beta_{F}$ ,  $\gamma_{P}$  and  $V_{B}$ . This mechanization is similar to that shown in Figure 10 for the single rotor helicopter.





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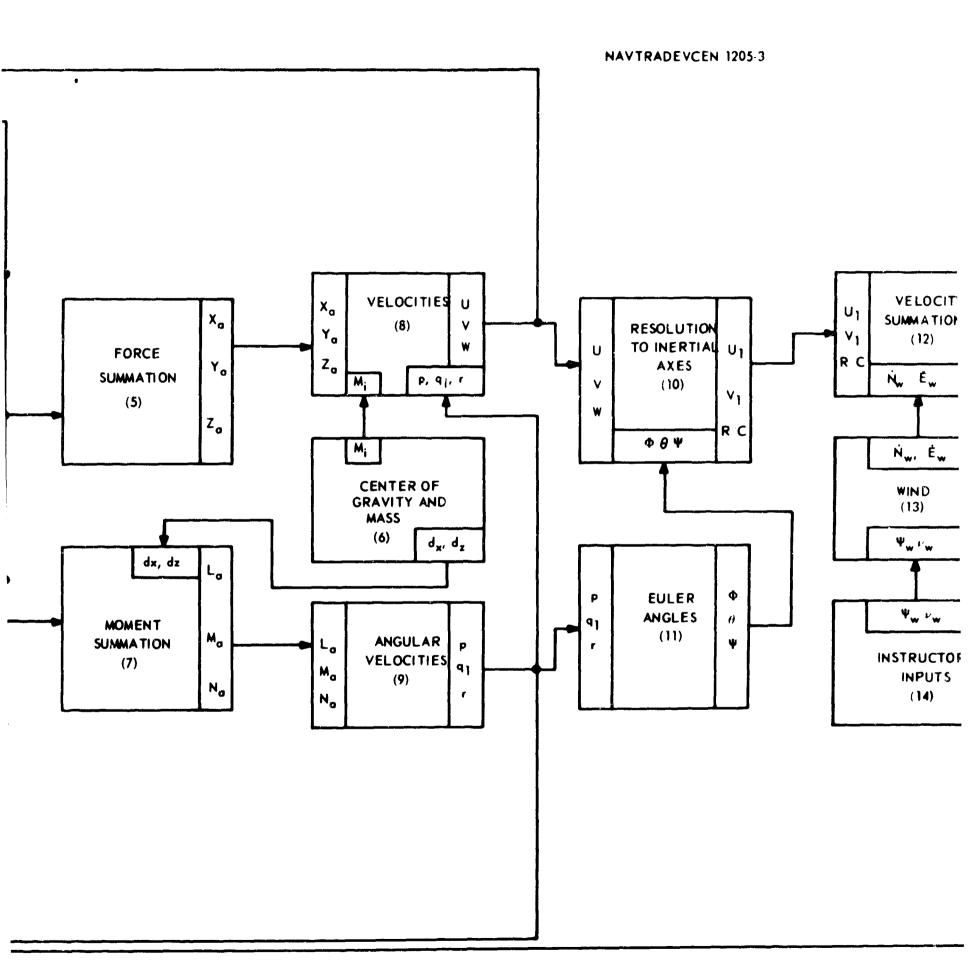
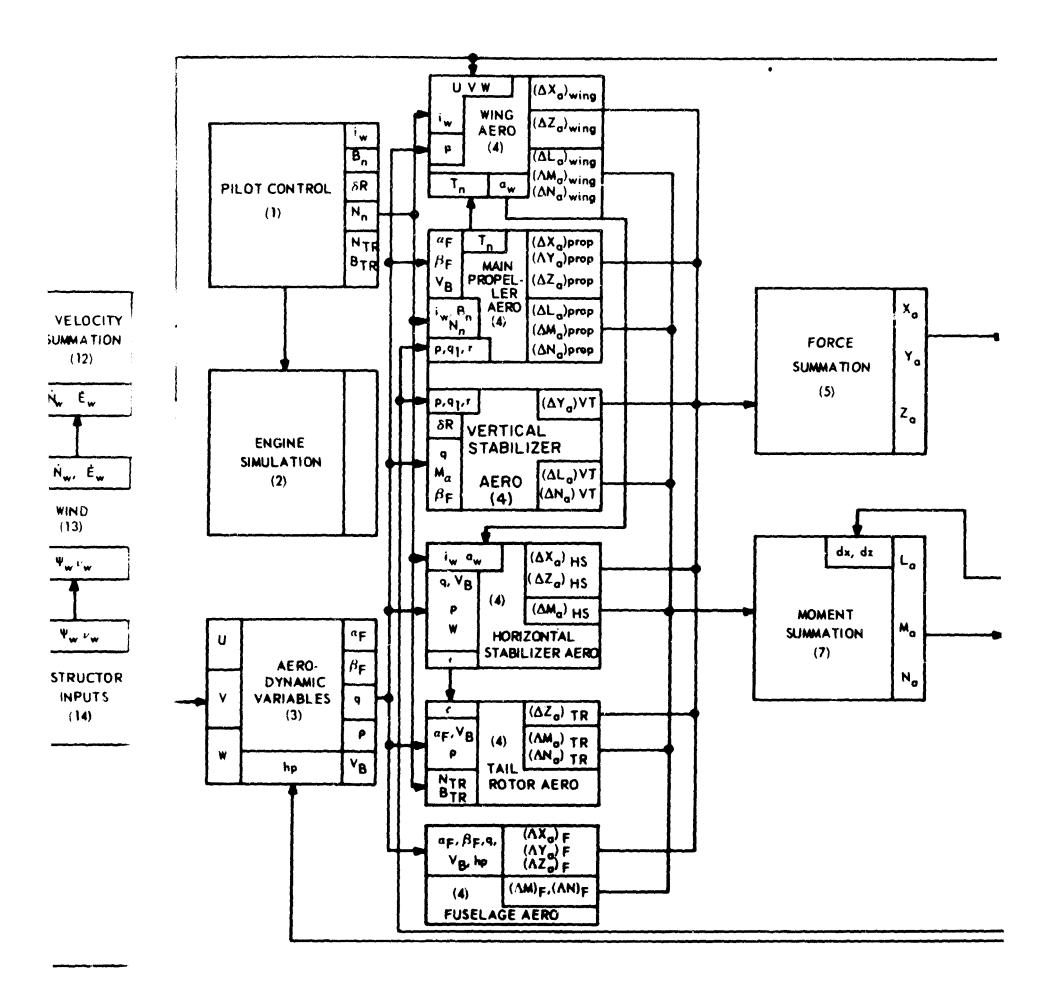


Figure 29. Simplified Block Diagram V STOL (Tilt-Wing) Aircraft



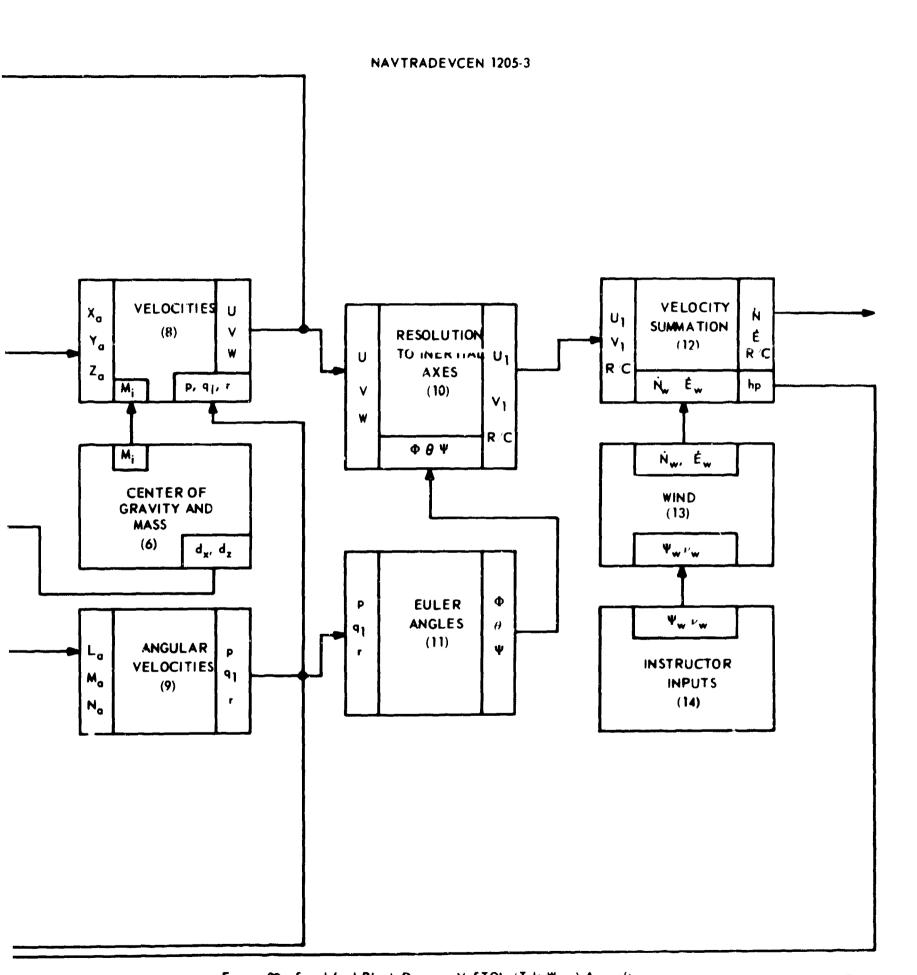


Figure 29. Simplified Block Diagram V STOL (Tilt-Wing) Aircraft

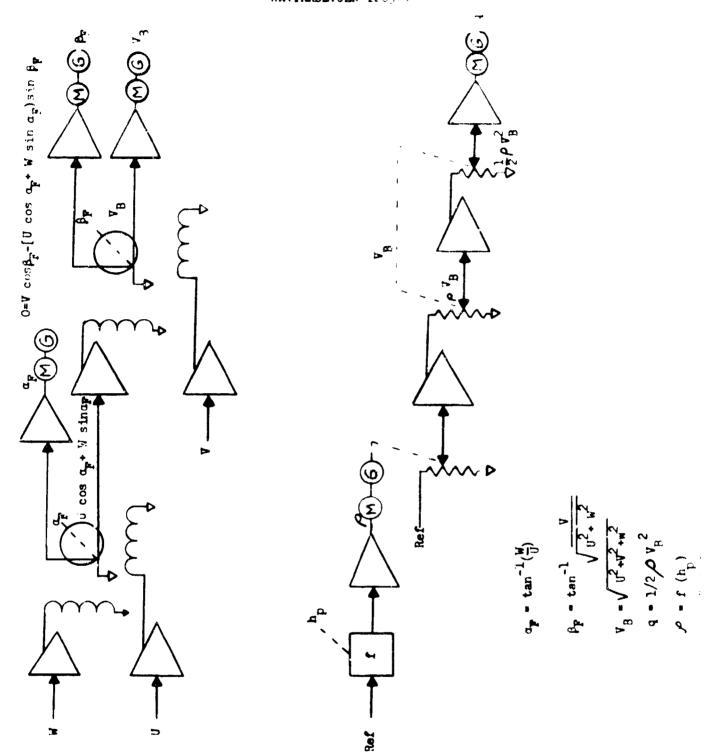
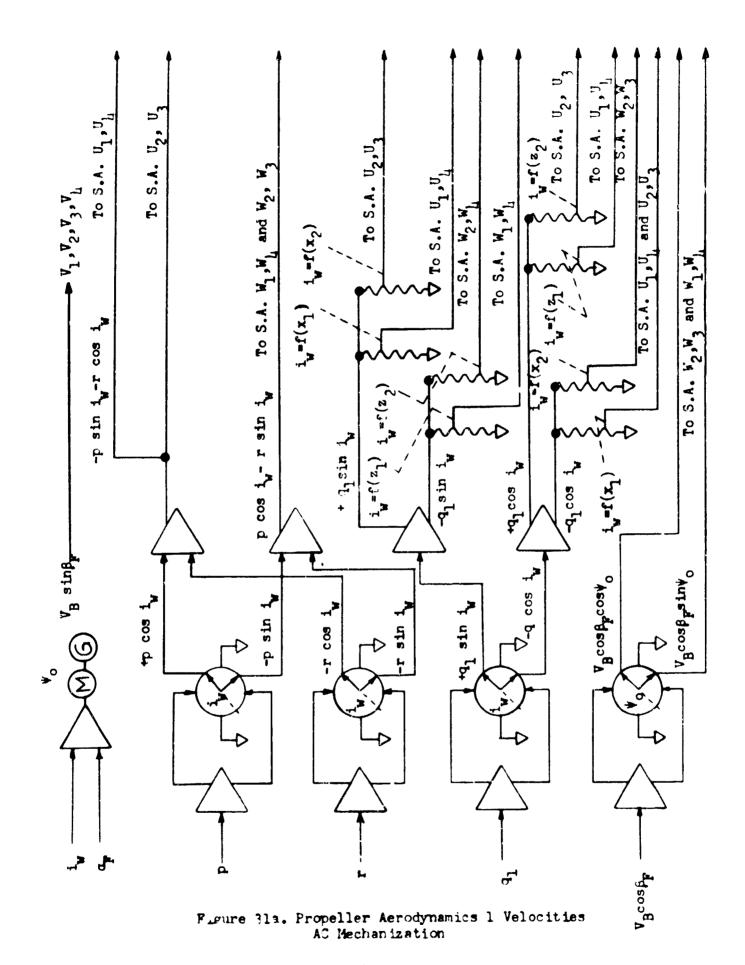


Figure 30. Aerodynamic Variables AC Mechanisation

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Block (1) Aero Terms. The AC mechanization of Block (1), Figure 29 is divided into the following six parts:

- 1. Main Propeller Aerodynamics. Figures 31 through h1 mechanize the equations having to do with propeller aerodynamics. Figure 31 develops velocities associated with each propeller. Figure 32 develops the advance ratio associated with each propeller. Figures 33 and 3 $\mu$  show coefficients used in propeller aerodynamics developed as functions of advance ratio and propeller blade pitch. Figure 35 is the mechanization of each propeller thrust ( $T_n$ ) and torque ( $T_n$ ). Figure 36 is the mechanization of the normal component of thrust ( $T_n$ ) and propeller moments ( $T_n$  and  $T_n$ ). Figure 37 resolves  $T_n$  and  $T_n$  into appropriate components due to wing tilt ( $T_n$ ) and orientation of  $T_n$  by the angle  $T_n$ . Figure 38 is the mechanization of the force components ( $T_n$ ), (
- 3. Vertical Stabilizer Aerodynamics. Figure 1,6 shows the AC mechanization of equations 6.222 to 6.227 for the force and moment contributions due to the vertical stabilizer.
- 4. Horizontal Stabilizer Aerodynamics. Figure 47 shows the AC mechanization of equations 6.228 to 6.233 for the force and moment contributions due to the horizontal stabilizer.
- 5. Tail Rotor Asrodynamics. Figure 48 shows the AC mechanization of equations 6.234 to 6.246 for the force and moment contributions due to the tail rotor.
- 6. Fuselage Aerodynamics. Figure 49 shows the AC mechanization of equations 6.247 to 6.251 for the force and moment contributions due to the effects of the fuselage.
- Blocks (5) through (14). These blocks of Figure 29 are similar to the same numbered blocks for the single and tandem rotor helicopter.
  - Block (5), Figure 29 mechanized by Figure 50.
  - Block (6), Figure 29 mechanized as in Section III.A.



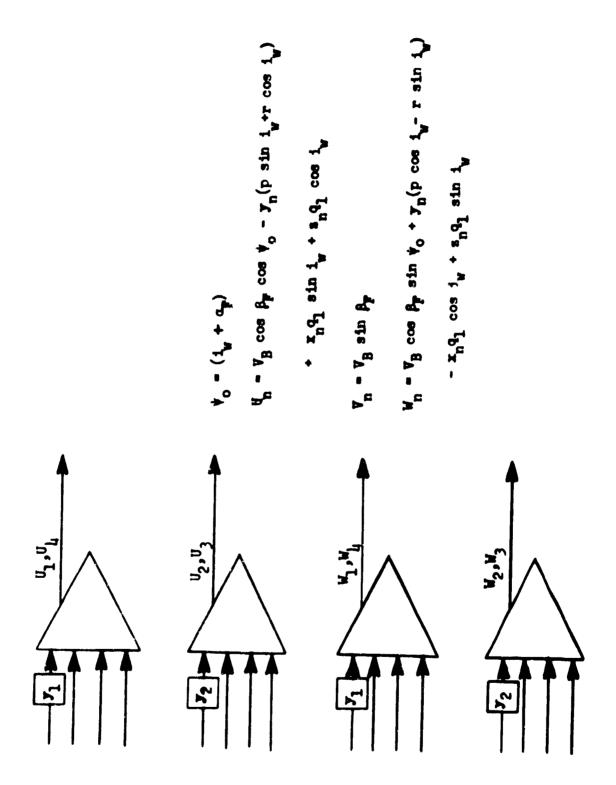


Figure 31b. Propeller Aerodynamics Velocities AC Mechanization

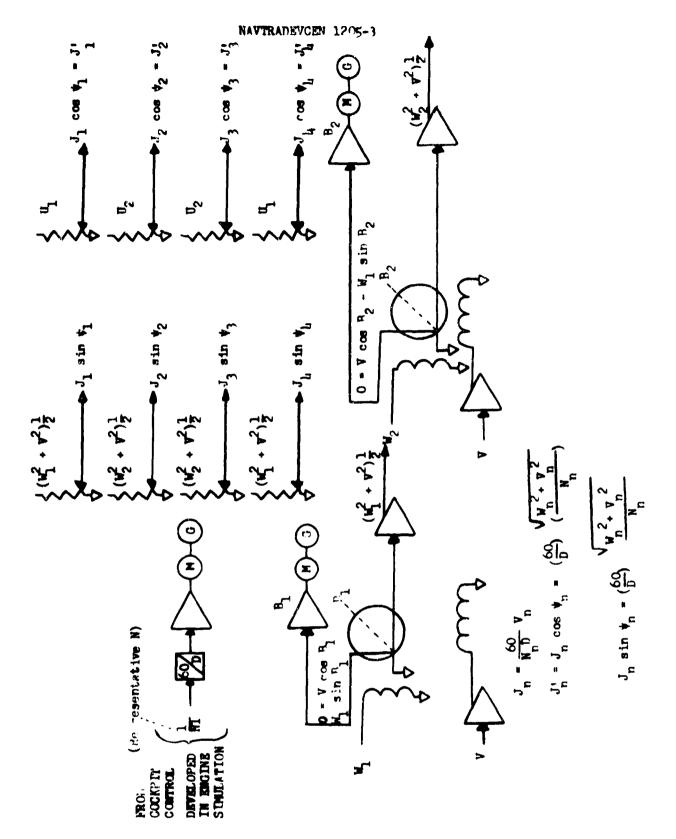


Figure 32. Propeller Aerodynamics Advance Ratio AC Mechanisation

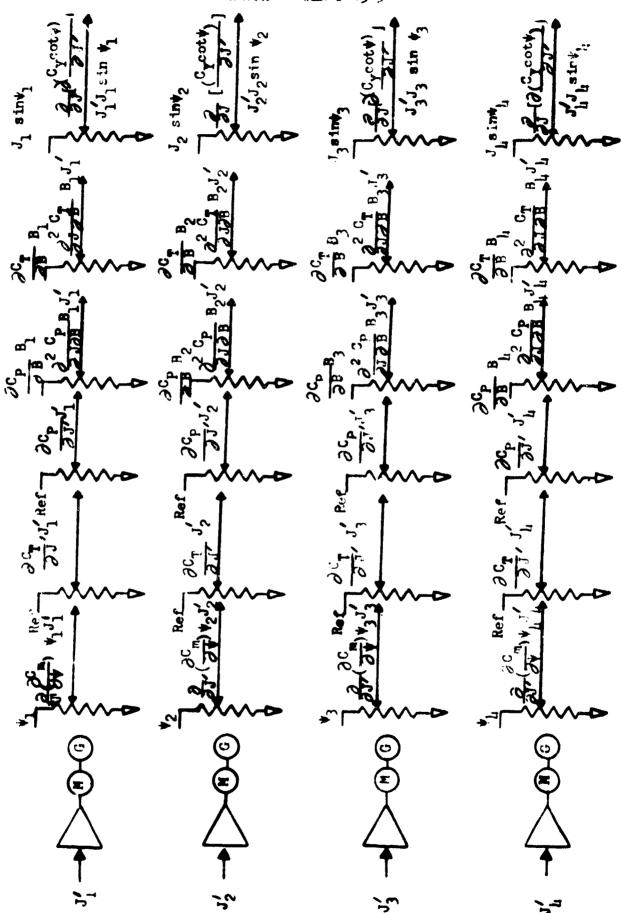


Figure 33. Propeller Aerodynamics Coefficients

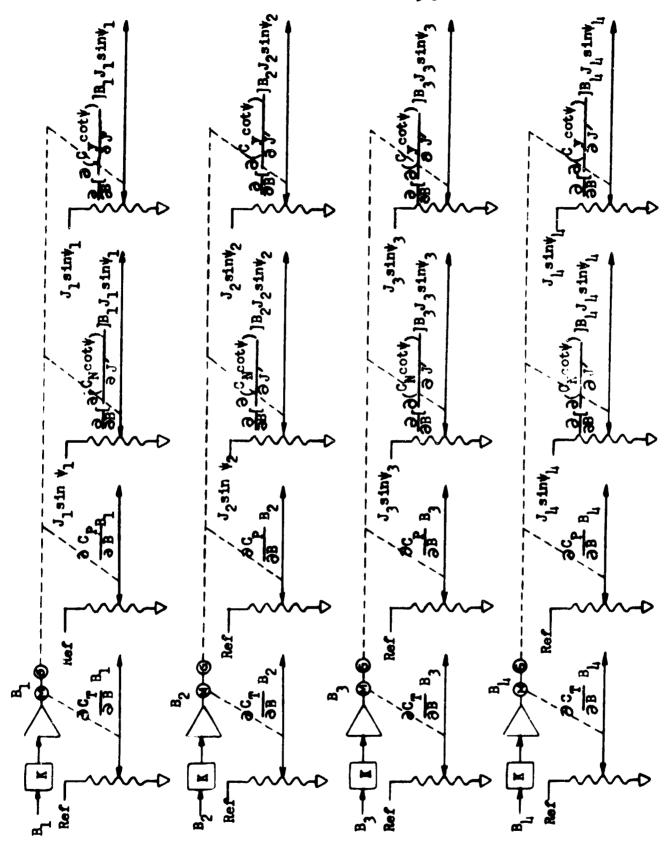


Figure 3h. Propeller Aerodynamics Coefficients AC Mechanization

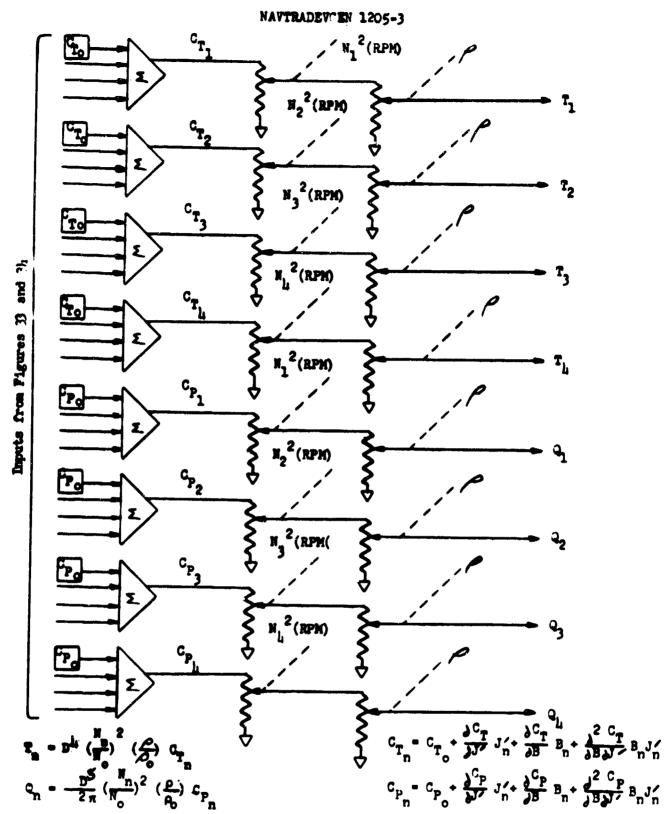


Figure 35. Propeller Aerodynamics  $T_n$  and  $Q_n$  AC Mechanisation

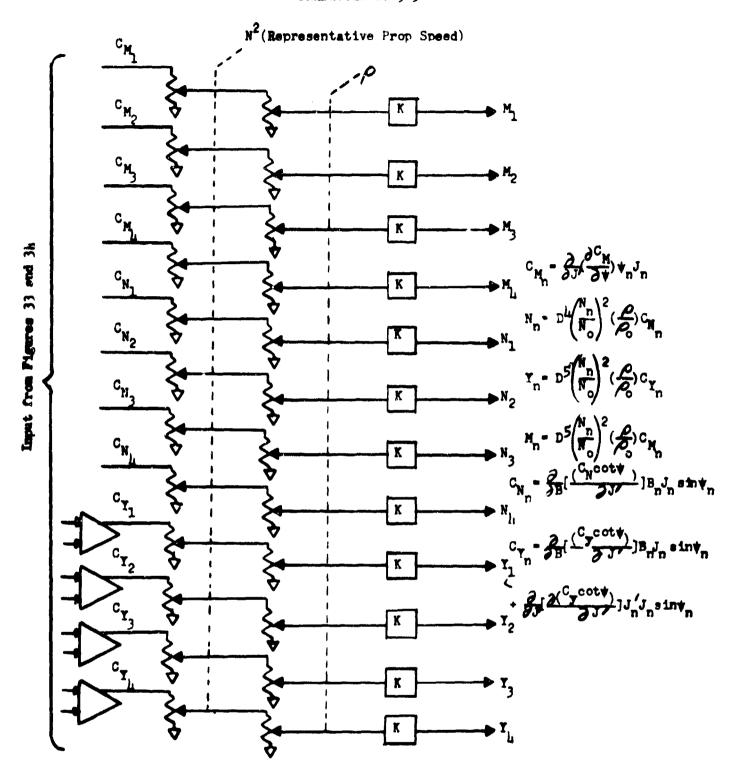
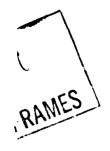
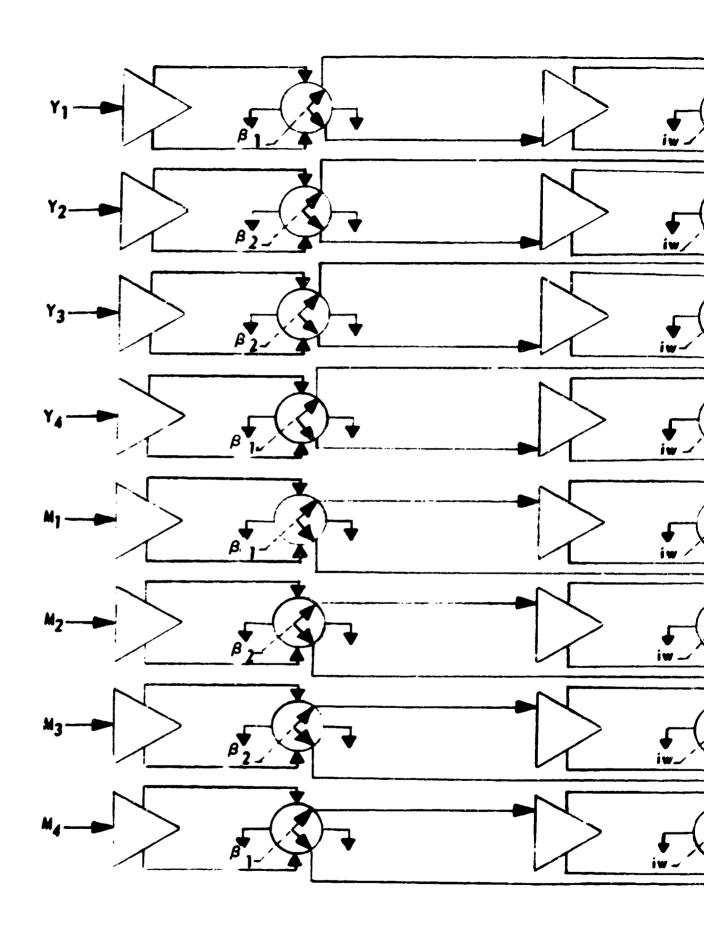


Figure 36. Propeller Aerodynamics  $M_n$ ,  $N_n$  and  $I_n$ 





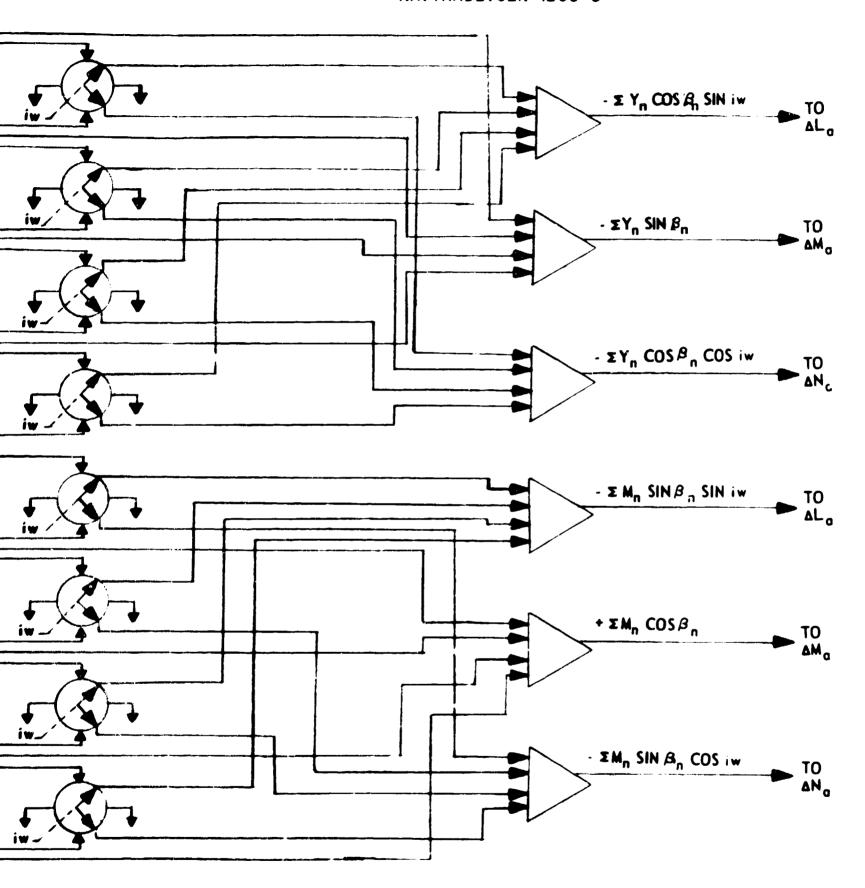


Figure 37. Propeller Aerodynamics Y and M Components AC Mechanization

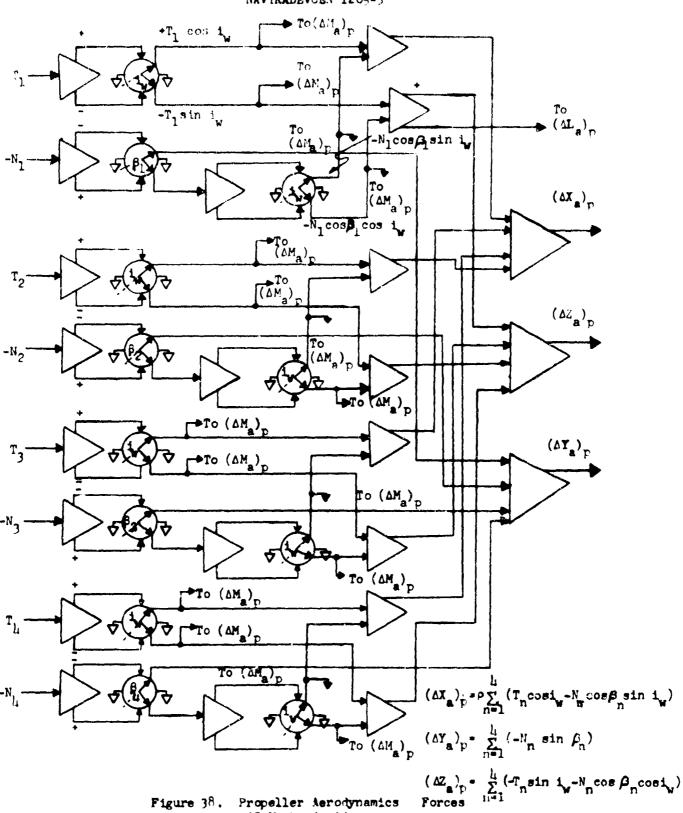


Figure 38. Propeller Aerodynamics AC Mechanization

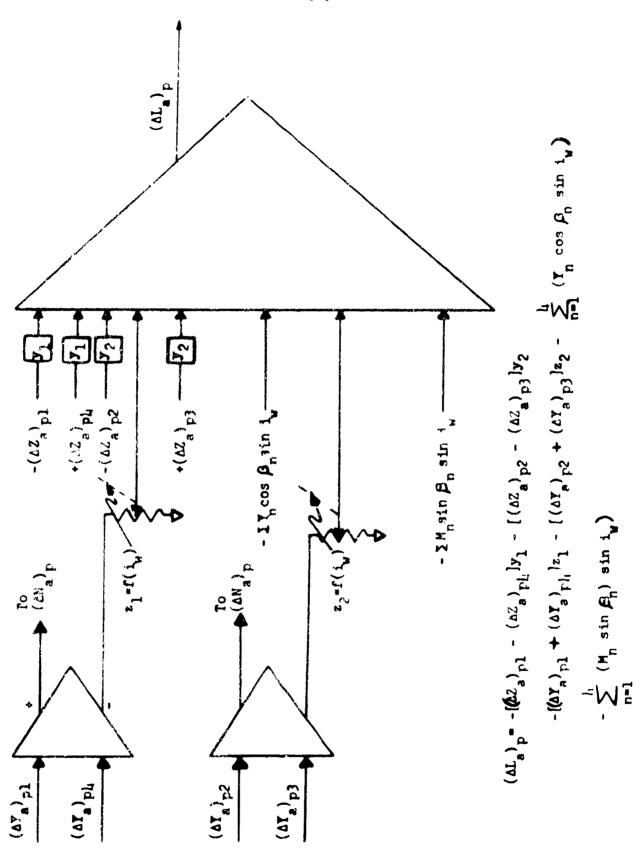


Figure 39. Propeller Aerodynamic Moment -(AL)

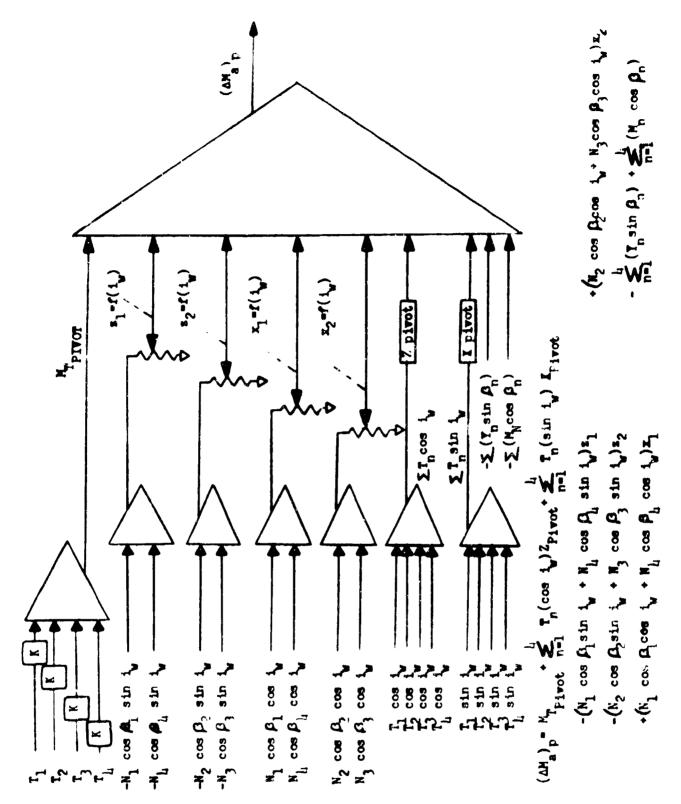
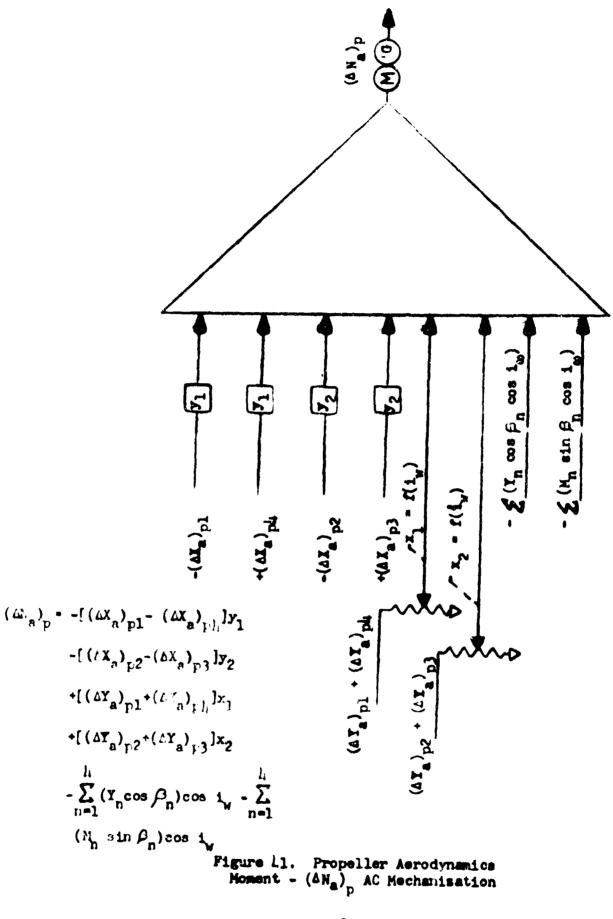
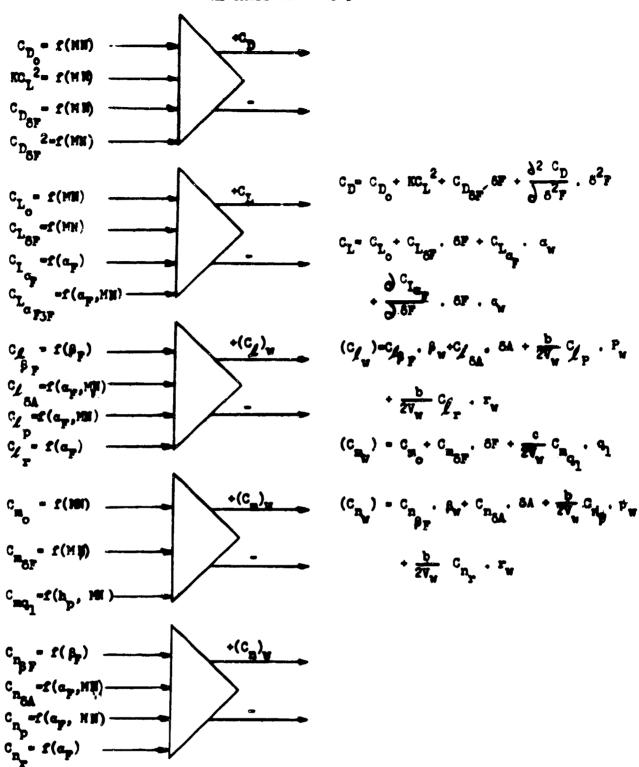


Figure 1.0. Propeller Aerodynamics
Moment - (ΔM<sub>p</sub>)<sub>p</sub> AC Mechanisation



Pigure h2. Wing Aerodynamics  $\alpha_{_{\mathbf{W}}}$ ,  $\beta_{_{\mathbf{W}}}$ ,  $\nabla_{_{\mathbf{W}}}$ 



Pigure 13. Wing Aerodynamics Coefficients
AC Machanisation

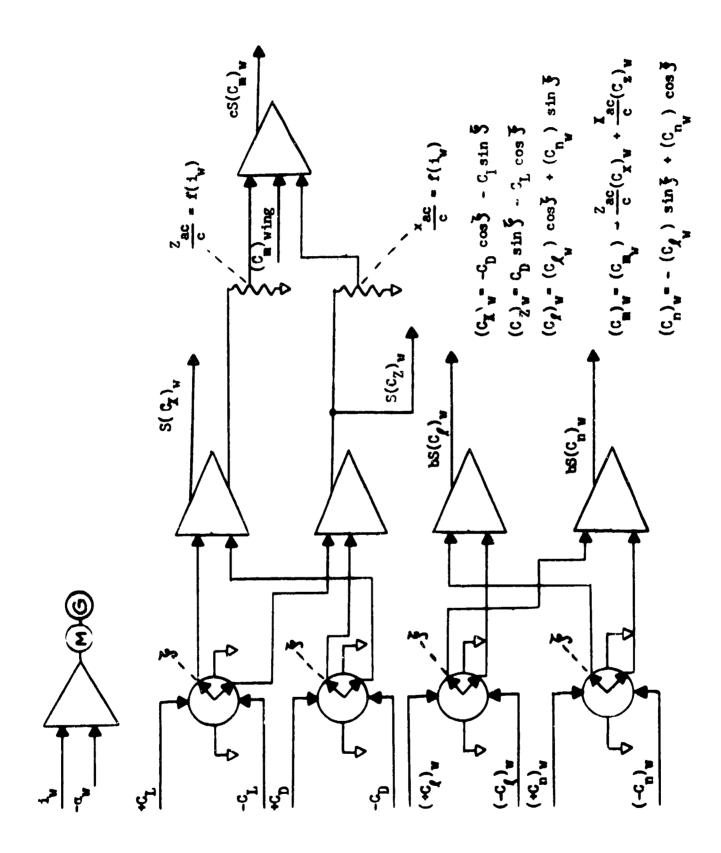


Figure 1:1. Wing Aerodynamics Coefficients AC Mechanisation

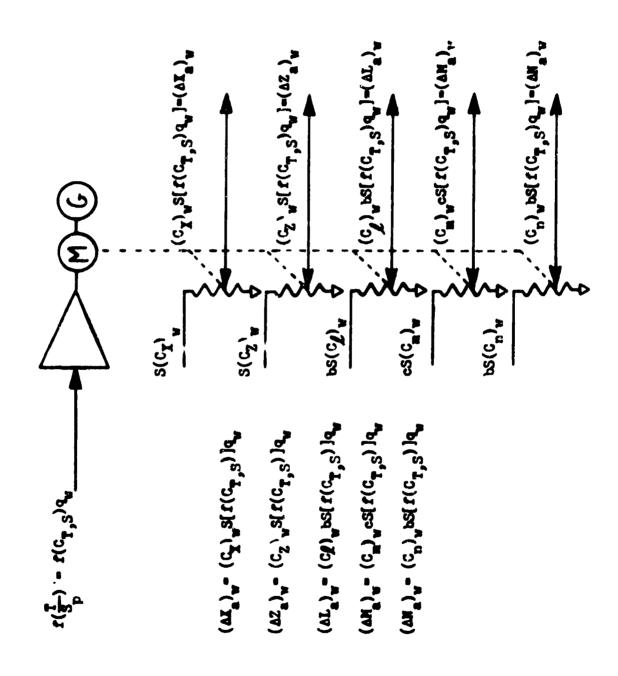


Figure 45. Ving Aerodynamics Forces and Homente AC Hechanisation

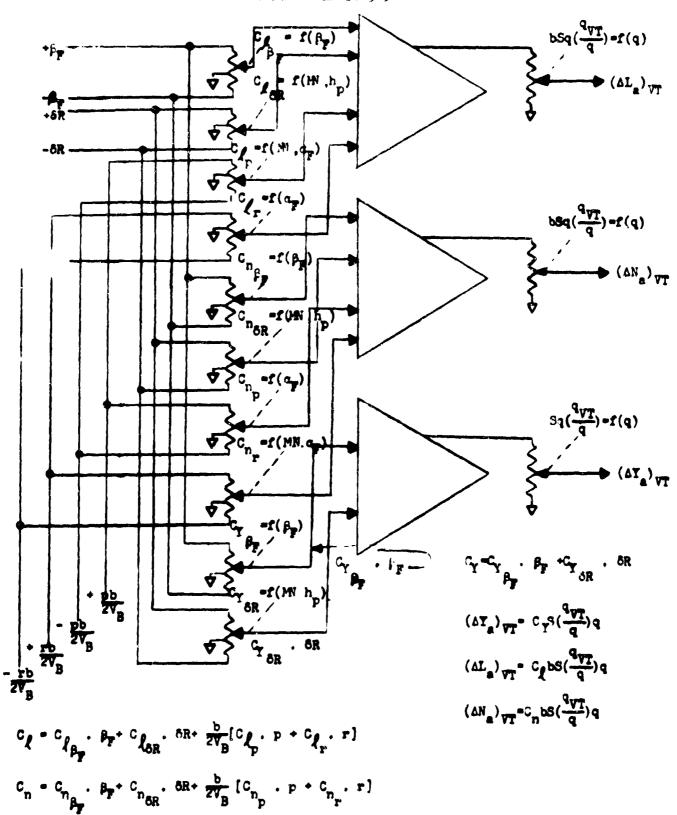
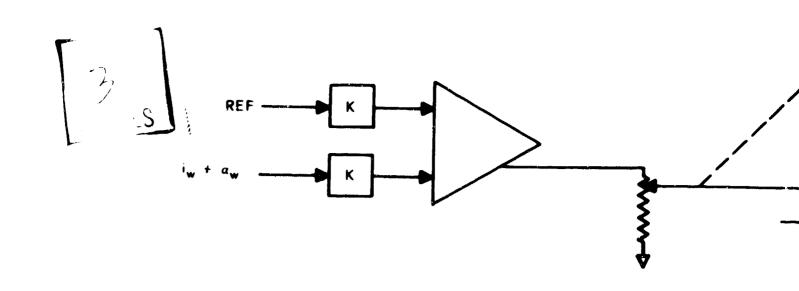
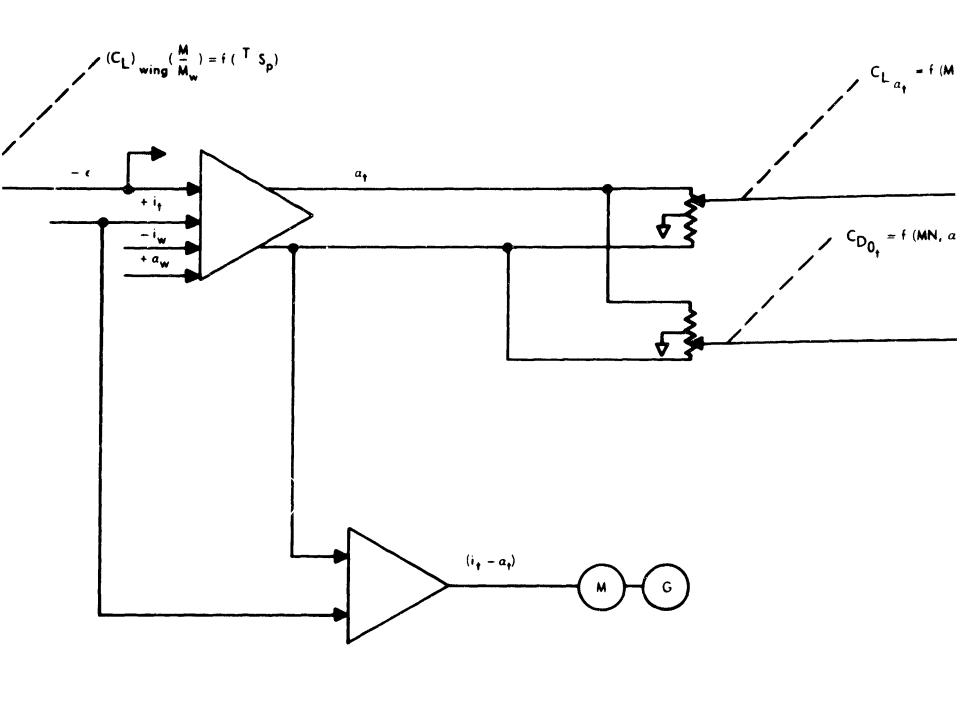
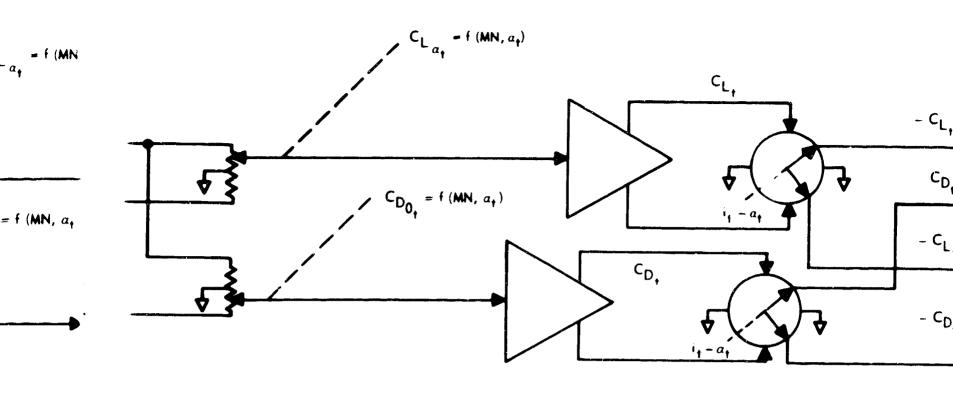


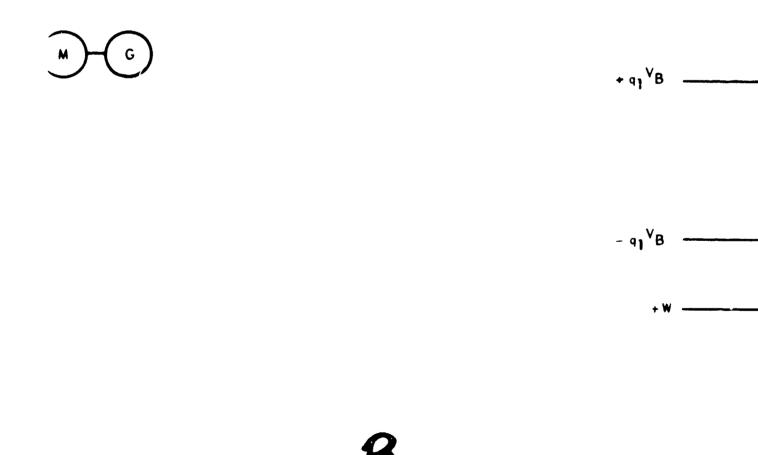
Figure 16 Vertical Stabiliser Aerodynamics Force and Momente AC Mechanisation











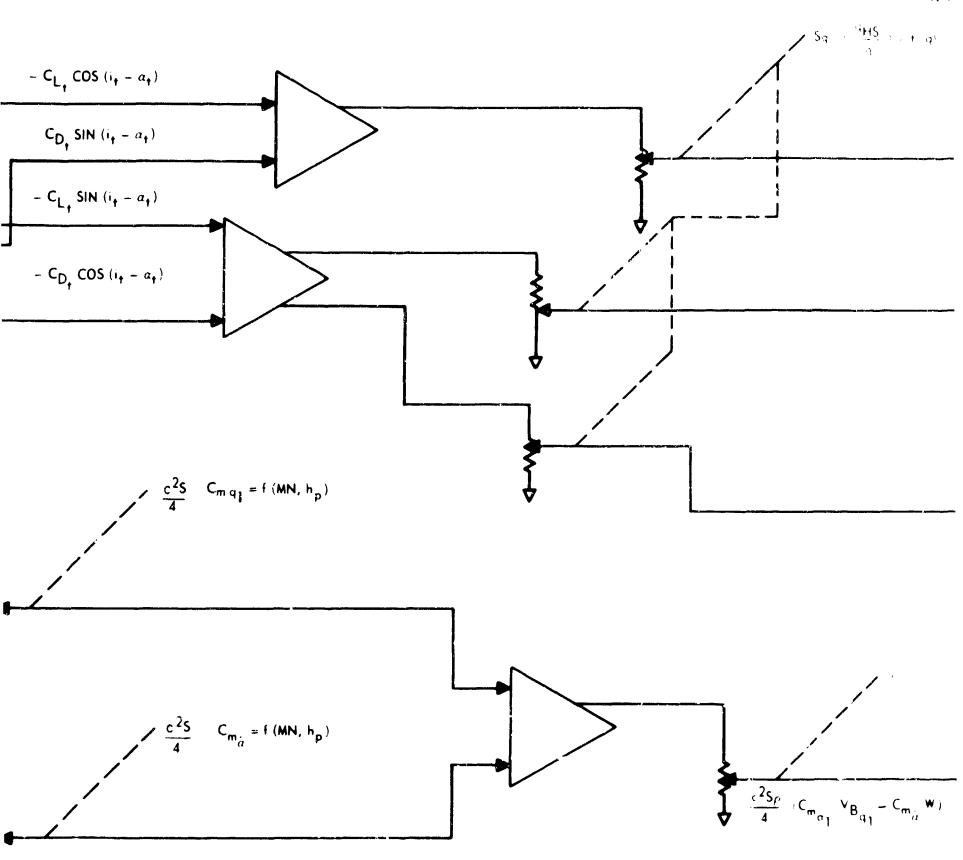
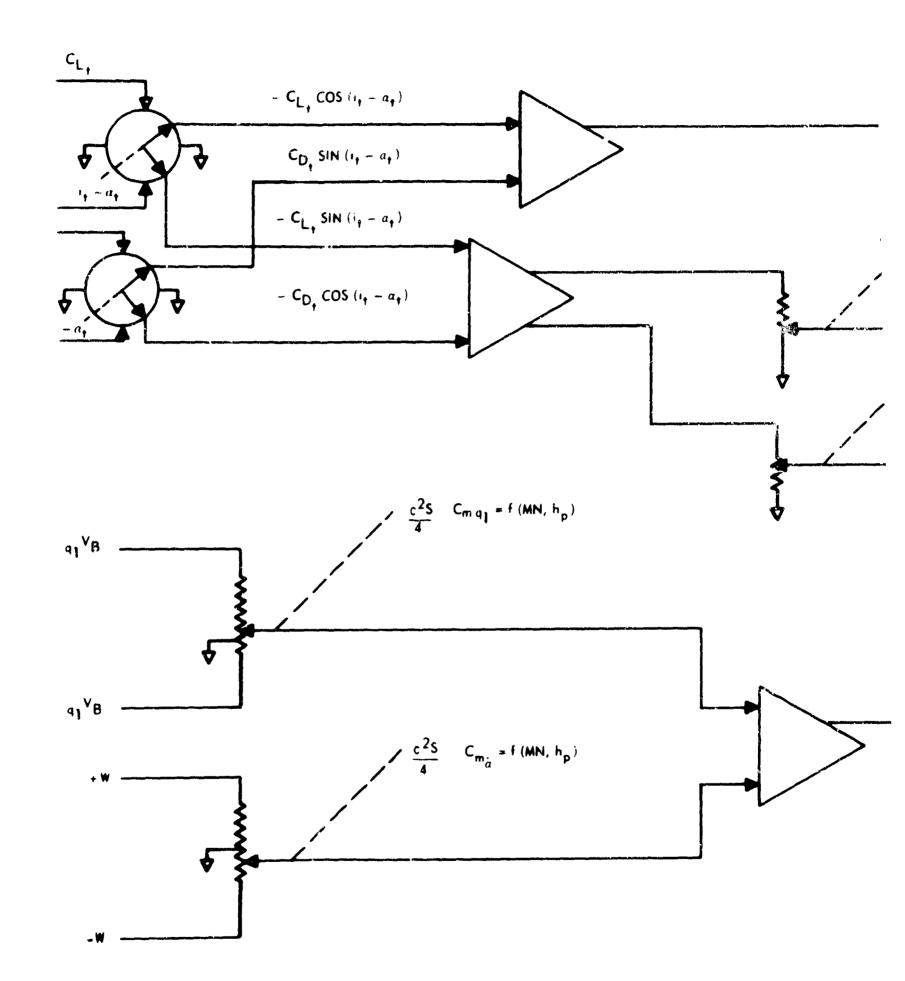


Figure 47 FORC



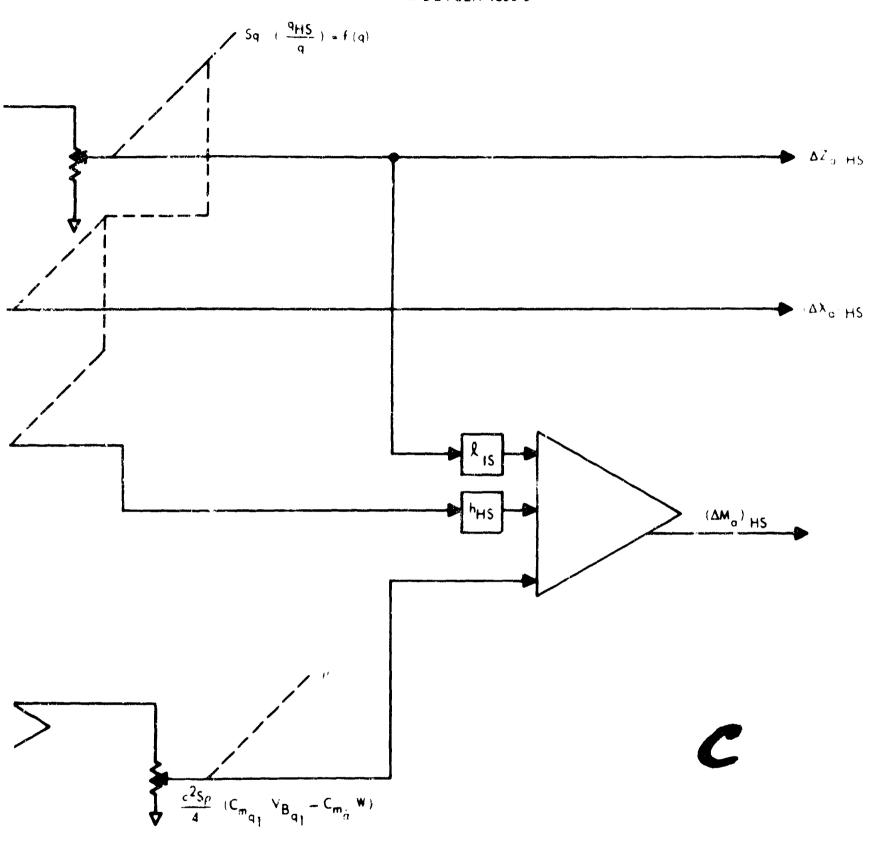


Figure 47. HORIZONTAL STABILIZER AERODYNAMICS FORCES AND MOMENT AC MECHANIZATION

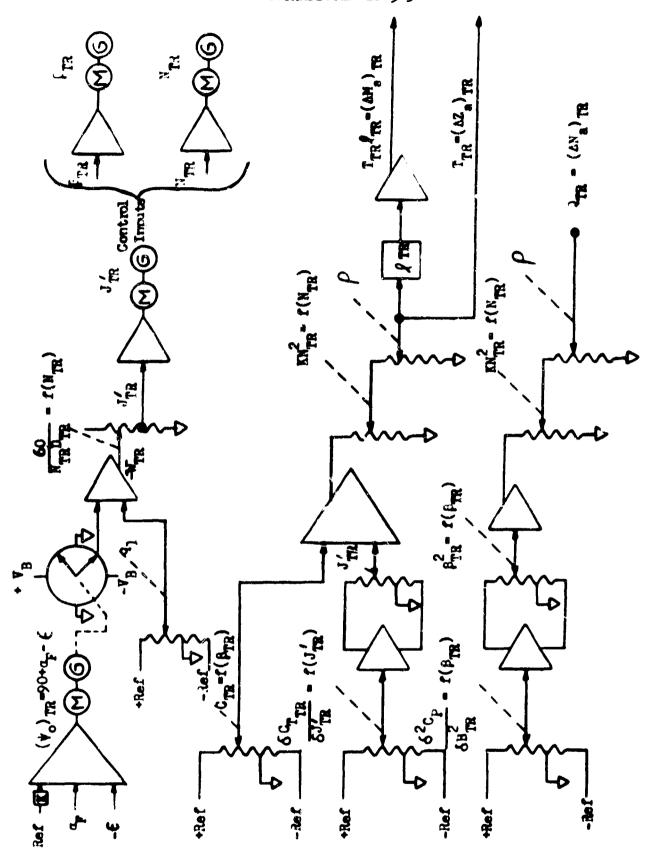


Figure 1.8. Tail Rotor Aerodynamics Force and Moments (Sheet 1) AC Mechanization

$$(\psi_{o})_{TR} = 90 + (\alpha_{F} - \epsilon)$$

$$W_{TR} = V_{B} \cos (\psi_{o})_{TR} - I_{TR} Q_{1}$$

$$J'_{TR} = (\frac{60}{D_{TR}}) \cdot (\frac{-W_{TR}}{N_{TR}})$$

$$C_{T}_{TR} = C_{T}_{TR} (B_{TR}) + \frac{J^{C}_{T}_{TR}}{J^{T}_{TR}} (J'_{TR})$$

$$(\Delta Z_{a})_{TR} = T_{TR}$$

$$C_{P}_{TR} = \frac{J^{a}_{C}_{P}}{J^{a}_{TR}} (B_{TR})^{2}$$

$$u_{TR} = V_{B} \sin (\psi_{o})_{TR}$$

$$J_{TR} = (\frac{60}{D_{TR}}) \cdot \frac{V_{TR}}{N_{TR}}$$

$$V_{TR} = (u_{TR}^{2} + w_{TR}^{2})^{2}$$

$$(\Delta N_{a})_{TR} = C_{TR} \cdot (\Delta M_{a})_{TR} - T_{TR} \cdot I_{TR}$$

$$T_{TR} = D_{TR}^{1} \cdot (AM_{a})_{TR} - C_{TR}^{2} \cdot (AM_{a})_{TR} - T_{TR}^{2} \cdot I_{TR}$$

$$C_{TR} = D_{TR}^{2} \cdot (AM_{a})_{TR} - C_{TR}^{2} \cdot (AM_{a})_{TR} - C_{TR}^{2} \cdot (AM_{a})_{TR}^{2} - C_{TR}^{2} \cdot (AM_{a})_{TR}^{2$$

Equations for Tail Rotor Aerodynamics Force and Moments AC Mechanization.

Figure 18. Tail Rotor Aerodynamics Force and Moments (Sheet 2)
AC Machanization

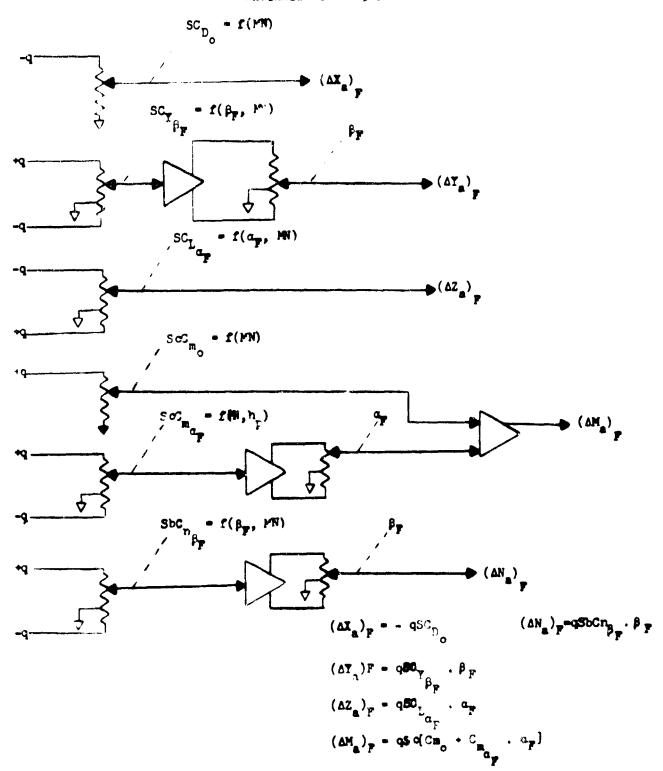


Figure 19. Fuselage Aerodynamics Forces and Moments AC Mechanisation

- Block (?), Figure 29 mechanised by Figure 50.
- Block (8), Figure 29 mechanised by Figure 51.
- Block (9), Figure 29 mechanised by Figure 52.
- Block (10), Figure 29 mechanised by Figure 4.
- Block (11), Figure 29 mechanised by Figure 5.
- Elock (12), Figure 29 mechanised as in Section III.A.
- Rlock (13), Figure 29 mechanised as in Section III.A.
- Mock (14), Figure 29-instructor imputs as in Section III.A.

This completes the mechanisation of the tilt-wing aircraft.

Summary Tilt-Wing Aircraft. The mechanisation of the tilt-wing aircraft was accomplished by evaluating the block diagram of the aircraft (Figure 29) block by block just as for the single and tandem-rotor helicopters in accord with Figure 1. As for the helicopters, an evaluation of component complexity is done in order to choose between an AC or IC system of mechanisation. Table 23 is an accounting of the tilt-wing aero-dynamics: Block (h) of Figure 29. In Table 23 the various figures that have already been considered are interpreted according to component (amplifier, serve, potentiometer, sine-cosine potentiometer and resolver) count for AC and DC mechanisations. The results of Table 23 are incorporated into Table 2h which is the total tabulation of tilt-wing components just as was done for the single rotor helicopter in Table 18. The tilt-wing summary is shown in Table 25 which corresponds to Tables 19 and 22 for the helicopters.

The complexity of the tilt-wing AC system is 566-1/4 versus 915-1/4 for the DC system. As in the AC and DC system comparisons for the helicopters, this difference in complexity is marked. Again the difference in complexity is primarily due to the greater number of amplifiers needed for the DC mechanisation (the need of sign inversions for many functions) and the weight associated with the DC amplifier being greater than of the AC amplifier. Consequently, unless DC amplifiers can be redesigned to give both signs of a function and are competitive in complexity, or the choice for a DC system is based on other factors than components, the AC system is favored.

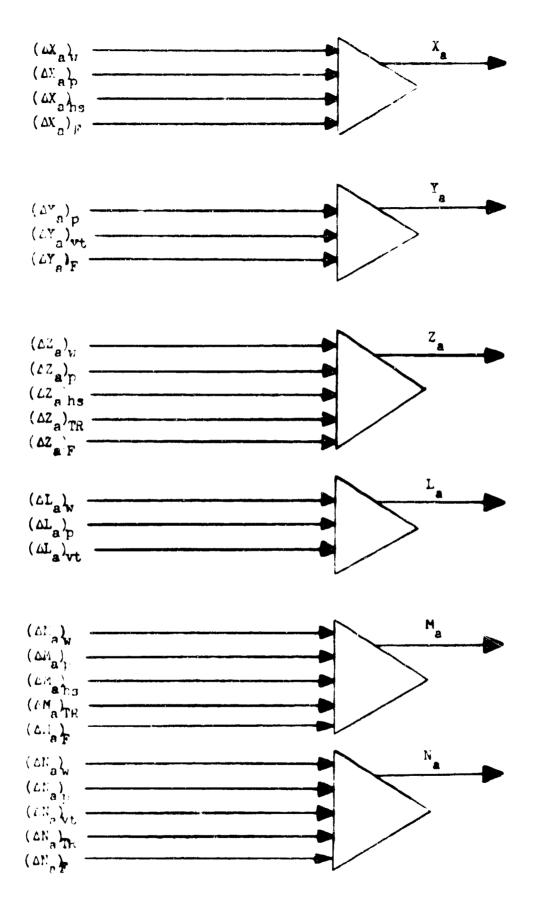


Figure 50. Force \( \Sigma\) Mechanization

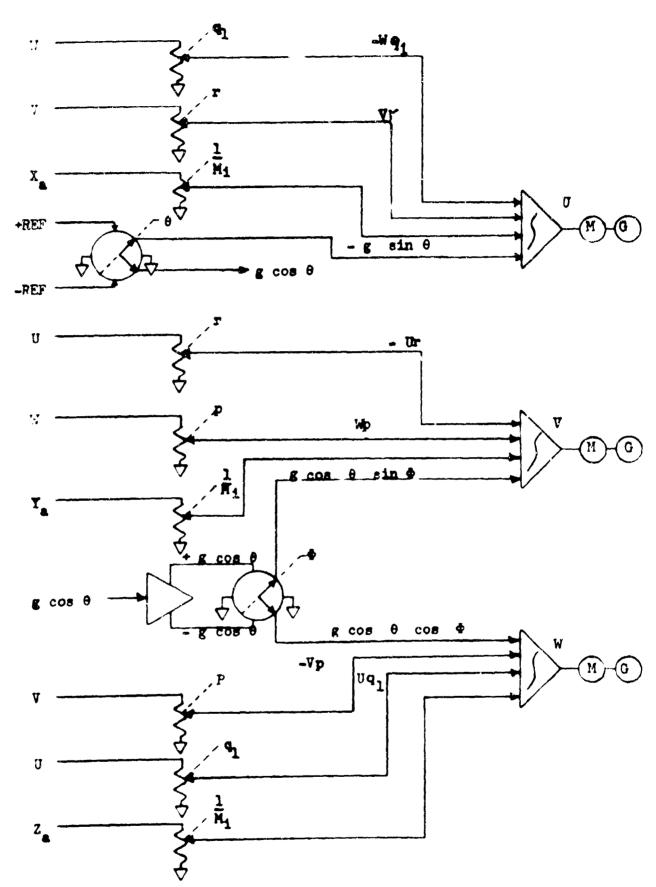


Figure 51. Integration - Velocities (U, V, W) AC Mechanization

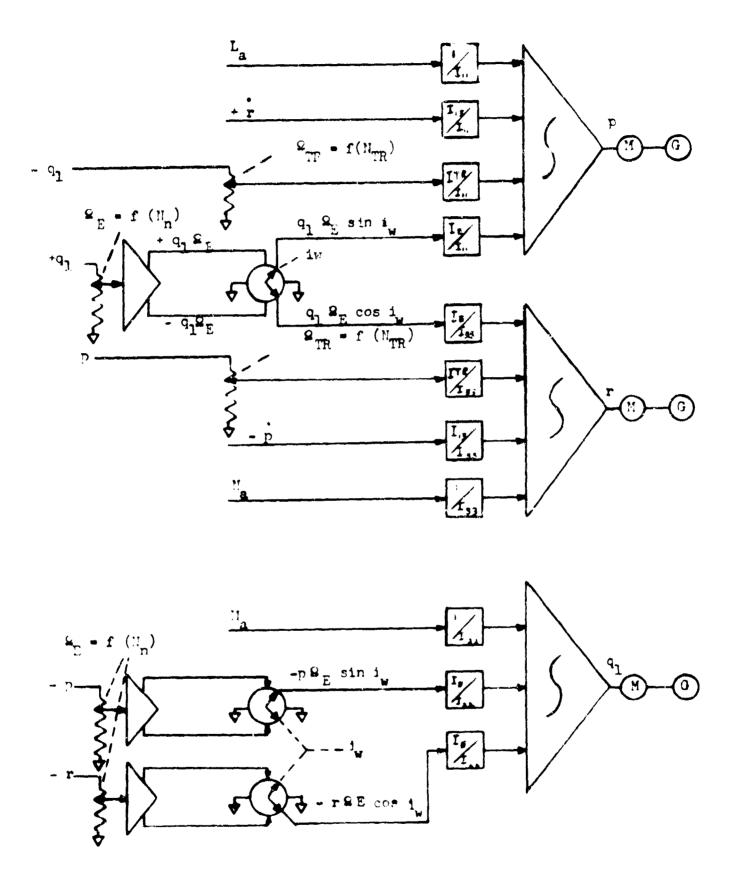


Figure 52. Intermation = Augular Velocities (p, q, r) AC Mechanishts n

15 - 14 - 14 - 14 - 14 - 14 - 14 - 14 -	Arte	11/101	S	rvo	Р	ं०६	S-0	Pot	Re	olver
FLENKE	AC	DC	A.C.	DC	AC	ЭС	AC	DC	AC	DC
31	13	19	1	1	8	8	4	4		
32	7	7	3	3	ę	8		4	2	
33	! 6.4	4	į,	4	24	57				
34.		14	L	4	16	16				
35	В	е			16	16				
36	1	l.			24	SI?				
37	22	<b>3</b> 8					16	16		
3€	23	36					12	15		
39	)	5			2	2				
440	8	e	1	1	4	4				
41	1	1			2	2				
42	12	11	3	3	5	2		6	3	
43	5	1.0								
نيل	6	7	1	1	2	۷	4	4		
45	1	1	1	1	<b>U</b>	5				
46	3	3			13	13				
47	9	1:3	1	1	9	9	2	2		
48	10	12	14	4	11	11	1	1		
49	L	7			,¥	9				

Table 23. Tilt-wing Aerodynamics Tabulation Block (4)

	Amoli	fier	Ser	70	P	ot	S-0	Pot	Re	solve
	AC	DC	AC	DC	AC	DC	AC	DC	AC	DC
Block (2)										
Block (2)										1
Block (3) Figure 30	11	13	5	5	3	3		4		
Block (h) Figure 31 to 19	147	198	23	23	155	155	39	39	5	
Block (5) Figure 50	3	3								
Block (6)	3	3	3	3	2	2				
Block (7) Figure 50	9	3								
Cock (8)	Ь	5	3	3	9	9	2	2		
Block (9) Figure 52	6	9	3	3	5	5	,	3		
3lock (10)	9	15	3	3				6	1	
71ock (11)	7	12	3	3			2	4	1	
Block (12)	2	2								
3lock (13)										
Block (14)										
Total	195	263	43	43	174	174	46	53	9	

Table 24. Tilt-Wing Tabulation

DC AC Wt. No. No. Wt. 195 193 Amplifier 263 526 Servo 43 301 43 301 43-1/2 174 ot 174 43-1/2 58 S-C Pot 11-16 46 22-2/3 4-3/2 Resolver 9 893-1/6 555-1/2 Complexity

Table 25. Tilt Wing Summary

#### SECTION IV

#### SUMMARY

This report presents a set of guidelines for the selection of the optimum analog mechanisation of the V/STOL simulations set forth in reports NAVTRADEVCEN 1205-1 and 1205-2. The guidelines were developed as a series of recommendations by consideration and discussion of certain aspects governing the selection of an optimum computer. These aspects are summarized below and the resultant recommendations briefly stated.

#### A. AIRCRAFT DATA CONVERSION FOR USE IN THE COMPUTER

Raw aircraft data supplied by the aircraft manufacturer is generally empirical in nature and supplied in the form of smooth curves. The most economical and least complex method of storing and presenting this information to the computer is through the use of tapped or shaped potentiometers driven by serve shafts. Since potentiometers may be used with equal facility in either AC or DC computers, the conversion of data does not influence the choice of computer type one way or the other.

#### B. SIMPLICITY OF SIMULATION EQUATIONS

To obtain an optimum simulation of a given set of simulation equations it is necessary to simplify the given equations by removal of mathematically insignificant and physically insignificant terms of the equations. This is done to the extent allowed by the required extent of simulation. The equations mechanized in this report were already in the simplified state when taken from Volumes I and II. Since the simplification of the equations is a first step in the simulation process, the optimisation obtained by the simplifications would be the same in either an AC or IC computer. Hence, as with data conversion, equation simplification does not influence the choice of computer.

### C. COMPUTER FLEXIBILITY

The need for flexibility in the computer used for aircraft simulation is apparent when one considers the usual requirement that the simulator be developed concurrently with the development of the aircraft to be simulated. The aircraft manufacturers are forced to work with a great deal of empirical data and consequently required to redirect design efforts in order to obtain the exact aerodynamic characteristics selected as a design goal. This results in a considerable amount of engineering changes. Since these changes are manifested as changes to the aerodynamic functions stored in tapped potentiometers it is a simple matter to retap the potentiometers in either an AC or a DC computer since both use potentiometers. Consequently, as in paragraph A. above, this aspect does not influence the computer choice.

#### D. COMPUTATIONAL SEQUENCE

The computational sequence used during the mechanisation of a set of simulation equations is an extremely important optimisation technique. It has a direct effect on the accuracy, flexibility and complexity of the computer. However, as in A, B, and C above, it has no direct bearing on the choice of a computer type as AC or BC. Once the choice has been made to use AC or BC carrier computation, the computational sequence can be utilised to arrive at an optimum mechanisation.

#### E. CHOICE OF CARRIER

The choice of carrier to be used in the simulation computer is the most important aspect to be considered when making the selection of computer type. The simulation problem must be examined to determine the the computer response requirements dictated by the expected signal frequencies. In Section II this was done for the V/STOL simulation first to determine which AC carrier should be used. It was decided that if an AC carrier were to be used it should be 60 cycles. This decision was made since the advantages of accuracy and response of a 400 cycle system are overshadowed by the reduced response requirements of the V/STOL simulation, the relative ease in meeting computer size restrictions in flight simulators, and the maintenance and phase shift problems introduced by 400 cycle carriers. Having narrowed the choice to either a DC or AC system the advantages and disadvantages afforded by the various computational techniques were then discussed.

It was decided that out of the five basic computational techniques of amplification, integration, multiplication, trigonometric resolution and function generation the AC techniques afforded the best applicability to the V/STOL simulation problem in all areas except function generation and multiplication. In these two areas the techniques were found to be equally weighted. Consequently, as far as applicability of techniques is concerned, the choice of computer type is recommended as a 60 cycle AC carrier computer.

#### F. CHOICE OF SYSTEM

The results of the above discussions in conjunction with the component summaries of Section III indicate clearly the optimum computer to be used on the V/STOL simulation mechanisation is the 60 cycle AC computer. Not only can the mechanisation be done with less components but the cost and computer size are also reduced.

### SECTION V

### BIRLIOGRAPHY

- 1. Volume I, Helicopter Analysis Report, NAVTRADEVCEN 1205-1
- 2. Volume II, V/STOL Analysis Report, NAVTRALEVCEN 1205-2
- 3. Connelly, Mark E., Simulation of Aircraft, Report 7591-R-1, 15 February 1958
- 4. Connelly, Mark E., Computers for Atroraft Simulation, Report 7591-R-2, 15 December 1959
- 5. Northrop Aircraft, Inc., Dynamics of the Aircrame, Buder Report AE-61-411, September 1952
- 6. Vertol, Technical Aircraft Data for the Design and Fabrication of the Model HRB-1 Helicopter Operational Flight Trainer, Volume 3 of 3 volumes, Report No. 107-M-62.

### SECTION VX

### NOMENCIATURE AND EQUATIONS

### A. HELLCOPIER

### I. MINTERNOLLARURE

The following list of symbols is used throughout this report. The list of symbols are arranged in alphabetical order with lower case letters listed first, then capital letters followed by greek letters and symbols of miscollaneous origin.

MINROT	DEAM'RIPTION	UNITS	POSITIVE SENSE
· Ch	Rotus coning angle	radians	υp
·le	Longitudinal flap angle	radians	Rearward
ble	Lateral flap angle	radians	Right
d.	Longitudinal center of gravity	feet	Forward of reference point
ch	Lateral center of gravity position	feet	Right of reference point
₫ <b>3</b>	Normal center of gravity position	feet	Below reference point
E	Operator constant = 32,2	ft/ees <sup>2</sup>	Downwar
<b>T</b> P	Pressure altitude	feet	Upwards
'n	Rate of climb	ft/sec	Upward
q	Incorpressible dynamic pressure	1b/ft <sup>2</sup>	
G <sub>2</sub>	Fuselage dynamic pressure	16/ft <sup>2</sup>	
<b>9</b> 2	Pitching rate	red/sec	Nose up
G*-3-	Blade element dynamic pressure	lb/ft <sup>2</sup>	
r	Turning rate	red/sec	Nose right
t	Air temperature	degrees C	
Δt	Ground temperature variation from standard (99°F)	degrees ?	
7	Distance from blade hinge to blade station	feet	Maximum et

SYMB :	DESCRIPTION	UNITS	POSITIVE SENSE
A le	Lateral control angle	degrees	Right
A <sub>v</sub>	Elade element area	fest <sup>2</sup>	
F	Longitudinal control angle	deg <b>rees</b>	Forward
c	Flade chord	feet	
) <b>\-</b> \ <b>y</b>	Blade element drag coefficient	none	
<sup>€</sup> L <b>∀-y</b>	Flade element lift coefficient	none	
$c_{ m T}$	Tail rotor coefficient of thrust		
COTR	Coefficient of tail rotor torque	non- dimensional	Accelerates rotor
מ	Drag	lbs.	Rearward
D <sub>F</sub>	Fuselage drag force	lbs.	Rearward
D <b>√-y</b>	Elade element drag	lbs.	Rearward
E	East position		
£	Ground speed, east	ft/sec	
F <sub>LW</sub>	Force - Left wheel	lbs.	Upward
F <sub>RW</sub>	Force - Right wheel	lbs.	Upward
F <sub>TW</sub>	Force - Tail Wheel	lbs.	Upward
$^{\mathtt{F}}\mathbf{x}_{\mathtt{R}}$	I Force due to main rotor	lbs.	Forward
$\mathbf{F}_{\mathbf{Y}_{\mathcal{P}}}$	Y Force due to main rotor	lbs.	Right
н	Altitude above the field	feet	Upward
H <sub>F</sub>	Altitude of field	feet	Upward
H <sub>LW</sub>	Height left wheel above field	fest	Minus after touchdown
H <sub>H<b>O</b>M</sub>	Height right wheel above field	feet	Minus after touchdown

SYMBOL	DESCRIPTION	UNITS	Positive sense
R <sub>TW</sub>	Height tail wheel above field	feet	Mimus after touchdown
ITOT	Moment of inertia of rotor system as seen at main rotor	slug-ft <sup>2</sup>	
I <sub>x</sub>	Moment of inertia about I axis	elug-ft <sup>2</sup>	
I <sub>XX</sub> B	Blades moment of inertia about flapping hinge	1710 slug-ft <sup>2</sup>	
I <sub>y</sub>	Moment of inertia about I axis	slug-ft <sup>2</sup>	
Ig	Moment of inertia about Z axis	slug-ft <sup>2</sup>	
L	Lift	lbs.	Upward
La	Rolling moment about plane X axis	16 <b>-</b> ft	Right wing down
L <sub>F</sub>	Fuselage lift force	lbs.	Upward
I <sub>MR</sub>	Lift due to main rotor	lbs.	Upward
LR	Main rotor rolling moment	lb-ft	Pushes right wing down
L <sub>RH</sub>	Rotor hub rolling moment	lb-ft	Right wing down
Ly, Lyor	Rotor lift force	lbe.	Ũ <b>p</b>
T <b>y-y</b>	Hlade element lift	lbs.	<b>Operard</b>
M	Pitching mement	16-8t	Nose up
Ha	Pitching moment about place T exis	16 <b>-</b> ft	Nose up
M	Mach number		
MB	Hade mass	elage	
M <sub>F</sub>	Puselage pitching moment	16 <b>-</b> £t	Pushes nose up
Mı	Mass of aircraft	aluga	
H <sub>LO</sub>	Landing gear pitching moment	16-24	Pashes nose

SYMBOL	TE-CRIPTION	UNITS	POSITIVE SENSE
M <sub>R</sub>	Effect of main rotor on pitching moment	lb-ft	Pushes mose up
M <sub>PH</sub>	Rotor bub pitching moment	lb-ft	No se up
₩ ♦	Blade element aerodynamic flapping moment	ft-lbs	Moves blade tip up, increase
N	Engine rotational velocity	RPM	
Ň	Ground speed, north	ft/sec	
Ña	Bank moment about plane Z axis	lb-ft	Nose right
N <sup>k</sup>	Fuselage yaw moment	lb-ft	Pushes nose right
NR	Main cotor yaw moment	lb-ft	pushes nose right
N TW	Effect of tail wheel on yew moment	1b-ft	Pushes nose
p	Rolling rate	red/sec	Right wing down
P <sub>B</sub> L	Pressure brake, left	lbe-ft <sup>2</sup>	
PBR	Pressure Brake, right	lbs-ft <sup>2</sup>	
P <sub>S</sub>	Static pressure at sea level	in. of Hg.	
$c^{ET}$	Left engine torque	ft-lbs	Speeds up rotor
Q <sub>ER</sub>	Right engine torque	ft-lbs	Speeds up rotor
Q <sub>MDR</sub>	Main rotor torque	ft-lbs	Speeds up rotor
Q <sub>RB</sub>	Rotary brake torque	ft-lbs	Speeds up rotor
O_TR	Tail rotor torque	rt-lbe	Loads engine
OTR q	Tail rotor turbulence factor	non- dimensional	

### MANTRA DEVCEN 1205-3

SYMBOL	DESCRIPTION	UNITS	POSITIVE SENSE
Ř	31 ft. Main rotor radius	feet	
R/C	Rate of climb	ft/sec	Upward
ŢŢ	X axis velocity in air mass	ft/sec	Forward
$v_{\mathbf{G}}$	Speed in X body axis direction relative to a point on the ground	ft/sec	Forward flight
UPTR	Tail rotor normal velocity	ft/sec	Positive to the right
<sup>U</sup> Р <b>V-У</b>	Hlade element relative velocity in air perpendicular to blade span (long) and to $\mathbf{U}_{T}$	ft/sec	Underside of blade exposed to the wind
<sup>U</sup> T <b>∀-y</b>	Elade element relative velocity in air perpendicular to blade span (long) axis and to rotor rotation axis	ft/sec	Positive in hover
$\mathbf{u}_{\mathbf{w}}$	Wind speed in X axis	ft/sec	Wind blows on nose
٧	Y axis velocity in air mass	ft/sec	to right
v <sub>G</sub>	Speed in Y body axis direction relative to a point on the ground	ft/sec	Flight to right
v <sub>T</sub>	Fuselage (total) airspeed	ft/sec	Always positive
v <sub>ra</sub>	Total velocity of tail rotor hub	ft/sec	Always positive
٧w	Wind speed in Y axis	ft/sec	Wind blows on right wing
W	Z axis velocity in air mass	ft/sec	Down
WF	Fuel flow	lb/hr	Drains tank
$M^{\mathbf{G}}$	Speed in Z Rody axis direction relative to a point on the ground	ft/sec	Descent
W <sub>1</sub> ,	Induced airflow in Z body axis direction	ft/sec	Air blows down
(W <sub>1</sub> )	Mean inflow velocity	ft/sec	Air blows downward
(W <sub>1</sub> )	Local inflow velocity	ft/sec	Air blows down

### NAVTRATEVOEN 1205-3

SIMBOL	DESCRIPTION	UNITS	POSITIVE SENSE
-₩w	Wind speed in / axis	fo/sec	Wind blows down
$\frac{(W_1)}{(W_1)}$	Inflow distribution factor = F(y)		
x	Longitudinal force	lbs	Forward
X <sub>a</sub>	Total serodynamic force in fuselage body I direction	158	Forward
r,	Passlage longitudinal force	lbs	Forward
x <sub>ro</sub>	Landing gear friction	lbs	Toward nose
Y	Lateral force	lbs	right
T <sub>a</sub>	Total serodynamic force in fuselage Y direction	lbs	right
T <sub>B</sub>	Distance from flap hinge to blades c.g. = 8.75 ft.	ft.	
Yp	Puselage lateral forces	7ps	right
YTR	Side force due to tail rotor	1be	Positive to right
Z	Normal force	lbs	Downward
Z.	Total force in fuselage 2 direction	180	Downward
Z <sub>p</sub>	Promise automatical desires	lbe	alman manda
z <sub>10</sub>	landing gear normal force	1bs	Downward
α	Angle of attack	degrees	Relative Wind from below x axis
a <sub>p</sub>	Puselage angle of attack	degrees	Wind comes from below x axis
<sup>C</sup> TR	Tail rotor disc place velocity engls	degrees	Relative wind from below x exis
Q+~F	Slade angle of attack	degrees	Wind comes from below blade x-y plane

SYMBOL	<u> TESCRIPTION</u>	UNITS	POSITIVE SENSE
$\beta_{\overline{F}}$	Sideslip angle	degrees	Relative wind from right
β <sub>B</sub>	Hall angle (instrument)	degrees	Pall right
β TR	Tail rotor sideslip angle	degrees	Relative wind from right
β 🛊	Blade flap angle at asimuth	degrees	Blade tip
\$ *	Rate of change of blade element flap angle	deg/sec	Elade Tip upward
θ	Pitch angle of fuselage I axis	degrees	Level = 0° Up = 90°
ė	Rate of change of Euler angle, 0 (Pitch angle)	rad/sec	Nose up
e <sub>TR</sub>	Pitch of tail rotor blade at 3/4 point	degrees	Positive when leading edge is deflected toward pylon
			py 1011
P	Air density	slugs/ft <sup>3</sup>	ру 1011
<i>P</i>	Air density Rell angle of fuselage	slugs/ft <sup>3</sup>	Positive right wing down
<i>P</i> •	•		Positive right
•	Rell angle of fuselage  Rate of change of Euler Angle, *	degrees	Positive right wing down Right wing
•	Rell angle of fuselage  Rate of change of Euler Angle, © (Roll angle)	degrees	Positive right wing down Right wing down Wind comes from below the un- pitched blade
\$ \$ \$ \$\psi_{\psi_{\psi}}	Rate of change of Euler Angle, & (Roll angle)  Hlade element inflow angle	degrees rad/sec degrees	Positive right wing down  Right wing down  Wind comes from below the unpitched blade plane  North = 0°
* * * * * * * * * * * * * * * * * * *	Rate of change of Euler Angle, (Roll angle)  Hlade element inflow angle  True heading of fuselage I axis	degrees degrees	Positive right wing down Right wing down Wind comes from below the un- pitched blade plane North = 0° East = 90° Wind blows toward this

### NAVTRAINEVOEN 1205-3

SYMBOL	DESCRIPTION	UNITS	POSITIVE SENSE
<b>∧</b>	Tail rotor solidity/advance ratio parameter	Non-dimensional	
2	Tail rotor velocity/thrust ratio	non- dimensional	
AR	Aft rotor rolling moment	lòft.	Roll right
FR	Front rotor rolling moment	lbft.	Roll right
ARH	Aft rotor hub rolling moment	lbft.	Roll right
FRH	Front rotor hub rolling moment	1bft.	Roll right
$\neg$	Fuselage rolling moment	16ft.	Roll right
TLO	Landing Gear rolling moment	lbft.	Roll right
A RA	Rolling moment due to rough air	lbft.	Roll right
4	Fuselage rolling moment	lbft.	Roll right

### HELICOPTER SIMULATION EQUATIONS

### a. SINGLE ROTOR DEVICES

## (1) FUSELAGE AERODYNAMICS

# ag βr Puselage Angle of Attack and Sideelip Angle

$$\alpha = h^{\circ} + \arctan \frac{W - f \left(\frac{W_1}{W_1}\right)}{U} f(W)$$
(6-1)

$$\beta = \arctan \sqrt{U^2 + \left(W - f\left(\frac{W_1}{max}\right) f\left(W\right)\right)^2}$$
 (6-2)

# G. Fuselage Dynamic Pressure

$$q = \frac{1}{2} / [ u^2 + v^2 + (w - f) (w_{1}) ^2 ]$$
 (6-3)

# Dp, Puselage Drag

$$D_{p} = q \left\{ 500 \left[ 1 - f \left( \frac{1}{4} \right) + f \left( \frac{1}{4} \right) f \left( \frac{1}{4} \right) \right] + \frac{1}{4} 2.25 \right\}$$
 (6-4)

K<sub>1</sub> = 0 for no external stores aboard

= 1.0 with external stores aboard

# Lp, Passlage Lift

$$L_p = \{91.125 [.309 + f(q)] + K_1 5.63\} q$$
 (6.5)

K1 = 0 for no external stores abound

- 1.0 with external stores aboard

## Puselage Airspeed

$$v_{T} = \sqrt{v^{2} + v^{2} + \left(w - f\left(\frac{w_{1}}{man}\right) f\left(w\right)\right)^{2}}$$
 (6-6)

## (2) TAIL ROTOR AERODINAMICS

$$\frac{\rho_{TR}}{\rho} - f(a) \tag{6-7}$$

## CTR, Tail Rotor Torque at Main Rotor Shaft

$$C_{\text{TR}} = -\left[C_{\text{Q}_{\text{TR}}} / R_{\text{TR}}^{2} (\Omega R)_{\text{TR}}^{2} R_{\text{TR}}\right] 6.1$$

$$C_{\text{Q}_{\text{TR}}} = .008 l_{1} f \begin{pmatrix} C_{\text{T}_{\text{TR}}} \end{pmatrix}$$
(6-8)

# $C_{\overline{T}_{\overline{T}R}}$ , Tail Rotor Coefficient of Thrust

$$C_{T_{TR}} = A_{32} + B_{32}$$
;  $A_{32} = .0480 \ f (Q_{TR}) + .0211 \ f(Q_{TR})f(A_{1})(6-10)$ 

# UPTR, Tail Rotor Normal Velocity (Nondimensional)

$$U_{P_{TR}} = \frac{V - 36.06 r + 2.7 l_{1} p}{30.5 \Omega}$$
 (6-11)

# A , Tail Rotor Solidity/Advance Ratio Parameter

$$-4 = 0.1945 A_{34} + 0.1790 B_{34}$$
 (6-12)

$$A_{3h} = f(\mathbf{g})$$
  $B_{3h} = f(\boldsymbol{\beta}_{TR})$ 

# $\alpha_{\mbox{\scriptsize TR}},$ Tail Rotor Disc Plane Velocity Angle

$$\alpha_{\text{TR}} = \tan^{-1} \frac{W + 36.06 \, q_1}{U}$$
 (6-13)

 $U = U \sin \alpha_{TR} - (W + 36.06 q_1) \cos \alpha_{TR}$ 

# $\beta_{TR}$ , Tail Rotor Sideslip Angle

$$\beta_{TR} = \tan^{-1} \frac{V - 36.06 \text{ r} + 2.7 \text{l} \text{ p}}{\sqrt{U^2 + (W + 36.06 \text{ q}_1)^2}}$$
 (6-1h)

$$0 = \sqrt{U^2 + (W + 36.06 q_1)^2} \sin \beta_{TR} - (V-36.06 r + 2.7 lp) \cos \beta_{TR}$$

# VTR, Total Velocity of Tail Rotor Hub

$$v_{TR} = \sqrt{v^2 + (v - 36.06r + 2.74p)^2 + (w + 36.06 q_1)^2}$$
 (6-15)

## 1. Tail Rotor Velocity/Thrust Ratio

$$\mathcal{A} = .056L \, V_{TR} \, f \left( {}^{C}_{TR} \right) \tag{6-16}$$

# $\theta_{\rm TR}$ , Pitch of Tail Rotor Elade at $3/\mu$ Point

$$\theta_{TR} = 10.03 \ \Delta C' - 1.8$$

$$0 \le \Delta C' \le 2.293$$

$$\Delta C' = .1076_R + .0676_{\theta C} + 1.77 + ASE Inputs$$
(6-17)

# R VSC BC

### (3) LANDING GEAR

# FRW, Right Wheel Force

$$F_{EW} = -10,000 \left( H_{EW} + \frac{h}{l_1} \right)$$
 (6-18)

Only when right wheel has touched down. Otherwise sero.

# F<sub>IN</sub>, Left Wheel Force

$$F_{LW} = -10,000 \left(H_{LW} + \frac{\dot{h}}{l_L}\right)$$
 (6-19)

Only when left wheel has touched down. Otherwise zero.

# F<sub>TW</sub>, Tail Wheel Force

$$P_{TW} = -2,500 \left( H_{TW} + \frac{\dot{h}}{4} \right)$$
 (6-20)

Only when tail wheel has touched down. Otherwise sero.

#### (4) LONGITUIENAL FORCE

$$x_n = x_p + x_{LO} + x_R + \Delta x_{RK} + x_{WH}$$
 (6-21)

# $\mathbf{X}_{\mathbf{p}}$ , Puselage Longitudinal Force

$$I_p = I_p \sin \alpha_p - D_p \cos \alpha \cos \beta$$
 (6-22)

# Inding Gear Force

$$z_{LO} = K [.025 z_{LO} - 2.53 (P_{HR} + P_{EL}) K_{O}$$
 (6-23)

$$K = +1$$
  $U_0 > 2.25 fps$ 

$$K = 0$$
 -2.25  $< U_0 < 2.25$ 

$$x = -1$$
  $v_0 < -2.25 fpe$ 

## (5) SITE FORJE

# Ya, Total Side Force

$$Y_{a} = Y_{F} + Y_{TR} + F_{Y_{R}} + \Delta Y_{RA} + Y_{WH}$$
 (6-24)

# Yp, Pucelage Side Feres

$$Y_{p} = -D_{p} \sin \beta_{p} \qquad (6-25)$$

### (6) DOWN FORCE

# Za, Total Down Porce

$$z_a = z_p + z_{10} - z_{10} + z_{20} + z_{10}$$
 (6-27)

# Zy, Passlage Effect

z<sub>p</sub> - - L<sub>p</sub> cos c<sub>p</sub> - D<sub>p</sub> sin e cos 
$$\beta_p$$
 (6-28)

# Z<sub>10</sub>, Landing Gear Force

$$Z_{LO} = -(P_{EM} + P_{LM} + P_{TM})$$
 (6-29)

#### (7) ROLLING MOMENTS

### Total Rolling Moments

$$L_{a} = Y_{a} d_{b} + L_{R} + L_{RH} + 2.7h Y_{TR} + L_{LO} + \Delta L_{a} + q_{1}$$

$$\Omega = (564.5) + L_{R} + L_{LR}$$
(6-30)

# LR, Main Rotor Rolling Moments

$$L_{R} = 7.85 P_{Y_{R}}$$
 (6-31)

# Lin, Landing Gear Rolling Moments

$$I_{LO} = 6.5 (P_{LN} - P_{RN})$$
 (6-32)

# $\mathcal{L}_{\mathbf{F}}$ , Fuselage Effect

### (8) PITCH MOMENTS

# Mg, Total Pitch Moment

$$H_{a} = Z_{a} d_{x} - I_{a} d_{x} + H_{R} + H_{LG} + H_{F} + H_{RH} - \frac{Q_{TR}}{6.1} + \Delta M_{a} - p \Omega (564.5) + H_{WH}$$
(6-94)

### Horisontal Stabiliser

All horisontal stabiliser effects are cancelled due to incorporation into proper fuselage effects.

## MR, Main Rotor Effect

$$H_{R} = -7.85 F_{I_{R}} = .073 I_{MR}$$
 (6-36)

# $\mathbf{H}_{\mathbf{LO}}$ , Landing Gear Pitch Momente

$$H_{LO} = 4.38 (F_{HH} + F_{LH}) = 18.99 F_{TW} + 5.36 X_{LO}$$
 (6-37)

## Mp, Fuselage Pitch Moments

$$M_p = \{390 [.058 + f(\alpha)] + K_1 23.6\}$$
 q (6-38)

K1 = 0 for no external stores aboard

 $K_1 = 1.0$  with external stores aboard

#### (9) YAW MOMENTS

## N Total Yaw Moments

$$N_{a} \sim -Y_{a} A_{x} + N_{y} + N_{F} + N_{F} - 36.06 Y_{TR} + N_{LG} - Q_{MR}$$

$$+ I_{TOT} \mathring{\Omega} + N_{R} + \Delta_{N_{a}} + N_{WH} \qquad (6-39)$$

## N<sub>W</sub>, Wheel Yaw Moment

With either or both main wheels on ground and tail wheel on ground with tail wheel look off

$$K_{\rm sf} = 2200 \, \rm U_{\rm G} \, r \, K_{\rm G}$$
 (6-40)

# N<sub>F</sub>, Fuselage Effects

$$N_{\rm p} = 1228.8 \ q \ f(\beta)$$
 (6-41)

# N<sub>r</sub>, Turning Moment Due to Turning Rate

$$-N_T = 102,762 \frac{T}{V_T} q$$
 (6-42)

## N<sub>I.G</sub>, Landing Gear Yaw Moment

$$N_{T,G} = K \ 16.45 \ [P_{BE} - P_{BL}] \ K_G$$
 (6-43)

#### (10) HIATE ELEMENT AEROIMNAMICS

#### y, cos v, sin v Values

In an equation containing y, cos \( \psi \) and/or sin \( \psi \), the equation must be computed as many times as necessary to include all combinations. That is 3 times for y alone

6 times for sin \( \psi \) and/or cos \( \psi \) alone
18 times for both \( y \) and sin \( \psi \) and/or cos \( \psi \)

Stations are distinguished by subscripts v-y. Thus, the 18 blade element stations are denoted 0-9.9, 0-21.8, 0-28.1, 60-9.9, 60-21.8, etc.

### Tangential Velocity

### Vertical Velocity

$$U_{P_{\psi \to y}} = W - W_{1 \psi \to y} - \psi \qquad (0.0173) + (1.052 + y)$$

$$(q_{1} \cos \psi + p \sin \psi) \qquad (6-45)$$

$$-\beta_{\psi}(U \cos \psi - V \sin \psi) (.0173)$$

# a, Inflow Angle

$$\Phi_{\psi \to y} = \frac{\overline{U}_{p_{\psi \to y}}}{\overline{U}_{T_{\psi \to y}}} \quad \text{(rediens)}$$

### Made Angle of Ittack

$$c_{\psi-y} = \theta_{\psi-y} + c_{\psi-y} \tag{6-47}$$

# 0, Pitch Angle, Degrees

$$\theta_{\psi-y} = A_{Os} - A_{ls} \cos \psi - B_{ls} \sin \psi + \theta_{l} y \qquad (6-48)$$

$$A_{0s} = f(\delta_{\theta_0})$$

$$A_{1s} = f(\delta_{\theta_L}, \delta_{\theta_0}, \delta_{\theta_F})$$

$$B_{1s} = f(\delta_{\theta_L}, \delta_{\theta_C}, \delta_{\theta_F})$$

$$\theta_1 = -.258 \text{ deg/ft.}$$

## P. Density of Atmosphere

$$\rho' \begin{cases} 0 \text{ when } \Omega < 5 \\ \rho \text{ when } \Omega \geq 5 \end{cases}$$

# 

# Que, Que, Main Rotor Shaft Moment

$$c_{MR_{\psi}} = \rho \left[ (78.5 \text{L} \ \text{U}_{T} \ \text{U}_{P} \ \text{C}_{L} \Big|_{\psi=9.9} - 73.02 \ \text{U}^{2}_{T} \ \text{C}_{D} \Big|_{\psi=9.9} \right]$$

$$+ (190.0 \ \text{U}_{T} \ \text{U}_{P} \ \text{C}_{L} \Big|_{\psi=21.8} - 180.3 \ \text{U}^{2}_{T} \ \text{C}_{D} \Big|_{\psi=21.8} \right)$$

$$+ (60.12 \ \text{U}_{T} \ \text{U}_{P} \ \text{C}_{L} \Big|_{\psi=28.1} - 106.2 \ \text{U}^{2}_{T} \ \text{C}_{D} \Big|_{\psi=28.1} ) \right]$$

$$Q_{MR} = 5/6 \quad \chi \quad Q_{MR}$$
 (6-51)

# Ly, LMR, Rotor (2) Forces

$$I_{\psi} = \left[ 7.733 \text{ } v^{2}_{T} \text{ } c_{L} \right]_{\psi = 9.9} + 8.395 \text{ } v^{2}_{T} \text{ } c_{L}$$

$$+ 1.969 \text{ } v^{2}_{T} \text{ } c_{L} \right]_{\psi = 28.1}$$

$$(6-52)$$

$$L_{MR} = 5/6 \left( \sum_{\psi} L_{\psi} \right) \left[ 1 + f(H) \cdot f(V_{T}) \right]$$
 (6-53)

$$D_{\psi} = \rho \left[ (6.435 \ v_{T}^{2} \ c_{D} \right]_{\psi = 9.9} - 6.872 \ v_{T} \ v_{P} \ c_{L} \Big|_{\psi = 9.9}$$

$$+ (9.340 \ v_{T}^{2} \ c_{D} \Big|_{\psi = 21.8} - 8.741 \ v_{T} \ v_{P} \ c_{L} \Big|_{\psi = 21.8} )$$

• (3.390 
$$\sigma^2_{T}$$
  $\sigma_{D}$  = 2.046  $\sigma_{T}$   $\sigma_{P}$   $\sigma_{D}$  +-28.1

$$R_{\rm R} = 5/6 \sum_{\phi} (.0173 \beta_{\phi} L_{\phi} \cos \phi - D_{\phi} \sin \phi)$$
 (6-55)

FTR, Rotor T Force

$$R_{1R} = +\frac{5}{6} \sum \{-D_{\psi} \cos \psi - .0173 \beta_{\psi} L_{\psi} \sin \psi\}$$
 (6-56)

CL , Coefficient of Lift Function of a

$$C_{L_{y,xy}} = k_1 f(\alpha_{y,xy})$$
 1 = 1, 2, 3, 4, 5 (6-57)

$$\sigma^2_{T_{+-y}} c_{D_{+-y}} = f(a_{+-y}, \sigma_{T_{+-y}})$$
 (6-58)

By, Plap Angle

$$\beta = 57.3 \ (a_{00} - a_{10} \cos \phi - b_{10} \sin \phi) \tag{6-59}$$

$$\hat{\beta} = 57.3 \Omega \left( e_1 \sin \psi - b_2 \cos \psi \right) \tag{6-50}$$

angle Fourier Coefficients

$$\begin{array}{c} \text{H} \beta_{0} + \text{H} \beta_{0} + \text{H} \beta_{120} + \text{H} \beta_{180} + \text{H} \beta_{240} + \text{H} \beta_{300} \\ & \text{4.768.092} \end{array}$$
 (6-61)

$$a_{10} = \frac{{}^{1}\beta_{60} + {}^{1}\beta_{60} + {}^{1}\beta_{60} - {}^{1}\beta_{60}}{2{}^{1}48_{0}} + b_{10}(0.565) - a_{1}(1.054) (6-62)$$

$$b_{1s} = \frac{-(M_{\beta_{0}} + 0.5M_{\beta_{0}} + 0.5M_{\beta_{0}} + 0.5M_{\beta_{0}} + 0.5M_{\beta_{0}} + 0.5M_{\beta_{0}} + 0.5M_{\beta_{0}} + 0.5M_{\beta_{0}})}{215,160}$$

$$-a_{18}(0.565) - p(1.054)$$
 (6-63)

# LRH, MRH, Rotor Hub Moments on Puselage

$$L_{RH} = - \bullet \frac{5}{6} \sum_{\phi} L_{\phi} \sin \phi + \frac{5}{2} M_{B} I_{B} \bullet \Omega^{2} b_{10} \qquad (6-64)$$

$$M_{RH} = - e^{\frac{5}{5}} \sum_{k} L_{k} \cos k + \sum_{k} M_{E} Y_{B} \cos^{2} a_{10}$$
 (6-65)

# (W<sub>1</sub>), Local Inflow Velocity

$$(W_1)_{+-y} = (W_1)_{\frac{y}{2000}} = (W_1)_{\frac{y}{20$$

#### (11) TRANSLATIONAL AND ANOULAR RATES

#### Body Axis " Ground" Velocities

$$v_{G} = \int \left[ \frac{x_{a}}{R_{G}} - g \sin \theta \right] dt \qquad (6-67)$$

$$V_0 = \int \left[ \frac{Y_0}{M_1} + g \cos \theta \sin \theta - V_0 r \right] dt \qquad (6-66)$$

$$W_0 = \sqrt{\frac{R_1}{R_2}} + g \cos \theta \cos \theta - U_0 q_1$$
 (6-69)

# N. B. h. Earth Axis Velocities

$$\ddot{\mathbf{H}} = \cos \phi \left( \ddot{\mathbf{V}}_{0} \cos \theta + \sin \theta \left( \ddot{\mathbf{V}}_{0} \sin \theta + \ddot{\mathbf{W}}_{0} \cos \theta \right) \right)$$

$$- \sin \Upsilon \left( \ddot{\mathbf{V}}_{0} \cos \theta - \ddot{\mathbf{W}}_{0} \sin \theta \right) \qquad (6-70)$$

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$$\dot{E} = \sin \theta \left\{ U_0 \cos \theta + \sin \theta \left( V_0 \sin \theta + W_0 \cos \theta \right) \right\}$$

. . .

$$h = U_0 \sin \theta - \cos \theta (V_0 \sin \theta + V_0 \cos \theta) \qquad (6-72)$$

### Wind Velocity in Body Arms

Wind blown from the beading (true) at V ft/sec.

No vertical component of wind is considered.

$$- \pi_{y} = \pi_{y}^{2}$$
  $\cos \theta \cos (\Psi - \Psi_{y} + 180^{\circ})$  (6-73)

$$-\cos \Phi \sin (\Psi - \Psi_{\mu} + 180^{\circ})$$
 (6-74)

+ 
$$\sin \theta \sin (Y - Y_W + 180^\circ)$$
 (6-75)

### Relative Air Velocity in Body Axes

$$v = v_{G} + v_{W} \tag{6-76}$$

$$\nabla = \nabla_{G} + \nabla_{W} \tag{6-77}$$

$$W = W_G + W_G \tag{6-78}$$

### Pusslage Angular Rates

$$p = \int \frac{L_a}{L_{xx}} dt \qquad (6-79)$$

$$q_1 = \int \frac{H_a}{I_{TV}} dt$$
 (6-80)

$$r = f \frac{H_a}{I_{aa}}$$
 dt (6-81)

### Mean Inflow Velocity

$$\frac{L_{NR}}{mean} = \frac{L_{NR}}{2PNR^2\sqrt{u^2 + \left(W-f\left(\frac{W_1}{mean}\right)f\left(W\right)^2 + v^2}}$$
 (\*-82)

# 2, Mair. Potor Velocity

$$\frac{1}{6} = \frac{\frac{1}{10} - \frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10}}{10,275}$$
 (6-83)

### North and Bast Positions, Altitude

$$N = \int \hat{N} dt$$
 (4-84)

$$\mathbf{E} = \int \dot{\mathbf{E}} d\mathbf{t}$$
 (6-85)

$$h = \int \hat{h} dt$$
 (e-8e)

### Heading Angle

In 
$$(r \cos \Phi + q_1 \sin \Phi) \sec \theta$$
 rdns/sec. (6-87)

### Pitch Angle

$$\theta = q_1 \cos \Phi - r \sin \Phi$$
 rdns/sec (6-88)

### Roll Angle

$$\Phi = p + f \sin \theta$$
 rdns/sec (6-89)  
 $\Phi = 57.3 \int \Phi dt$  degrees

#### (12) MASS AND INERTIA

## Center of Bravity Position (Feet)

$$d_{x} = -.917 + .333 K_{1} + .333 K_{2} - .0096 M_{fwd}$$
 (6-96)

d<sub>z</sub> = 0

**dv** • ○

#### b. TANIEM ROTOR DEVICES

#### (1) PUSETAGE AERODINAMICS

# $\alpha_p$ , $\beta_p$ Puselage Angle of Attack and Sideslip Angles

$$\alpha_{p} = 9.5^{\circ} + \tan^{-1} \left[ \frac{W - f(^{W}1_{AV}) f(W)}{U} \right]$$

$$\beta_{p} = \tan^{-1} \left[ \frac{V}{U^{2} + [W - f(W_{1AV}) f(W)]^{2}} \right]$$
(6-91)

### q. Puselage Dynamic Pressure

$$q = \frac{1}{2} \rho \left[ V^2_T - 33900 f(W) f(W_{i_{AV}}) + 21238 f(W) f(W_{i_{AV}}) \right] (6-92)$$

# Ly, Paselage Lift

$$L_{\mathbf{p}} = \mathbf{q}_{\mathbf{p}} \mathbf{f}(\beta_{\mathbf{p}}) + \mathbf{q}_{\mathbf{p}} \mathbf{f}(\alpha_{\mathbf{p}}) \tag{6-93}$$

# Dp, Fuselage Drag

$$D_{\mathbf{p}} = q_{\mathbf{p}} \mathbf{r} \left( \beta_{\mathbf{p}} \right) + q_{\mathbf{p}} \mathbf{r} \left( \alpha_{\mathbf{p}} \right) \tag{6-94}$$

#### Puselage Airspeed

$$v_T - \sqrt{v^2 + v^2 + [w - f(w_{1_A V}) f(w)]^2}$$
 (6-95)

#### (2) LANDUNG GEAR

$$\frac{z_{10}}{z_{10}} = -(f(H) - K_1 h)K_H(94,000 - 8360 (.025 + K_{BOVB} + K_{LWB})$$

$$\frac{v_0}{|v_0|}$$
(6-96)

$$\frac{x_{LO}}{x_{LO}} = -[f(H) - x_1h]x_H[8360 + 94000 (.025 + x_{HMB} + x_{LMF})$$

$$\frac{v_0}{|v_0|}$$
(6-97)

# Tio Landing Gear Rolling Moment

$$T_{LO} = Z_{LO} \left[ K_2 \Phi - K_3 P \right] \tag{6-98}$$

(3) LONGITUDINAL FORCE

# I Total Longitudinal Force

$$X_{a} = X_{p} + P_{X_{pR}} + P_{X_{AR}} + \Delta X_{RA} + X_{LO} - .0436 L_{AR}$$
 (6-99)

# I, Puselage Longitudinal Force

$$x_p = -0.986 n_p - 0.165 L_p$$
 (6-100)

(4) SIVE FORCE

# I, Total Side Force

$$T_a = Y_p + F_{T_{pq}} + \Delta Y_{RA} + F_{Y_{AR}}$$
 (6-101)

# I<sub>P</sub> Fuselage Side Force

$$T_{\mathbf{p}} = -q_{\mathbf{y}} f(\beta_{\mathbf{p}}) \tag{6-102}$$

(5) DOWN FORCE

# Za, Total Down Force

$$z_a - z_F - L_{FR} - L_{AR} + \Delta z_{RA} + z_{LO}$$
 (6-103)

(6) VERTICAL FORCES

# Zp, Fuselage Effect

$$z_{p} = 0.165 n_{p} = 0.986 L_{p}$$
 (6-104)

(7) ROLLING MOMENTS

$$L_{a} = + \gamma_{AR} + \gamma_{FR} + \gamma_{FRH} + \gamma_{ARH} + \gamma_{F} \qquad (6-105)$$

$$AR = (7.65 (P_{Y_{AR}})$$
 (6-107)

# y, Puselage Rolling Moment

$$p = q f(\beta_p) + q[f(\alpha_p) f(\beta_p)] - K_1 p,$$
 (6-108)

K to be determined

#### (8) PITCH MOPENTS

# M, Total Pitch Moment

$$H_a = Z_a d_x + M_{PR} + M_{AR} + M_{LO} + \Delta M_{RA}$$
 (6-109)

# MAR Rotor Pitching Moments

$$N_{FE} = -8.18 P_{N_{FR}} + 16.18 I_{FR}$$
 (6-110)

$$H_{AR} = -[8.377 \ F_{X_{AR}} = 16.19 \ L_{AR}]$$
 (6-111)

#### (9) YAN HOMENTS

# N., Total Yaw Moment

$$H_{a} = - T_{a} d_{x} + H_{y} = Q_{yR} + Q_{AR} + H_{LO} + \Delta H_{RA} + H_{yR} + H_{AR}$$
 (6-113)

## NPR, NAR Rotor Yaw Moments

$$N_{FR} = 16.49 P_{T_{FR}}$$
 (5-114)

$$N_{AR} = -16.8 l_4 F_{Y_{AR}}$$
 (6-115)

## N<sub>p</sub> Puselage Yaw Moments

$$N_F = q f (\beta_F) - K_1 r$$
  $K_1$  to be determined (6-116)

#### (10) MOMENTS TURNING

## N, Turning Moment Due to Turning Rate

$$-N_{r} - K_{1} \frac{r}{V_{T}} q$$

$$-K_{2} \rho_{r} V_{T}$$
(6-117)

#### (11) BLADE ELEMENT AERODYNAMICS

#### y, cos Y, sin Y values

In an equation containing y, cos Y and/or sin Y, the equation must be computed as many times as necessary to include all combinations of the forward rotor. That is 3 times for y alone. Six times for sin Y and/or cos Y alone. Eighteen times for both y and sin Y and/or cos Y.

Stations are distinguished by subscripts Y-y. Thus, the 18 blade element stations for each rotor are denoted  $(0^{\circ} -y)$  FR,  $(60^{\circ} -y)$  FR,  $(60^{\circ} -y)$  AR,  $(60^{\circ} -y)$  AR, etc. The subscript FR or AR denotes forward rotor blade station or aft rotor blade station

$$U_{T \downarrow -y} = (e + y) \mathcal{L} + V \cos T + U \sin T$$
 (6-118)

Local Vertical Velocity
$$\frac{V_{p}}{(Y-y)FR} = W-W_{1} - y \stackrel{?}{\nearrow} (0.0173) + (e + y)$$
(6-119)

(q cos T + p sin T)

$$-B_{\Psi}$$
 (0 cos  $\Psi$  -  $V$  sin  $\Psi$ ) (.0173) - 16.49 q<sub>2</sub>

# (Y-y)FR' (Y-y)AR Inflow Angle

$$\mathbf{q}_{\mathbf{Y}-\mathbf{y}} = \frac{\mathbf{U}_{\mathbf{P}} \mathbf{Y}_{-\mathbf{Y}}}{\mathbf{U}_{\mathbf{T}} \mathbf{Y}_{-\mathbf{y}}} \qquad (RAMIAN) \qquad (6-120)$$

# G(Y-y) Blade Angle of Attack

$$a_{\overline{Y}-\overline{Y}} = \theta_{\overline{Y}-\overline{Y}} + \Phi_{\overline{Y}-\overline{Y}} \tag{6-121}$$

# $\theta_{(Y-Y)FR}$ and $\theta_{(Y-Y)AR}$ Pitch Angle, Degrees

$$\theta_{Y-y} = A_{0s} - A_{1s} \cos Y - B_{1s} \sin Y - \theta_{1y}$$
 (6-122)

# MB, Flapping Momente

$$\mathbf{M}_{\overline{\mathbf{Y}}}^{2} = \rho \left[ \mathbf{Q}..8 \ \mathbf{U}^{2}_{\overline{\mathbf{T}}(\overline{\mathbf{Y}}-7.3)} \mathbf{C}_{\overline{\mathbf{L}}(\overline{\mathbf{Y}}-7.3)} + 132.6 \ \mathbf{U}_{\overline{\mathbf{T}}(\overline{\mathbf{Y}}-17)}^{2} \right]$$
(6-123)

# Cypr, CyR, Car Rotor Shart Moments

$$Q_{FR} = \frac{105}{7} \left[ \frac{\sigma_{F} \sigma_{F} \sigma_{F}}{(Y-7.3)FR} - \frac{11}{7} \left[ \frac{\sigma_{F}^{2} \sigma_{F}}{(Y-7.3)FR} \right] \right]$$
(6-124)

$$+ \frac{20 \text{ U}_{\text{T}} \text{U}_{\text{P}} \text{C}_{\text{L}}}{|(\text{Y}-23.1)\text{FR}} - \frac{13 \text{ U}_{\text{T}}^{2} \text{C}_{\text{D}}}{|(\text{Y}-23.1)\text{FR}}]$$

$$\downarrow_{\text{FR}} - \frac{1}{2} \sum_{\text{V}} \downarrow_{\text{V}_{\text{FR}}} \cdot \mathbf{f}(A_{\text{O}_{\text{S}_{\text{FR}}}}) \cdot \mathbf{f}(U) \qquad (6-125)$$

$$\downarrow_{\text{AR}} - \frac{A_{\text{O}_{\text{S}_{\text{AR}}}}}{|A_{\text{O}_{\text{S}_{\text{FR}}}}|} \downarrow_{\text{FR}} \cdot \mathbf{f}(\text{V}) \cdot \mathbf{f}(A_{\text{O}_{\text{S}_{\text{FR}}}}) + \mathbf{f}(A_{\text{O}_{\text{S}_{\text{FR}}}})[\downarrow_{\text{FR}} + 1000(A_{\text{O}_{\text{S}_{\text{AR}}}} - A_{\text{O}_{\text{T}_{\text{FR}}}})]$$

$$(6-126)$$

# L<sub>YFR</sub>, L<sub>FR</sub>, L<sub>AR</sub> Rotor (2) Forces

$$L_{Y_{FR}} = \sqrt{[7.5 \text{ U}_{T}^{2}\text{C}_{L}]_{(Y=7.3)}} + 7.8 \text{ U}_{T}^{2}\text{C}_{L}|_{(Y=17)} + \text{U}_{T}^{2}\text{C}_{L}|_{(Y=23.1)}$$

$$(6-127)$$

$$L_{FR} = \frac{1}{2} \left( \sum_{\Psi} L_{Y_{FR}} \right) [1 + f(H) \cdot f(\Psi_{T})] 1.10 f(U) \qquad (6-128)$$

$$L_{AR} = 1.19 \text{L}_{FR} \cdot \frac{A_{O_{3}_{AR}}}{A_{O_{3}_{FR}}} \cdot f(U) \cdot f(V) \cdot f(A_{O_{3}_{FR}})$$

$$+ f(A_{O_{3}_{FR}}) [L_{FR} + 1000 \Delta A_{O_{3}}] + 1000 |\Delta A_{O_{6}}| K_{FRS} + 2000 \text{ Q}_{1}$$

(6-129)

$$K_{\overline{F}RS}$$
 = 1.0 when  $L_{\overline{F}R} \ge L_{MAX}$ 

$$L_{AR} - L'_{AR}$$
 when  $L'_{AR} \leq L'_{MAX}$ 

$$L_{\text{MAX}} = (6.5 \times 10^6) \rho \cdot f(U)$$

# DyFR, FXFR, FXAR Rotor (X) Forces

$$D_{\Psi_{FR}} = \rho \left[ (7.13 \ U_{T}^{2}C_{D}|_{(\Upsilon-7.3)} - 7.5 \ U_{T}U_{P}C_{L}|_{(\Upsilon-7.3)} \right]$$

$$+ (4.38 \ U_{T}^{2}C_{D}|_{(\Upsilon-17)FR} - 7.8 \ U_{T}U_{P}C_{L}|_{(\Upsilon-17)}$$

$$+ (6.37 \ U_{T}^{2}C_{D}|_{(\Upsilon-23.1)} - U_{T}U_{P}C_{L}|_{(\Upsilon-23.1)} \right]$$

$$F_{X_{\overline{PR}}} = \frac{1}{2} \sum_{\Psi} (.0173 \ \beta_{\overline{Y}} L_{\overline{Y}R} \cos Y - D_{\underline{Y}} \sin Y)$$
 (6-131)

$$\mathbf{F}_{\mathbf{AR}} \sim \mathbf{F}_{\mathbf{FR}} + 300 \, \mathbf{f}(\mathbf{U}) \cdot \mathbf{f}(\mathbf{V}) \cdot \mathbf{f}(\mathbf{Q}) \Delta \mathbf{B}_{\mathbf{18}}$$

# F<sub>YFR</sub>, F<sub>YAR</sub> Rotor (Y) Forces

$$\mathbf{F}_{\mathbf{YR}} = \frac{1}{2} \sum_{\mathbf{Y}} [-D_{\mathbf{Y}} \cos \mathbf{Y} - .O173 \beta_{\mathbf{Y}} \mathbf{L}_{\mathbf{Y}} \sin \mathbf{Y}]$$
 (6-133)

$$\mathbf{F}_{\mathbf{A}\mathbf{R}} = \mathbf{F}_{\mathbf{Y}\mathbf{F}\mathbf{R}} + 300 \ \mathbf{f}(\mathbf{U}) \cdot \mathbf{f}(\mathbf{V}) \cdot \mathbf{f}(\mathbf{E}) \ \Delta \mathbf{A}_{\mathbf{B}}$$
 (6-134)

$$C_{L_{y-y}} = K_1 f(\alpha_{y-y})$$
 i = 1, 2, 3, 4,5 (6-135)

$$U_{\mathbf{T}_{\psi-\mathbf{y}}}^{2} C_{\mathbf{D}(\psi-\mathbf{y})} = \mathbf{f}(\alpha_{\psi-\mathbf{y}}, U_{\mathbf{T}_{\psi-\mathbf{y}}})$$
 (6-136)

# $\beta_{\underline{Y}}$ , Flap Angle, FR, $\beta_{\underline{Y}}$

$$\beta_{\frac{Y}{YR}} = 57.3(a_{0s_{\frac{Y}{YR}}} - a_{1s_{\frac{Y}{YR}}} \cos Y - b_{1s_{\frac{Y}{YR}}} \sin Y) \deg.$$
 (6-137)

$$\hat{\beta}_{Y} = 57.3\Omega(a_{18} \sin Y - b_{18} \cos Y) \text{ deg/sec.}$$
 (6-138)

# a<sub>O3</sub>, a<sub>ls</sub>, b<sub>ls</sub>, Flap Angle Fourier Coefficients

$$^{8}Os_{FR} = \frac{\frac{M_{\beta}O_{FR} + M_{\beta}60_{FR} + M_{\beta}12O_{FR} + M_{\beta}18O_{FR} + M_{\beta}2U_{O}_{FR} + M_{\beta}3OO_{FR}}{U,550,253}$$
(6-139)

$$+ b_{18} (.390) - 1.028q_1$$
 (6-140)

$$\frac{\frac{\text{MB}_{\text{O}_{\text{FR}}} \cdot 0.5 \text{ Mg}_{\text{O}_{\text{FR}}} - 0.5 \text{ Mg}_{\text{O}_{\text{FR}}} - 0.5 \text{ Mg}_{\text{O}_{\text{FR}}} + 0.5 \text{ Mg}_{\text{O}_{\text{FR}}}}{180_{\text{FR}}} + \frac{0.5 \text{ Mg}_{\text{O}_{\text{FR}}} + 0.5 \text{ Mg}_{\text{O}_{\text{FR}}}}{160_{\text{Oli}3}} + \frac{0.5 \text{ Mg}_{\text{O}_{\text{FR}}} + 0.5 \text{ Mg}_{\text{O}_{\text{FR}}}}{160_{\text{FR}}} + \frac{0.5 \text{ Mg$$

$$\gamma_{FRH} = -.2125 \sum_{\psi} (L_{YFR} \sin \tau) + 11 \Lambda^2 b_{18_{FR}}$$
 (6-11/2)

$$H_{FRH} = -.2125 \sum_{Y} I_{\overline{MR}} \cos Y + \ln \Omega^2 a_{1a_{\overline{YR}}}$$
 (6-144)

$$\mathbf{H}_{\mathbf{ARH}} = \mathbf{H}_{\mathbf{FRH}} + \mathbf{K} \Delta \mathbf{E}_{\mathbf{1a}} \tag{6-145}$$

$$\frac{W_{1}}{(\psi-y)} = (W_{1}) \times \left(\frac{W_{1}}{W_{1}}\right) \times \left(1 + \frac{y^{\prime\prime}}{h690} \cos \psi - \frac{y^{\prime\prime}}{h690} \sin \psi\right) \times \left(6-1h5a\right)$$

#### (12) TRANSIATIONAL AND ARRUIAR RATES

 $U_0 = / \begin{bmatrix} \frac{X_0}{H_1} - g \sin (\theta - 9.5) \end{bmatrix} dt$  (6-146)

$$V_0 = \int \left[ \frac{Y_a}{H_1} + g \cos (\theta - 9.5) \sin \theta - T_0 r \right] dt$$
 (6-147)

$$W_0 = \int \left[ \frac{z_a}{H_1} + g \cos (\theta - 9.5) \cos \theta + V_0 q_1 \right] dt$$
 (6-148)

#### MAVTRAINVCKR 1205-3

# N. E. h Earth Axes Velocities

$$\dot{V} = \cos T \left( U_{(1)} \cos \left( \theta_{p} - 9.5 \right) + \sin \left( \theta_{p} 9.5 \right) \left( V_{(1)} \sin \theta + V_{(2)} \cos \theta \right) \right)$$

$$- \sin T \left( V_{(1)} \cos \theta - V_{(1)} \sin \theta \right) \qquad (6-1)(9)$$

$$\dot{z} = \sin Y \left( V_{0} \cos \left( \theta_{\phi} - V_{0} \right) + \sin \left( \theta_{\phi} V_{0} \right) \right)$$

$$+ \cos Y \left( V_{0} \cos \Phi - V_{0} \sin \Phi \right)$$

$$(6-150)$$

$$h = V_0 \sin (0_{p}-9.5) \sim \cos (0_{p}-9.5)(V_0 \sin \theta + V_0 \cos \theta)$$
 (6-151)

### Wind Velocity in Body Area

Wind Move from Tw Hunding (True) at Villeso

No Vertical Compensat of Wind is Considered

$$- 7 - 7 - 9 - 9.5$$
 occ  $(7 - 7 + 180^{\circ})$  (6-152)

### Relative Velocity in Air in Body Area

$$v = v_0 + v_{1}$$
 (6-155)

$$\nabla = \nabla_{\Omega} + \nabla_{\Omega} \tag{6-156}$$

#### Puselage Angular Rates

$$q_1 = \sqrt{\frac{M_{\rm a}}{T_{\rm yy}}} \, dt \tag{6-159}$$

$$r = \int \frac{N_a}{T_{max}} dt \qquad (6-160)$$

#### Mean Inflow Velocity

$$W_{1(mean)PR}^{'} = \frac{.00028 \text{ L}_{PR}^{'}}{\cancel{P} \text{ V}_{T}^{'}} .00028 - \frac{1}{2 \text{ W}_{R}^{2}}$$
 (6-161)

### 2 Rotor Angular Velocity

### North and Rast Positions, Altitude

$$N - \int N dt \qquad (6-163)$$

$$\mathbf{z} = \int \mathbf{E} \, d\mathbf{t} \tag{6-16} \mathbf{L}$$

$$h = \int h dt$$
 (6-165)

### Heading Angle

$$\bar{T} = (r \cos \Phi + q_1 \sin \Phi) \sec (\theta_p - 9.5) RONS/SEC (6-166)$$

### Fitch Angle

$$\theta = q_1 \cos \phi - r \sin \phi$$
 RINS/SEC (6-167)

### Roll Angle

$$\Phi = p \cdot \psi \sin (\theta_p - 9.5)$$
 RDNS/SEC (6-168)

$$\Phi = 57.3 / \Phi \text{ dt}$$

## dx, dy, dz, Center of Gravity Position

$$dx = .300 - .00687 (M_{f_R} + M_{f_L}) + f (INST)$$

$$dy = [5.11 M_{f_R} - 5.11 M_{f_L}]/M_1$$

$$dz = 0$$
(6-169)

#### . V/STOL AIRCRAFT (TILT-WING)

#### 1. NOMENCIATURE USED IN KC-142A EQUATIONS

Symbol	Definition
b	Wing Span
•	Mean Aerodynamic Chord
it	Incidence Angle Horisontal Stabiliser
1,	Incidence Angle - Wing
r.	Main Propellers n=1, 2, 3, 4 - Top View Laft to Right, looking forward
q	Dynamic Pressure - Free Stream
<sup>Q</sup> HS	Dynamic Pressure at Horisontal Stabiliser
₫ <sub>V</sub> Ţ	Bynamic Pressure at Vertical Tail
٩.	Dynamic Pressure due to Power on Wing Effects
P <sub>n</sub>	Flade Pitch Angle - Main Propeller
<sup>©</sup> T,S	Coefficient of Thrust at Wing Due to Inflow Velocity
$\mathbf{p}_{\mathbf{n}}$	Diameter Main Propeller
D <sub>TR</sub>	Diameter Tail Rotor
7	Puselage
HS	Horizontal Stabiliser
" <b>E</b>	Inertia of Main Propellar Hlades and Shaft
TR	Inertia of Tail Rotor Mades and Shaft
$\mathbf{J_n}$	Advance Ratio Main Propeller

Symbol	Definition
J <sub>TR</sub>	Advance Ratio Tail Propeller or Rotor
rt <sub>n</sub>	Main Propeller Moment (Initially Pitching)
N <sub>n</sub>	Main Propeller Thrust Component Normal to T
N <sub>n</sub>	RFM - Main Propeller
No	Nominal RPM - Main Propeller
N <sub>TR</sub>	RPM - Tail Propeller
Q <sub>n</sub>	Main Propeller Torque Coefficient
\$	Total Area of Wing
S <sub>p</sub>	Total Area of Main Propeller Disks
Ť	Total Thrust of Main Propellers
Tn	Main Propeller Thrust
TR	Tail Propeller or Rotor
? <sub>TR</sub>	Thrust - Tail Rotor
♥ <sub>B</sub>	Total Velocity in Aircraft Body Axes
VT	Vertical Tail
<b>V</b>	Total Velocity in wind Stability Axes
W	Wing
Yn	Main Propeller Moment (Initially Turning)
a <sub>F</sub>	Angle of Attack - Puselage
<sup>a</sup> H5	Angle of Attack - Horisontal Stabiliser
<b>~</b>	Angle of Attack - Wing
$oldsymbol{eta}_{\scriptscriptstyle  extsf{F}}$	Sideslip Angle - Fuselage
<b>T</b> R	Hlade Pitch Angle - Tail Rotor
B.	Sideslip Angle - Wing
E	Downwash Angle

#### NAVTRACEVOEN 1205-3

Symbol	Definition
₽.	Angular Velocity Main Propeller
<b>≜</b> e	Angular Acceleration Main Propeller
I <sub>TR</sub>	Inertia of tail rotor blades and shaft
2 <sub>TR</sub>	Angular velocity tail rotor
TR	Angular Acceleration Tail Rotor

#### 2. TILT WING AIRCRAFT SIMULATION EQUATION

#### a. AERODYNAMIC VARIABLES

$$\alpha_{\rm F} = \tan^{-1} \left( \frac{\rm W}{\rm U} \right) \tag{6-170}$$

$$\beta_F = \tan^{-1} \left( \frac{V}{V_0^2 + V^2} \right)$$
 (6-171)

$$v_{B} = \sqrt{v^2 + w^2 + v^2}$$

$$q = 1/2 \rho v_p^2$$
 (6-173)

### b. MAIN PROPFILER AFRODINAMICS

$$\psi_{0} = (i_{W} + a_{\overline{F}})$$
 (6-175)

 $u_n = V_R \cos \beta_F \cos \psi_o - y_n(p \sin i_w + r \cos i_w)$ 

$$+ x_{n}q_{1} \sin i_{w} + s_{n}q_{1} \cos i_{w}$$
 (6-176)

$$\mathbf{v}_{\mathbf{n}} = \mathbf{v}_{\mathbf{n}} \sin \beta_{\mathbf{F}} \tag{6-177}$$

$$\mathbf{w}_{n} = \mathbf{v}_{B} \cos \beta_{p} \sin \phi_{o} * \mathbf{y}_{n} (p \cos i_{w} - r \sin i_{w})$$

$$-x_nq_1\cos x_w + s_nq_1\sin x_w$$
 (4-178)

$$J_{n} = \frac{60}{N_{n}D} V_{n} \tag{5-179}$$

$$v_n = \sqrt{u_n^2 \cdot v_n^2 \cdot v_n^2}$$

$$J_n' = J_n \cos \psi_n = (\frac{60}{D}) (\frac{u_n}{N_n})$$
 (6-180)

$$J_{n} \sin \psi_{n} = (\frac{60}{D}) (\sqrt{\frac{v_{n}^{2} + v_{n}^{2}}{v_{n}}})$$
 (6-181)

$$C_{T_n} = C_{T_0} \cdot \frac{\int_{J'}^{C_T} J'_n}{\int_{J'}^{J'} J'_n} + \frac{\int_{J'}^{2} C_{T}}{\int_{J'}^{2} J'_n} (J'_n)^2 + \frac{\int_{J'}^{C_T} C_{T}}{\int_{B}^{B} B_n} + \frac{\int_{J'}^{2} C_{T}}{\int_{B}^{B} J'_n} B_n J'_n$$
 (6-182)

$$C_{p_{n}} = C_{p_{n}} + \frac{3C_{p}}{JJ'}J'_{n} + \frac{3^{2}C_{p}}{JJ'^{2}}(J'_{n})^{2} + \frac{3C_{p}}{B}B_{n} + \frac{3^{2}C_{p}}{BJ'}B_{n}J'_{n}$$
 (6-183)

$$C_{N_n} = \frac{3}{35} \left[ \frac{3(C_N \cot \psi)}{J_J'} \right] B_n J_n \sin \psi_n$$
 (6-184)

$$C_{Y_n} = \int_{B}^{\infty} \left[\frac{\partial (C_{Y \text{ cot } \psi})}{\partial J'}\right] B_n J_n \sin \psi_n + \frac{\partial}{\partial J'}$$

$$\left[\frac{\mathcal{J}(^{C}Y \cot \psi)}{\mathcal{J}J}\right]J_{n}J_{n} \sin \psi_{n} \tag{6-185}$$

$$c_{M_n} = \frac{3}{3J'} \left( \frac{3^n M}{3^n} \right) + J_n'$$
 (6-186)

$$T_n = D^{1/2} \left(\frac{K_n}{N_0}\right)^2 \left(\frac{P_0}{P_0}\right) C_{T_{1/2}}$$
 (6-187)

$$N_n = D^{\perp} \left(\frac{N_n}{N_0}\right)^2 \left(\frac{P_0}{P_0}\right) \gamma_{N_n}$$
 (6-188)

$$Y_n - D^5 \left(\frac{N_n}{N_o}\right)^2 \left(\frac{P_o}{P_o}\right) C_{Y_n}$$
 (6-189)

$$M_n = D^5 \left(\frac{N_n}{N_0}\right)^2 \left(\frac{P}{P_0}\right) \gamma_{M_n}$$
 (6-190)

$$Q_{n} = \frac{D^{5}}{2^{-3}n} \left(\frac{N_{n}}{N_{0}}\right)^{2} \left($$

$$(\Delta T_n) = \sum_{n=1}^{L} (T_n \cos t_n - N_n \cos \beta_n \sin t_n)$$
 (6-192)

$$(\Delta T_n) = \sum_{n=1}^{l_1} (-N_n \sin \beta_n)$$
 (6-193)

$$(\Delta Z_n)_p = \sum_{n=1}^{t_1} (-T_n \sin i_n - N_n \cos \beta_n \cos i_n)$$
 (6-194)

$$(\Delta \mathbf{I}_{a})_{p} = \{(\Delta \mathbf{I}_{a})_{p1} - (\Delta \mathbf{I}_{a})_{p1}\} \mathbf{y}_{1} - \{(\Delta \mathbf{I}_{a})_{p2} - (\Delta \mathbf{I}_{a})_{p3}\} \mathbf{y}_{2}$$

$$- \{(\Delta \mathbf{I}_{a})_{p1} + (\Delta \mathbf{I}_{a})_{p1}\} \mathbf{x}_{1} - \{(\Delta \mathbf{I}_{a})_{p2} + (\Delta \mathbf{I}_{a})_{p3}\} \mathbf{x}_{2}$$

$$= \sum_{n=1}^{l_1} (\mathbf{X}_n \cos \beta_n) \sin i_w - \sum_{n=1}^{l_1} (\mathbf{M}_n \sin \beta_n) \sin i_w$$

$$(\Delta M_a)_p = M_{T_{\text{Pivot}}} + \sum_{n=1}^{l_1} T_n(\cos i_w) *_{\text{Pivot}} + \sum_{n=1}^{l_2} T_n(\sin i_w) *_{\text{Pivot}}$$

- 
$$(N_1 \cos \beta_1 \sin i_w + N_1 \cos \beta_i \sin i_w) Z_1$$

- 
$$(N_2 \cos \beta_2 \sin i_w + H_3 \cos \beta_3 \sin i_w) Z_2$$
 (6-196)

+ 
$$(N_1 \cos \beta_1 \cos i_w + N_{\tilde{l}_1} \cos \beta_{\tilde{l}_2} \cos i_w) X_1$$

+ 
$$(N_2 \cos \beta_2 \cos i_w + N_3 \cos \beta_3 \cos i_w) \chi_2$$

$$= \sum_{n=1}^{L} (\mathbf{I}_n \sin \beta_n) + \sum_{n=1}^{L} (\mathbf{M}_n \cos \beta_n)$$

where 
$$M_{\text{Pivot}} = 1.825(T_1 + T_1) + 1.092(T_2 + T_1)$$

$$\frac{(\Delta X_{a})_{p} = -[(\Delta X_{a})_{p}] - (\Delta X_{a})_{p}]_{p}}{+[(\Delta Y_{a})_{p}] + (\Delta Y_{a})_{p}]_{p}} = \frac{(\Delta X_{a})_{p}}{+[(\Delta Y_{a})_{p}]_{p}} \times \frac{(\Delta Y_{a})_{p}}{+[(\Delta Y_{a})_{p}]_{p}} \times \frac{(\Delta Y_{a})_{p}}{+$$

### c. WING AERODYNAMICS

$$\frac{W}{p} = \frac{W}{W} = -0 \sin i_W + W \cos i_W$$
 (6-198)

$$u_p = U \cos i_w + W \sin i_w = V_B$$
 (6-199)

$$V = (u_p + \Delta V)$$
  $V = V_w$  (6-200)

$$\Delta V = u_p + (u_p^2 + \frac{2T}{\sqrt{20p}})$$
 (6-201)

$$c_{T,S} = T/Q_{Sp}$$
 (6-202)

$$q_{w} = (q + T/S_p)$$
 (6-203)

$$V_{w} = (v_{p}^{2} + (v_{p} + \Delta V)^{2} + v_{w}^{2})^{-1/2}$$
(6-204)

$$a_{\rm w} = \tan^{-1} \left( \frac{p}{u_{\rm p} + \Delta V} \right)$$
 (6-205)

$$\beta_{\rm W} = \tan^{-1} \frac{\rm V}{\left[\left(u_{\rm p} + \Delta \rm V\right)^2 + w_{\rm p}^2\right]^{1/2}}$$
 (6-206)

$$C_D = C_D + K C_L^2 + C_{D_{\overline{OP}}} + \delta P + \frac{\lambda^2}{3} \frac{C_D}{\delta^2 P} + \delta^2 P$$
 (6-207)

$$c_{L} = c_{L_{0}} + c_{L_{0}$$

$$(c_{m_{W}}) + c_{m_{O}} + c_{m_{OF}} \cdot \delta F + \frac{c}{22m_{W}} c_{m_{Q_{1}}} \cdot q_{1}$$
 (6-210)

$$(c_{n_{v}}) + c_{n_{p_{v}}} \cdot \beta_{v} + c_{n_{p_{v}}} \cdot \delta_{A} + \frac{b}{2V_{v}} c_{n_{p_{v}}} \cdot p_{v} + \frac{b}{2V_{v}} c_{n_{p_{v}}} \cdot r_{v}$$
 (6-211)

#### In Rody Axes

$$(C_X) = C_D \cos \left\{ -C_L \sin \right\}$$
  $\left\{ -i_L - a_L \right\}$  (6-212)

$$(c_z) = c_D \sin \zeta - c_L \cos \zeta$$
 (6-213)

$$(c_{\mathcal{Q}})_{n} = (c_{\mathcal{Q}}) \cos \beta + (c_{n}) \sin \beta$$
 (6-2.4)

$$(c_{x}) = (c_{x}) - \frac{ac}{c}(c_{x}) + \frac{ac}{c}(c_{x})$$
 (6>215)

$$(C_n) = -(C_n) \sin \beta + (C_n) \cos \beta$$
 (6-216)

$$(\Delta T_{a}) = (C_{T,B}) + (C_{$$

$$(\Delta Z_s) = (C_{Z_s} + C_{Z_s})$$
 (6-218)

$$(\Delta L_a) = (C_{\ell}) b 3 [f(C_{T,S})] q$$
 (6-219)

$$(\Delta M_{\bullet}) = (C_{m}) = S[f(C_{T,S})] Q_{\bullet}$$
 (6-220)

$$(\Delta h_n) = (c_n) b S \{f(c_{T,S})\} q_n$$
 (6-221)

## d. VERTICAL STABILIZER AERODYNAMICS

$$c_{\mathbf{Y}} - c_{\mathbf{Y}_{\kappa_{\mathbf{R}}}} \cdot \beta_{\mathbf{F}} + c_{\mathbf{Y}_{\kappa_{\mathbf{R}}}} \cdot \delta_{\mathbf{R}} \qquad (6-222)$$

$$C_{L} = C_{L_{p}} \cdot \beta + C_{L_{p}} \cdot \delta R + \frac{b}{2L_{p}} [C_{L_{p}} \cdot p + C_{L_{p}} \cdot r]$$
 (6-223)

$$C_{n} = C_{n_{p_{r}}} \cdot \beta r + C_{n_{p_{r}}} \cdot \delta R + \frac{b}{2T_{p}} \left[C_{n_{p_{r}}} \cdot n + C_{n_{p_{r}}} \cdot r\right]$$
 (6-224)

$$(\Delta \mathbf{x}_{\mathbf{q}})_{\mathbf{v}\mathbf{t}} = C_{\mathbf{x}}^{c} \left(\frac{q_{\mathbf{v}\mathbf{t}}}{q}\right) \mathbf{q} \tag{6-225}$$

$$(\Lambda L_a)_{\psi t} = G_{\chi} SS \left(\frac{Q_{\psi t}}{Q}\right) Q \qquad (6-226)$$

$$(\Delta N_a) = C_n bs \left(\frac{q_{vt}}{q}\right)q$$
 (6-227)

#### e. HORIZONTAL STABILIZER AEROLTNAMICS

$$a_t = a_p + i_t - \epsilon \tag{6-228}$$

$$C_{L_{t}} = C_{L_{\alpha_{t}}} \cdot \alpha_{t} \tag{6-229}$$

$$c_{p_{t}} = c_{p_{o_{t}}} + \kappa_{t} (c_{L_{g}})^{2}$$
 (6-230)

$$(\Delta \mathbf{x}_{\mathbf{a}})_{HS} = -\left\{C_{D_{\mathbf{t}}}\cos\left(\mathbf{1}_{\mathbf{t}} - \mathbf{a}_{\mathbf{t}}\right) + C_{\mathbf{L}_{\mathbf{t}}}\sin\left(\mathbf{1}_{\mathbf{t}} - \mathbf{a}_{\mathbf{t}}\right)\right\} \cdot S\left(\frac{\mathbf{q}_{\mathbf{S}}}{\mathbf{q}}\right)\mathbf{q}$$
 (6-231)

$$(\Delta Z_{\mathbf{a}})_{\mathbf{HS}} = \{ + C_{\mathbf{D}_{\mathbf{t}}} \sin (\mathbf{i}_{\mathbf{t}} - \alpha_{\mathbf{t}}) - C_{\mathbf{L}_{\mathbf{t}}} \cos (\mathbf{i}_{\mathbf{t}} - \alpha_{\mathbf{t}}) \} S (\frac{\mathbf{q}_{\mathbf{HS}}}{\mathbf{q}}) \mathbf{q}$$
 (6-232)

$$(\Delta M_a)_{HS} = -(\Delta I_a)_{HS} + (\Delta I_a)_{HS} + (\Delta I_a)_{HS} + \frac{c^2 s \rho}{l_1}$$
 (6-233)

$$\{c_{\mathbf{m}_{\dot{\alpha}_1}} \cdot \mathbf{a}_1 \, \mathbf{X}_{\dot{\beta}} + c_{\mathbf{m}_{\dot{\alpha}}} \cdot \dot{\mathbf{w}}\}$$

#### f. TAIL ROTOR AEROUTHAMICS

$$(*_{0})_{TR} = 90 + (a_{F} - \epsilon)$$
 (6-234)

$$u_{\overline{TR}} = V_{\beta} \sin \left( \phi_{0} \right)$$
 (6-235)

$$\mathbf{w}_{IR} = \mathbf{I}_{B} \cos \left(\mathbf{v}_{o}\right)_{IR} - \mathbf{l}_{IR} \mathbf{q}_{1} \tag{6-236}$$

$$J_{TR} = \left(\frac{6C}{D_{TR}}\right) \frac{\Psi_{TR}}{K_{TR}} \tag{6-237}$$

$$J_{\overline{TR}}' = (\frac{60}{\overline{D}_{rR}}) \left(\frac{-\overline{TR}}{N_{\overline{TR}}}\right) \tag{6-238}$$

$$\underline{\mathbf{y}}_{TR} = (\underline{\mathbf{u}}_{TR} + \underline{\mathbf{w}}_{TR}^2)^{-1/2}$$
(6-239)

$$C_{T_{\overline{TR}}} = C_{T_{\overline{TR}}} (B_{\overline{TR}}) + \frac{3 C_{T_{\overline{TR}}}}{3 J_{\overline{TR}}'} (J_{\overline{TR}}')$$
(6-240)

$$c_{P_{TR}} = \frac{3^2 c_{P}}{3 E_{TR}^2} (E_{TR})^2$$
 (6-261)

$$T_{TR} = \Gamma_{TR}^{L} \left( \frac{P}{P_0} \right) \left( \frac{N_{TR}}{N_{O_{TR}}} \right)^2 C_{T_{TR}}$$
 (6-242)

$$c_{TR} = c_{TR}^{5} \left( \frac{1}{N_{o_{TR}}} \right)^{2} c_{P_{TR}}$$
 (6-243)

$$(\Delta Z_{\underline{a}})_{TR} = T_{TR}$$
 (6-214)

$$(\Delta M_{\rm a})_{\rm TR} = T_{\rm TR} I_{\rm TR} \tag{6-245}$$

$$(\Delta N_{\bullet})_{TR} = Q_{TR}$$
 (6-246)

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$$(\Delta \mathbf{I}_{\mathbf{a}})_{\mathbf{p}} = -q S C_{\mathbf{p}}$$
 (6-247)

$$(AT_a)_F - q S C_{Y\beta_F} \cdot \beta_F$$
 (6-248)

$$(\Delta Z_{\mathbf{a}})_{\mathbf{p}} = -\mathbf{q} \cdot \mathbf{S} \cdot \mathbf{C}_{\mathbf{L}_{\mathbf{a}_{\mathbf{p}}}} \cdot \mathbf{a}_{\mathbf{p}}$$
 (6-249)

$$(\Delta M_{\alpha}) = qSe(C_{m} + C_{\alpha} \cdot \alpha_{p}) \qquad (6-250)$$

$$(\Delta N_a)_F = q Sb C_{n_{\beta_F}}$$
.  $\beta_F$  (6-251)

 $C_{D_0}$ ,  $C_{L_{\frac{1}{2}}}$ ,  $C_{m_0}$  and  $C_{n_0}$  also have effects in the wing carodynamics.

#### h. TILT WIND AIRCRAFT FORCE AND MOMENT EQUATIONS

#### (1) I Force Equation

$$C_{\mathbf{X}}S\{f(C_{\mathbf{T},S})\}q_{w} + \sum_{n=1}^{L} (T_{n} \cos i_{w} - N_{n} \cos \beta_{n} \sin i_{w})$$

$$-\{C_{D_{t}} \cos(i_{t} - \alpha_{t}) + C_{L_{t}} \sin(i_{t} - \alpha_{t})\} Sq(\frac{q_{HS}}{q}) - SqC_{D_{O}}$$

$$-m(U + Mq_{1} - Vr) + mg \sin n \theta$$

### (2) I Force Equation

$$\sum_{n=1}^{l_{\parallel}} (-N_n \sin \beta_n) + C_{\underline{y}} \operatorname{Sq}(\frac{q_{\underline{y}t}}{q}) + \operatorname{SqC}_{\underline{y}}, \beta_{\underline{y}}$$

$$= m(V + Ur - Wp) - mg \cos \theta \sin \Phi$$

### (3) 2 Force Equation

$$\begin{aligned} & C_{Z_{p}^{q}}[f(C_{T_{p}^{q}})]q_{p} + \sum_{n=1}^{L} (-T_{n} \sin i_{p} - N_{n} \cos \beta_{n} \cos i_{p}) \\ & + [C_{D_{t}} \sin (i_{t} - \alpha_{t}) - C_{L_{t}} \cos (i_{t} - \alpha_{t})] Sq(\frac{q_{HS}}{q}) + T_{TR} - SqC_{L_{\alpha_{p}}} \\ & - m(\mathring{\Psi} + \nabla p - Uq_{1}) - mg \cos \theta \cos \theta \end{aligned}$$

### (1) Roll Equation

$$\begin{array}{l} \text{C}_{A} \text{ bS}[f(C_{T,S})] \ q_{A} \\ + \{(+T_{1} \sin i_{A} + N_{1} \cos \beta_{1} \cos i_{A}) - (+T_{1} \sin i_{A} + N_{1} \cos \beta_{1} \cos i_{A})\}y_{1} \\ + \{(+T_{1} \sin i_{A} + N_{1} \cos \beta_{1} \cos i_{A}) - (+T_{3} \sin i_{A} + N_{3} \cos \beta_{3} \cos i_{A})\}y_{2} \\ + \{(+N_{1} \sin \beta_{1} + N_{1} \sin \beta_{1}) \ z_{1} + (+N_{2} \sin \beta_{2} + N_{3} \sin \beta_{3}) \ z_{2} \\ + \sum_{n=1}^{L} (Y_{n} \cos \beta_{n}) \ \sin i_{A} - \sum_{n=1}^{L} (M_{n} \sin \beta_{n}) \ \sin i_{A} + C_{A}b \ Sq(\frac{q_{vt}}{q}) \\ + I_{11}p \ + I_{13}(r + pq_{1}) + (I_{13} - I_{22}) \ q_{1}r + (I_{24} + \cos i_{A}) \\ + q_{1}(I_{2}\beta_{R}) \ \sin i_{A} + q_{1}I_{1R}\beta_{1R} \end{array}$$

### (5) Pitch Equation

$$C_{m} cs[f(C_{T,S})] q_{w}$$

$$+ M_{Tpivot} + \sum_{i} T_{n}(\cos i_{w}) z_{pivot} + \sum_{i} T_{n}(\sin i_{w}) x_{pivot}$$

$$-(N_{1} \cos \beta_{1} \sin i_{w} + N_{1} \cos \beta_{1} \sin i_{w}) z_{1}$$

$$-(N_2 \cos \beta_2 \sin \frac{1}{4} + N_3 \cos \beta_3 \sin \frac{1}{4}) s_2$$

$$+(\aleph_1 \cos \beta_1 \cos \frac{1}{2} + \aleph_1 \cos \beta_1 \cos \frac{1}{2}) x_1$$

+
$$(N_2 \cos \beta_2 \cos i_1 + N_3 \cos \beta_3 \cos i_1)x_2 - \sum_{n=1}^{l_1} (Y_n \sin \beta_n)$$
  
+  $\sum_{n=1}^{l_2} (M_n \cos \beta_n)$ 

+[
$$C_{D_{\xi}} \cos (i_{\xi} - \alpha_{\xi}) + C_{L_{\xi}} \sin (i_{\xi} - \alpha_{\xi})$$
]  $Sq(\frac{q_{HS}}{q})$   $h_{HS}$ 

+[
$$C_{D_t} \sin(i_t - a_t) - C_{L_t} \cos(i_t - a_t)] Sq(\frac{q_{HS}}{q})$$
  $1_{HS}$ 

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$$+ \frac{c^{2}s\rho}{l_{1}} \left[ c_{m_{1}} \cdot q_{1}X_{p_{1}} + c_{m_{1}} \cdot u_{1} \right] + T_{TR} L_{TR} + qSc(C_{m_{1}} \cdot c_{m_{1}} \cdot a_{p_{1}})$$

$$= L_{22}\dot{q} - L_{23}(n^{2} - p^{2}) + (L_{12} - L_{33}) + p(L_{23}) \sin i_{w} + r(L_{23}) \cos i_{w}$$

#### (6) Year Equation

$$\begin{array}{l} C_{n_{w}} bS\{f(G_{T,3})\}_{Q_{w}} \\ -[(T_{1}\cos i_{w} - M_{1}\cos\beta_{1}\sin i_{w}) - (T_{1}\cos i_{w} - M_{1}\cos\beta_{1}\sin i_{w})\} y_{1} \\ -[(T_{2}\cos i_{w} - M_{2}\cos\beta_{2}\sin i_{w}) - (T_{3}\cos i_{w} - M_{3}\cos\beta_{3}\sin i_{w})] y_{2} \\ -(+M_{1}\sin\beta_{1} + M_{1}\sin\beta_{1})x_{1} - (+M_{2}\sin\beta_{2} + M_{3}\sin\beta_{3})x_{2} \\ -\sum_{n=1}^{k} (T_{n}\cos\beta_{n})\cos i_{w} - \sum_{n=1}^{k} (M_{n}\sin\beta_{n})\cos i_{w} \\ + C_{n}bR(\frac{Q_{v_{1}}}{Q}) + QSbC_{n_{p}} \cdot A_{p} + C_{TR} \\ = I_{33}\dot{r} + I_{13} (\dot{p} - Q_{1}) + (I_{22} - I_{11}) PQ_{1} \\ -(I_{2}\dot{q}) \sin i_{w} - Q_{1}(I_{2}\dot{q}_{8}) \cos i_{w} - pI_{TR}\dot{q}_{1R} \end{array}$$

No simplifications have been made on the right side of these six equations. Terms ignored in mechanisation are those with diagonal line through them. External stores, rough air, or landing gear conditions are not developed in these equations.

NOTE: In equations 6-217 to 6-221 and equations 1, 3-6 of the preceding force and moment equations,  $\{f(C_{T,S}), q_{w}\}$  is a dynamic pressure term due to propeller slipstream.  $C_{T,S}$  is the coefficient of thrust due to the induced wing velocity  $\delta V$ , coefficient by the propeller slipstream, giving an increased lift effect. With engines off,  $\{f(C_{T,S}), q_{w}\} \geq 1.00$  and equations 6-217 to 6-221 become force and moment equations as would be expected for jet aircraft.  $C_{T,S}$  is a  $f(V_{B})$  and dependent on wing tilt and wing flap angles?